

Coupled channel effect in elastic scattering and fusion for ${}^{6,7}\text{Li}+{}^{28}\text{Si}$

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Abstract. The fusion excitation and elastic angular distribution were measured for ${}^{6,7}\text{Li}+{}^{28}\text{Si}$ from below to above Coulomb barrier ($\leq 3V_b$) energies. The barrier distribution derived from the fusion data was found to be broad and asymmetric at the sub-barrier region, compared to 1D BPM estimation. Effect of rotational coupling on fusion was found to be not so dominant. Phenomenological optical potential parameters, with surface and volume type imaginary potentials, were obtained from fitting of elastic scattering data and energy dependence of real and imaginary surface strengths were investigated around the barrier. CDCC calculations considering only breakup of projectile were performed for ${}^{6,7}\text{Li}+{}^{28}\text{Si}$ with the elastic scattering data, using the code FRESKO. The effects of breakup of projectile on elastic cross section do not agree with the energy dependence of real and imaginary strength with volume type imaginary potential around the barrier.

1 Introduction

The reaction dynamics of loosely bound projectiles with light mass target at near barrier energies is very important and not yet fully understood. The measured fusion cross section at above barrier energies showed suppression [1, 2] when compared with one dimensional barrier penetration model (1D BPM), whereas the same were enhanced at sub barrier energies [2, 3]. On the otherhand, the near barrier behaviour of the interaction potential for ${}^{6,7}\text{Li}+{}^{28}\text{Si}$ [4, 5] as a function of energy was found to be quite different compared to the observations with heavier targets. Recently, a simultaneous description of the elastic, fusion and reaction cross sections has been made by A. Gomez Camacho *et al.* for the same system [6] with phenomenological approach, where the nuclear polarization potential is split into a volume and a surface part to understand the energy dependence of the OM potential in terms of different polarization potentials. So for such light systems with reduced Coulomb strength, the influence of breakup and other direct reactions (e.g. transfer) on fusion, elastic scattering and barrier distribution is definitely interesting to probe the interplay of the different processes. With this motivation we present the results of the measurements and analysis of elastic cross sections for the ${}^{6,7}\text{Li}+{}^{28}\text{Si}$ systems. The effect of breakup on elastic was also observed in the energy range with $E/V_b = 0.9$ to 3.0, employing CDCC calculation.

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2 Experimental details and Analysis

In this perspective we have measured elastic angular distributions for ${}^{6,7}\text{Li}+{}^{28}\text{Si}$ at certain energies in the interval $E_{lab} = 11.5$ -26 MeV. The above barrier elastic scattering measurements were performed alongwith the measurement of above barrier fusion cross section for ${}^7\text{Li}+{}^{28}\text{Si}$ by evaporation α - method [1]. Experiment was performed at the 15 UD Pelletron facility of Inter University Accelerator Centre (IUAC), New Delhi with ${}^7\text{Li}$ beam at energies $E_{lab} = 16, 21$ and 26 MeV and ${}^6\text{Li}$ beam at energies $E_{lab} = 21$ and 26 MeV. The Si target of thickness $150\mu\text{g}/\text{cm}^2$ sandwiched between two Au layers was used. The elastic angular distribution was measured from the 2D spectra (E Vs ΔE) of two telescopes ($\Delta E: 25\mu\text{m}$, $E: 300\mu\text{m}$) placed at different angles, varying from $\theta_{lab} = 15.5^\circ$ to 94.5° , in small steps. Two monitor detectors ($300\mu\text{m}$) were mounted at forward angles $\pm 9.8^\circ$ (fixed to the wall of the chamber) with respect to beam axis and were used to monitor the beam axis and also for absolute normalisation purposes. The solid angles subtended by the telescopes and monitor detectors at the target centre were respectively 1.18×10^{-4} sr, 1.36×10^{-4} sr and 6.5×10^{-6} sr respectively. Angular resolution ($\Delta\theta$) of each telescope detector was about $\sim 0.7^\circ$.

