

Precise α_K and α_T Internal Conversion Coefficients Measurements of 39.752(6)-keV E3 Transition in ^{103m}Rh : Test of Internal Conversion Theory

TEXAS A&M PROGRAM TO MEASURE ICC

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Internal Conversion Coefficients (ICC):

- Big impact on quality of nuclear science*
- Central for the nuclear data evaluation programs*
- Intensely studied by theory and experiment*
- Important result: hole calculation now standard*

2002RA45 survey ICC's theories and measurements

- **Theory: RHFS and RDF comparison**

Exchange interaction, Finite size of nucleus, *Hole treatment*

- **Experiment:**

100 *E2, M3, E3, M4, E5* ICC values, 0.5%-6% precision,
very few <1% precision!

- **Conclusions, $\Delta(\text{exp:theory})\%$:**

No hole: **+0.19(26)% BEST!**

(bound and continuum states - SCF of neutral atom)

Hole-SCF: **-0.94(24)%**

(continuum - SCF of ion + hole (full relaxation of ion orbitals))

Hole-FO: **-1.18(24)%**

(continuum - ion field from bound wave functions of neutral atom

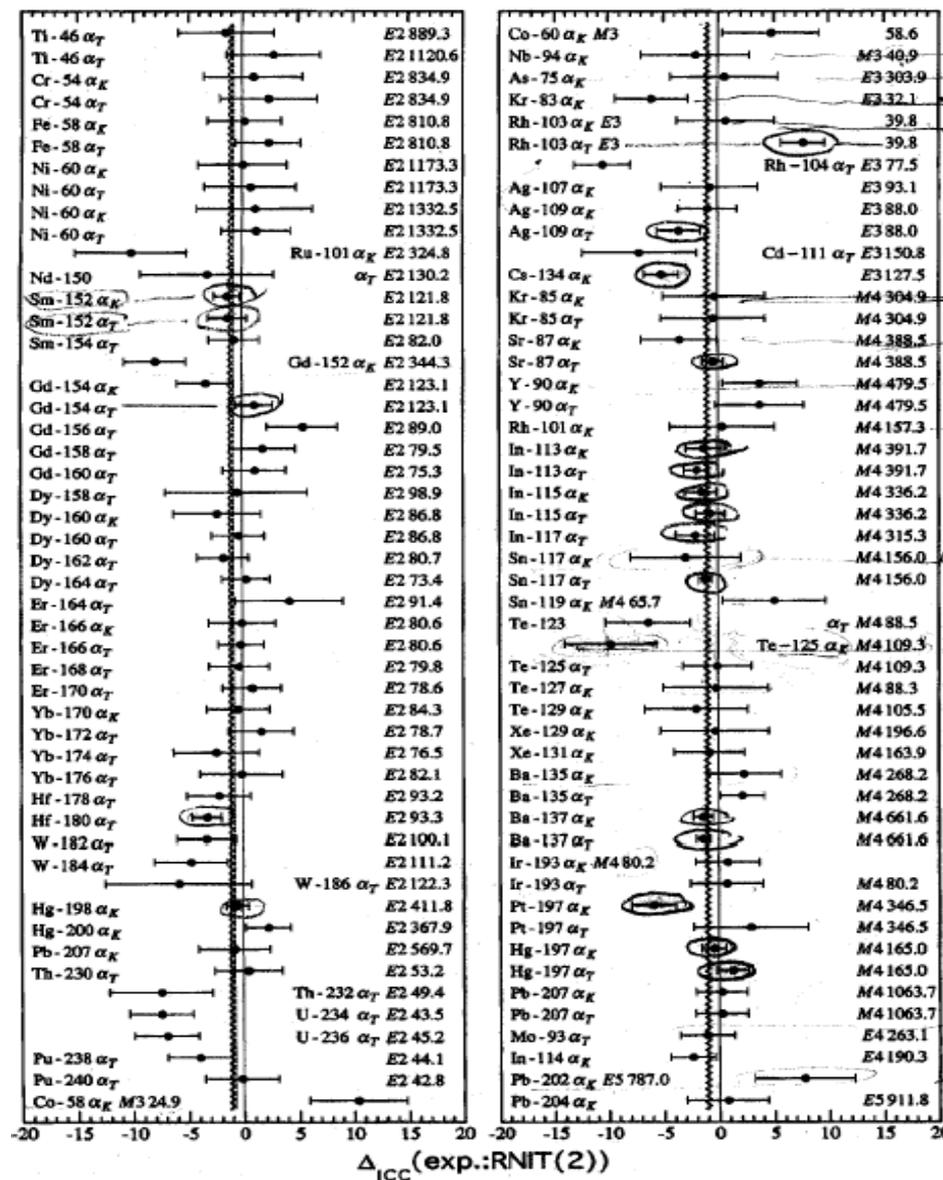
(no relaxation of ion orbitals))