A separate experiment was carried out using the General Purpose Scattering Chamber (GPSC) at the 14 UD BARC-TIFR Pelletron facility in Mumbai for the measurements of near barrier elastic scattering for ${}^7\text{Li}+{}^{28}\text{Si}$ system at $E_{lab} = 11.5$ and 13 MeV. A self supporting Si target of thickness $150\mu\text{g}/\text{cm}^2$ was used. During the experiment the beam current (${}^7\text{Li}^{2+}$) was varied from 2-20 pA. The elastically scattered particles were detected using the tele-

scope arrangements as discussed earlier. Two telescopes were used viz., (ΔE : 25 μm , E : 300 μm) and (ΔE : 15 μm , E : 500 μm). The detectors were placed on the rotating arm inside the scattering chamber with angular separation of 10° . Two monitor detectors (2 mm, 3 mm) were mounted at $\pm 15^\circ$ w.r.t. the beam axis. The solid angles subtended by the telescopes and monitor detectors at the target centre were respectively 9.9×10^{-4} sr, 1.7×10^{-4} sr and 4.7×10^{-6} sr. The angular resolution ($\Delta\theta$) of all the detectors was better than $\sim 0.4^\circ$. We also previously measured total fusion cross sections in the energy range $E_{lab} = 11.5$ - 26 MeV for ${}^6,7\text{Li}+{}^{28}\text{Si}$ [1] at the BARC-TIFR and IUAC Pelletron facilities. Moreover separate experiments were performed at sub-barrier energies from 7-11.5 MeV for ${}^6,7\text{Li}+{}^{28}\text{Si}$ [2,3] at IOP Pelletron facility, Bhubaneswar.

The elastic scattering data from 7.5 to 26 MeV were then analysed using the phenomenological Woods-Saxon potential employing the code ECIS94. The scattering data at other lower energies were taken from ref [4]. In the code ECIS94, rotational coupling of 2^+ state of the target with $\beta = -0.407$ was taken into account. Two sets of OM potential parameters with surface (OM1) and volume type(OM2)imaginary potentials were obtained from the best fit procedure. In order to obtain the best fit OM potential parameters, all six parameters were varied simultaneously. For surface type imaginary potential (OM1), the volume imaginary potential $W_v(R)$ was kept fixed with the energy independent parameter set of $W_F = 50$ MeV, $r_F = 1.0$ fm, $a_F = 0.4$ fm. The extracted reaction cross sections using both sets of potentials are found to be similar, however values are larger for ${}^6\text{Li}$ than ${}^7\text{Li}$. The energy dependence of effective potential parameters OM2 (Table 1 and Table 2), in a wide range of energies, is explored at the crossing radii as shown in Fig.3, Fig.4. The real and imaginary strength are evaluated at average crossing radius and is found to be almost independent of energy for $E_{lab} > 1.5 V_b$, although it starts to drop with decreasing energy towards the barrier. The real potential behaviour for ${}^6\text{Li}$ is almost similar to that of ${}^7\text{Li}$, however rate of decrease seems to be higher for ${}^6\text{Li}$ than ${}^7\text{Li}$. Also to connect the energy dependent behaviours of the real and the imaginary potential strengths at the surface using the dispersion relation was not successful. Our results differ from the previous observations [7] for the same systems ${}^6,7\text{Li}+{}^{28}\text{Si}$ where optical potentials were obtained by the double-folding procedure. These authors found almost energy independent normalisation factors (N_R) for real potentials, for both ${}^6\text{Li}$ and ${}^7\text{Li}$, where as normalisation factors (N_I) for imaginary potentials showed marked decreasing tendency towards the barrier for ${}^7\text{Li}$ compared to ${}^6\text{Li}$. Threshold behaviour of potentials (real and imaginary) is somewhat different from those usually found for cases involving medium and heavy mass targets Ref. [9–12].

The effect of breakup on elastic scattering was investigated within the continuum discretized coupled-channels (CDCC) framework using the code FRESKO [8] (Versions FRXP.18 and FRES 2.4). In CDCC calculation two body cluster structures of ${}^6\text{Li}$ ($\alpha+d$) and ${}^7\text{Li}$ ($\alpha+t$) were considered. The diagonal and non-diagonal coupling potentials for ${}^6\text{Li}+{}^{28}\text{Si}$ and ${}^7\text{Li}+{}^{28}\text{Si}$ were generated from the em-

Table 1. Optical Model (OM2) phenomenological potential parameters for ${}^7\text{Li}+{}^{28}\text{Si}$ with the extracted reaction cross sections as function of energy.