PHYSICAL ARGUMENT

K-shell filling time vs. time to leave atom

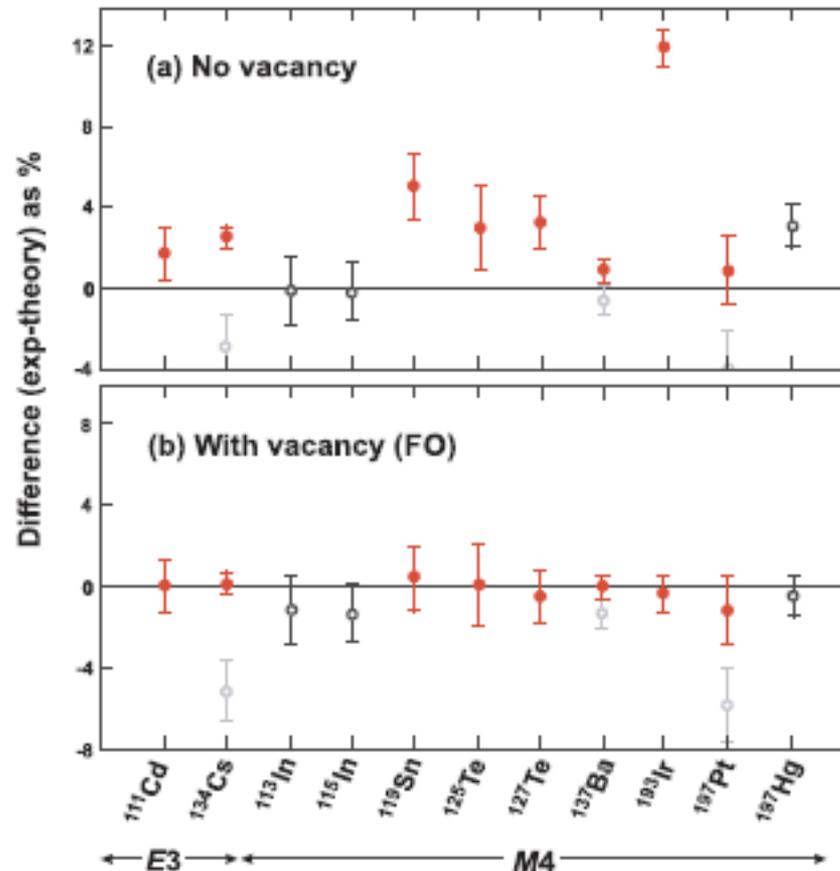
$\sim 10^{-15} - 10^{-17} \text{ s} \gg \sim 10^{-18} \text{ s}$