E_{lab} (MeV)	V_0 (MeV)	r_0 (fm)	a_0 (fm)	W_v (MeV)	r_v (fm)	a_v (fm)
8.5	5.1	1.12	0.808	5.96	1.17	0.786
10	10.2	1.12	0.788	10.32	1.17	0.786
11.5	16.9	1.08	0.766	5.87	1.16	0.783
13	17.3	1.08	0.766	16.92	1.16	0.783
16	19.7	1.08	0.766	23.29	1.16	0.783
21	20.8	1.08	0.766	15.93	1.16	0.783
26	49.6	1.07	0.717	20.46	1.16	0.700

Table 2. Optical Model (OM2) phenomenological potential parameters for ${}^6\text{Li}+{}^{28}\text{Si}$ with the extracted reaction cross sections as function of energy.

E_{lab} (MeV)	V_0 (MeV)	r_0 (fm)	a_0 (fm)	W_v (MeV)	r_v (fm)	a_v (fm)
7.5	5.7	1.02	0.822	3.79	1.19	0.865
9	19.6	1.01	0.812	9.16	1.19	0.845
11	20.1	1.01	0.809	15.41	1.17	0.776
13	33.9	1.01	0.792	22.39	1.17	0.776
16	45.9	1.01	0.793	38.24	1.17	0.733
21	57.3	1.01	0.766	42.98	1.16	0.675

perical $\alpha+{}^{28}\text{Si}$ [13], $d+{}^{28}\text{Si}$ [14] and $t+{}^{28}\text{Si}$ [15] optical potentials using the single folding approach. No target excitation was included in the CDCC calculations. In our calculation we discretized the continua following the scheme presented in Ref. [16]. However, for ${}^6\text{Li}+{}^{28}\text{Si}$, $L=0, 1, 2$ and 3 nonresonant and resonant states were included in the calculation although the resonance state at 5.65 MeV (1^+) excitation energy in $L=2$ continuum was excluded. Excitation of ${}^6\text{Li}$ upto 12 MeV was considered at higher bombarding energies. At lower bombarding energies the upper limit of excitation energy was suitably truncated. To match the elastic angular distribution at the highest bombarding energy for ${}^6\text{Li}+{}^{28}\text{Si}$ the input real and imaginary potentials for $\alpha+{}^{28}\text{Si}$ were normalized with factors of $N_R=0.7$ and $N_I= 2.8$. The normalization factors were kept fixed for lower bombarding energies. The resultant predictions are shown in Fig.1. Similar normalization values had earlier been used for ${}^6,7\text{Li}+{}^{59}\text{Co}$ by Beck, *et al.* [17]. For ${}^7\text{Li}+{}^{28}\text{Si}$, α and triton breakup from the bound excited state (0.47 MeV) as well as the resonant and non-resonant states of relative angular momentum of $L=0, 1, 3$ in the continuum were considered in the coupling scheme. The coupling to the continuum for $L=2$ had been neglected because of its insignificant contribution as observed by [18]. The continuum up to the excitation energy of 9.32 MeV ($k= 0.75$ fm $^{-1}$) was considered. For ${}^7\text{Li}+{}^{28}\text{Si}$, the normalisation factors for the real and imaginary input potentials for $\alpha+{}^{28}\text{Si}$

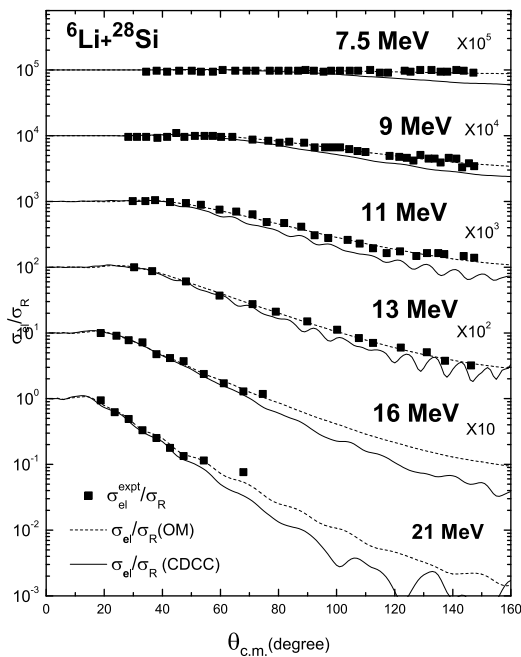


Fig. 1. Elastic angular distribution calculated with OM2 potential (dashed line) and CDCC calculation (solid line) for ${}^6\text{Li}+{}^{28}\text{Si}$ compared with measured data.

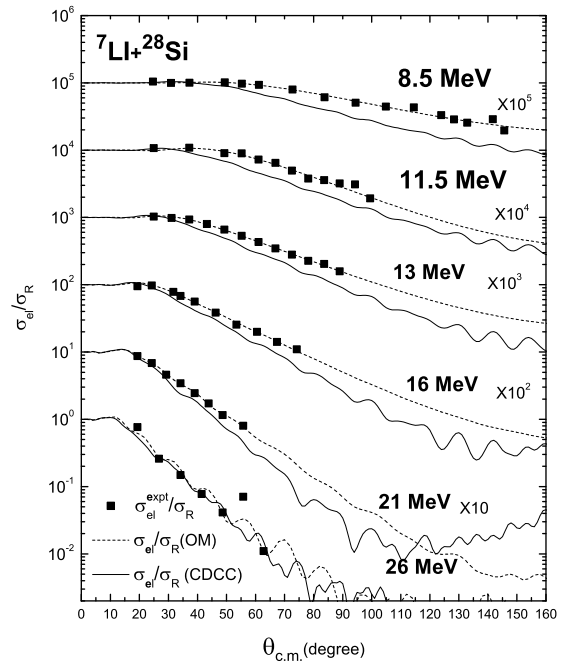


Fig. 2. Elastic angular distribution calculated with OM2 potential (dashed line) and CDCC calculation (solid line) for ${}^7\text{Li}+{}^{28}\text{Si}$ compared with measured data.

as well as for $t+{}^{28}\text{Si}$ were set at $N_R=0.7$, $N_I=2.8$ by reproducing the elastic angular distribution at the highest bombarding energy of 26 MeV. The same potential normalizations were used for all other incident energies. It is to be noted that a normalization factor of $N_R=0.6$ had been used for $\alpha+{}^{28}\text{Si}$ and $t+{}^{28}\text{Si}$ real empirical potentials in ${}^7\text{Li}+{}^{28}\text{Si}$ by Zerva, et al.[5]. The CDCC predictions from the present work are shown in Fig.2.

In order to observe the energy dependences of real and imaginary components of the effective potential, *i.e.* the 'bare' potential plus the polarization potential due to breakup, were extracted from the elastic angular distributions predicted by CDCC using a search routine. The energy dependence of resulting potential values evaluated at average crossing radius (R_{av}) are plotted and compared with those obtained by fitting the experimental elastic angular distributions in Figs.3 and 4.

3 Results

The comparison of measured elastic angular distributions with those predicted by CDCC model in Figs.1 and 2 show that at higher incident energies, coupling to breakup channel describes the data well. But at lower energies near the Coulomb barrier, the model predictions clearly underestimate the data. The model calculations appear to describe

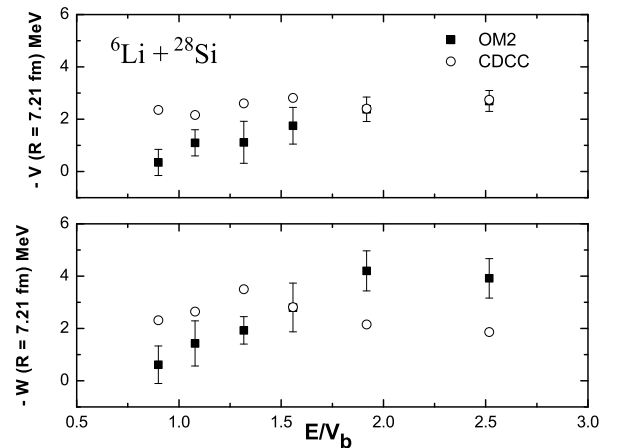


Fig. 3. Threshold behaviour of real and imaginary strength at average crossing radius for OM2 potential (solid square) and CDCC calculation (open circle) for ${}^6\text{Li}+{}^{28}\text{Si}$