2002Ra45: 100 α_K (exp) cases compared with 'hole FO' calculations



Overview of the scope and completeness of the method

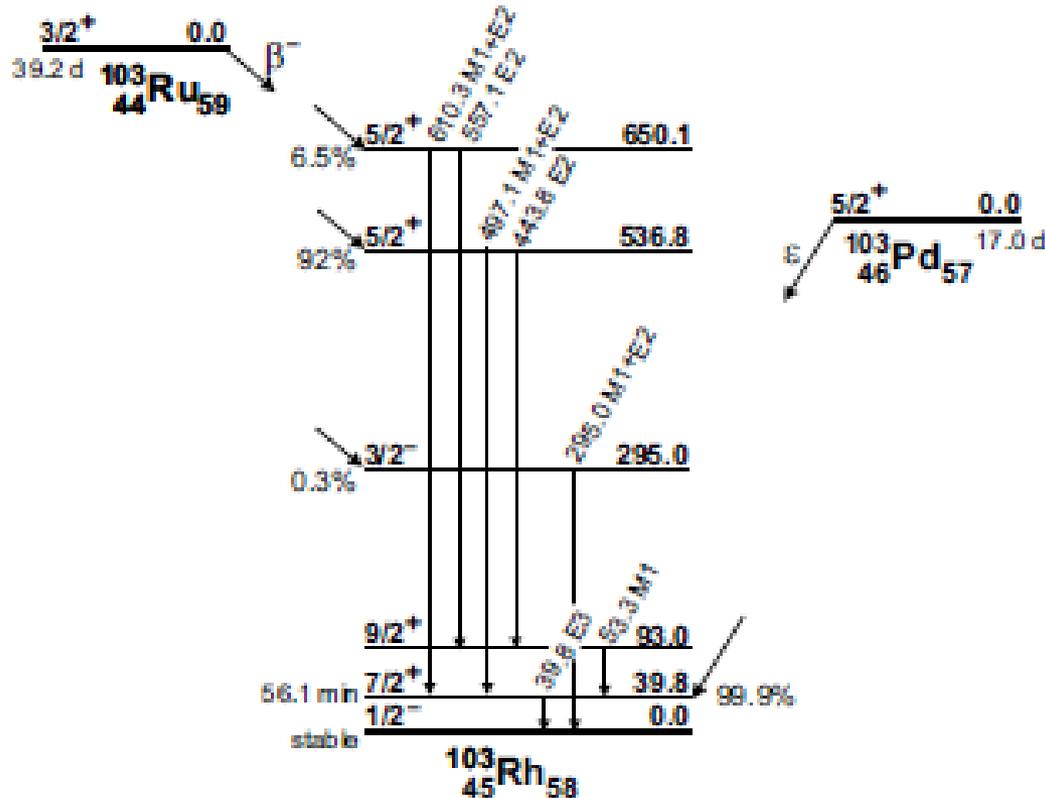
- **Scope:** *Minimize* ICC measurement unc ($\sim 1\%$) and *maximize* $\Delta_{theory}(\text{FO,NH})\%$ ($>4\%$, *E3*, *M4*)
- **Completeness:** There is no criterion to reach the scope of comparison between ICC theories “with hole” and “no hole” except for measuring precisely as many relevant cases as practically possible



III. $^{103\text{m}}\text{Rh}$ 39.748 keV, E3 transition

- $\alpha(\text{K})_{\text{exp}}$: 153 6 [1], 127 6 [2]
- $\alpha(\text{K})_{\text{hole_FO}} = 135.3(1)$, $\alpha(\text{K})_{\text{no_hole}} = 127.5(1)$, $\Delta_{\text{Theory}}(\text{FO,NH}) = 5.9\%$
- $\alpha(\text{T})_{\text{exp}}$: 1531 30 [2], 1430 89 [3]
- $\alpha(\text{T})_{\text{hole_FO}} = 1388(2)$, $\alpha(\text{T})_{\text{no_hole}} = 1404(1)$, $\Delta_{\text{Theory}}(\text{FO,NH}) = 1.1\%$

[1] M. Sainath *et al*, Ind. J. Pure and Appl. Physics 37, 87 (1999); [2] K.H. Czoek *et al*, Int. J. Appl. Radiat. Isotop. 26,417 (1975); [3] R. Vaninbroukx *et al*, Progress Report 1978, Central Bureau for Nuclear Measurements, Geel, Belgium, NEANDC(E)-202U, Vol. III, p. 28 (1979).



Texas A&M precision ICC measurements:

- KX to γ rays ratio method

$$\beta^- : \alpha_K = \frac{N_K}{N_\gamma} \cdot \frac{\varepsilon_\gamma}{\varepsilon_K} \cdot \frac{1}{\omega_K}$$

$$\varepsilon : \alpha_K + (1 + \alpha_T) P_{ec,K} = \frac{N_K}{N_\gamma} \cdot \frac{\varepsilon_\gamma}{\varepsilon_K} \cdot \frac{1}{\omega_K}$$

$$\sum_i (1 + \alpha_{Ti}) \cdot \frac{N_{\gamma i}}{\varepsilon_{\gamma i}} = (1 + \alpha_{T39.8}) \cdot \frac{N_{\gamma 39.8}}{\varepsilon_{\gamma 39.8}}$$

- N_K, N_γ measured from *only one K-shell converted transition*
- ω_K from 1999SCZX (compilation and fit)
- **Very precise detection efficiency for ORTEC γ -X 280-cm³ coaxial HPGe at standard distance of 151 mm:**
 - **0.2% , 50-1400 keV**
 - **0.4% , 1.4-3.5 MeV**
 - **~1% , 10-50 keV (KX rays domain)**

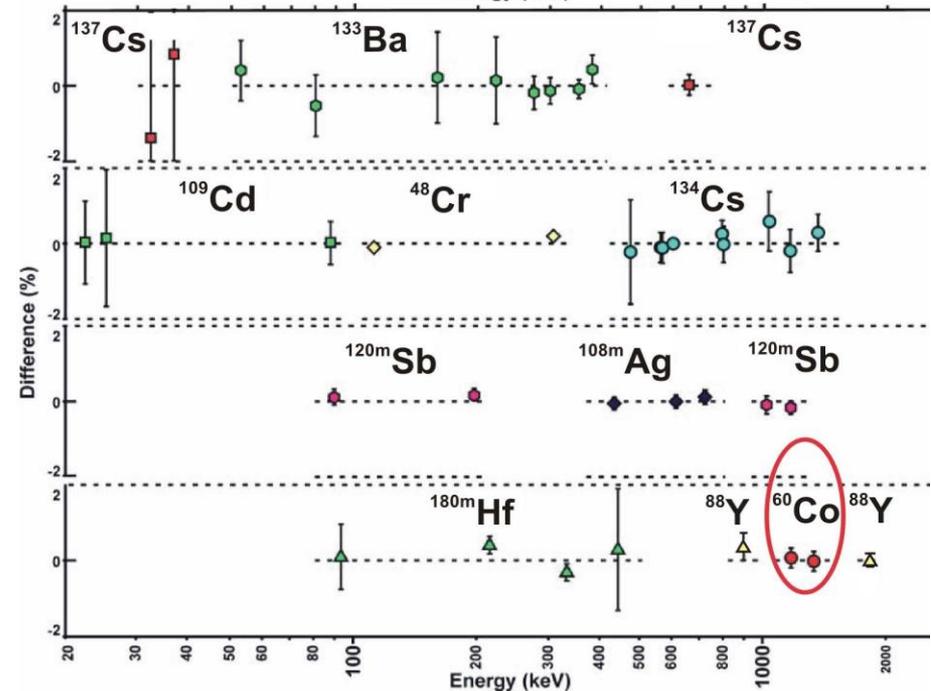
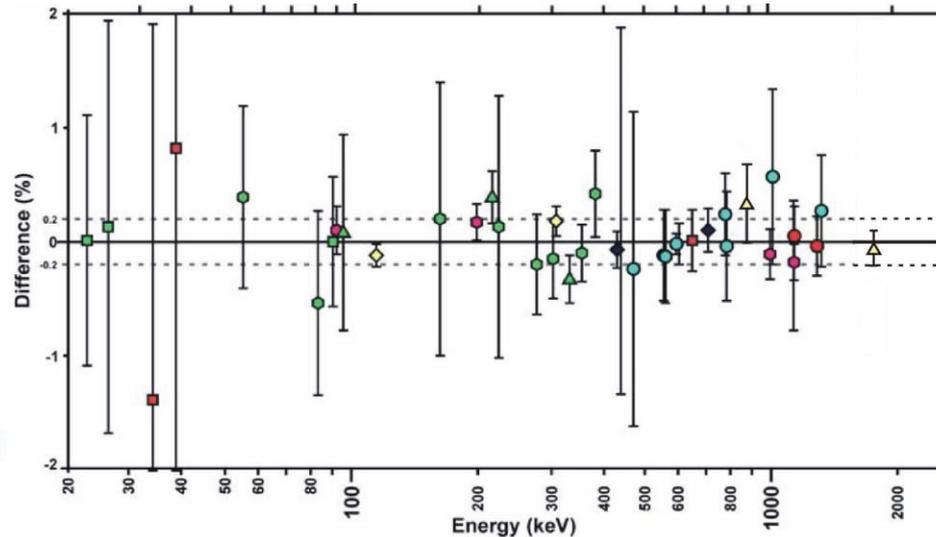
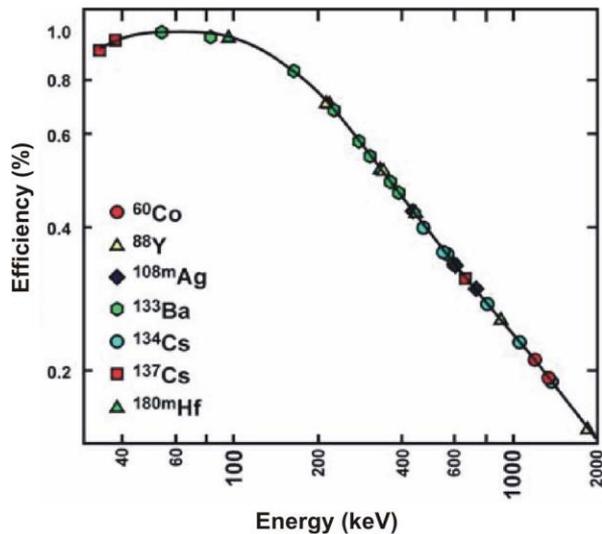
DETECTOR EFFICIENCY