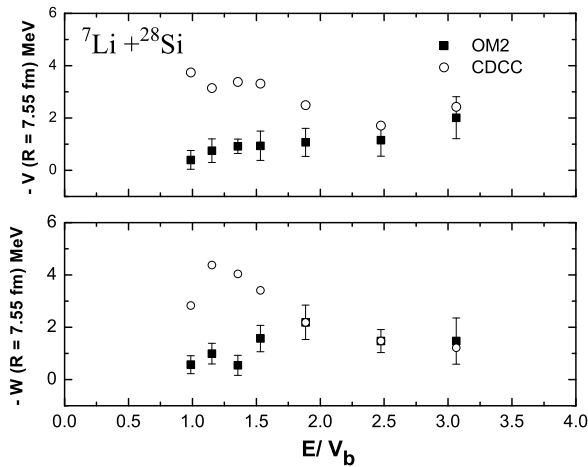


Fig. 4. Threshold behaviour of real and imaginary strength at average crossing radius for OM2 potential (solid square) and CDCC calculation (open circle) for ${}^7\text{Li}+{}^{28}\text{Si}$

the angular distributions of ${}^6\text{Li}+{}^{28}\text{Si}$ better than those of ${}^7\text{Li}+{}^{28}\text{Si}$ system. The underpredictions in case ${}^7\text{Li}+{}^{28}\text{Si}$ are quite significant. It is observed from Figs. 3 and 4 that the volume strengths of the optical model potential for both the systems show very similar trend with decreasing bombarding energies. The imaginary strength of the empirical potential decreases as the incident energy approaches the barrier whereas the real strength remains more or less flat with a slight declining trend. The energy variations of the effective potential components obtained from CDCC calculation follow the trend observed in the extracted data for ${}^6\text{Li}+{}^{28}\text{Si}$. But for the ${}^7\text{Li}+{}^{28}\text{Si}$, the nature of the theoretical prediction is largely different from the nature exhibited by the extracted experimental data. The behaviour of the calculated potential that includes the effect of breakup coupling indicates that for ${}^7\text{Li}+{}^{28}\text{Si}$ system breakup is not the dominating channel for coupling at lower energies. Experimental evidence of transfer channel at low energies has been reported in Ref. [19] and coupled channel calculation with such transfer channels at lower energies for ${}^7\text{Li}+{}^{28}\text{Si}$ need to be performed.

In Fig.5 the barrier distribution derived from the measured fusion excitation function of ${}^7\text{Li}+{}^{28}\text{Si}$ is presented. The extracted data have been compared with the 1D-BPM calculation and with calculation including the rotational coupling to the first excited state of ${}^{28}\text{Si}$. The coupling to the target excitation improves the description of the data but the effect is not so significant. The experimental barrier distribution, however, seem to be broad and asymmetric at the sub-barrier region. Due to a small number of data points around the barrier energy with large energy steps (2 MeV steps), the results shown are not very satisfactory to make any definite comment on the nature of the barrier distribution. Determination of the barrier distribution following the continuum discretized coupled channel calculation is in progress.

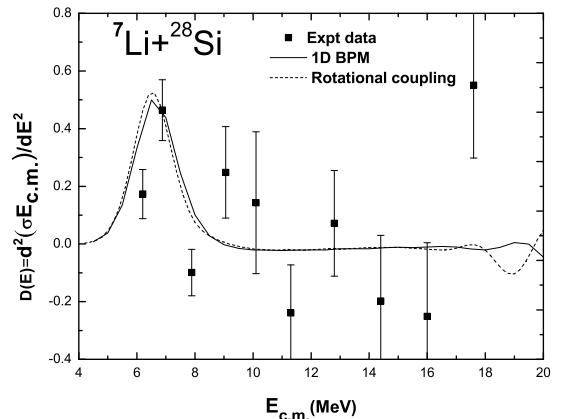


Fig. 5. Barrier distribution derived from measured fusion cross sections (solid square) compared with from 1D-BPM (solid line) and rotational coupling (dashed line) for ${}^7\text{Li}+{}^{28}\text{Si}$.

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