$50 \text{ keV} < E_\gamma < 1.4 \text{ MeV}$

Coaxial 280-cc n-type Ge detector:

- Measured absolute efficiency (^{60}Co source from PTB with activity known to + 0.1%)
- Measured relative efficiency (9 sources)
- Calculated efficiencies with Monte Carlo (Integrated Tiger Series - CYLTRAN code)

0.2% uncertainty for the interval 50-1400 keV



^{109}Cd Efficiency Calibration

22.6-keV AgKx & 88.0-keV E3 γ regions

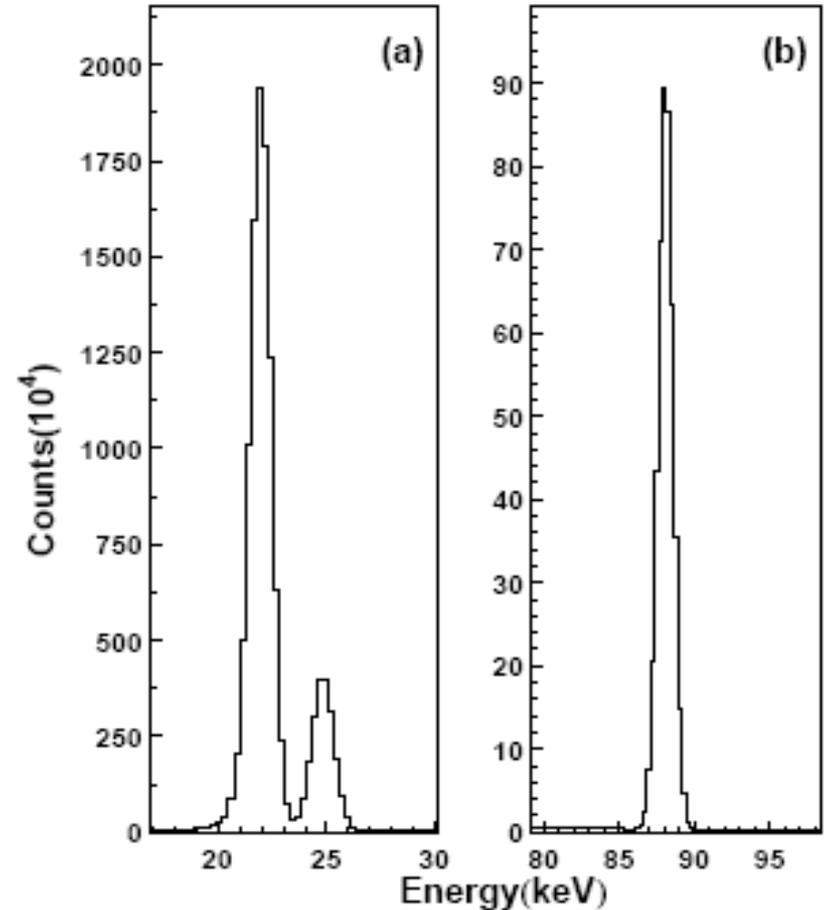
Photopeak efficiency:

^{109}Cd ε Decay: *single 88 γ*

-22.6-keV AgKx

-88.0-keV E3 γ ray

$$\frac{\varepsilon_{\gamma}}{\varepsilon_K} = \frac{\omega_K(\alpha_K P_{\gamma} + P_{ec,K})}{P_{\gamma}} \cdot \frac{N_{\gamma}}{N_K}$$



KX to γ rays ratio method

- Sources for n_{th} activation
 - Small selfabsorption ($< 0.1\%$)
 - Dead time ($< 5\%$)
 - Statistics ($> 10^6$ for γ or x-rays)
 - High spectrum purity
 - Minimize activation time (0.5 h)
- Impurity analysis - *essentially based on ENSDF*
 - Trace and correct impurity to 0.01% level
 - Use decay-curve analysis
 - Especially important for the K X-ray region
- Voigt-shape (Lorentzian) correction for X-rays
 - Done by simulation spectra, analyzed as the real spectra
- Coincidence summing correction
- Random summing (pile-up) monitoring / correction

^{103m}Rh Run

- *Radioactive Sources were prepared by (n_{th}, γ) reaction at TRIGA reactor of Texas A&M Nuclear Science Center at $\sim 7.5 \times 10^{12} \text{ n/cm}^2\text{s}$*
 - *Sources were prepared of materials with natural isotopic abundance: ^{102}Ru 32%, ^{102}Pd 1%*
1. ^{103m}Ru Source(1), $545 \mu\text{g/cm}^2 \text{ RuO}_2$ on Al backing. Activated for 20 h, measured after 1 months for ~ 20 days with **HPGe detector**. Found ^{153}Gd decay (239 d) 41.3-keV K_α peak affecting the 39.8-keV ^{103m}Rh peak of interest
 2. ^{103m}Ru Source(2), $1.1 \text{ mg/cm}^2 \text{ Ru}$ metal on $1.3 \text{ mg/cm}^2 \text{ Cu}$ metal. Activated for 32 h, measured after 1 months for ~ 77 days with **HPGe detector** and **Si(Li) detector**.
 3. ^{103m}Pd Source(3), $4.8 \text{ mg/cm}^2 \text{ Pd}$ metal. Activated for 4.5 h, measured after 2 months for ~ 44 days with **HPGe detector**.

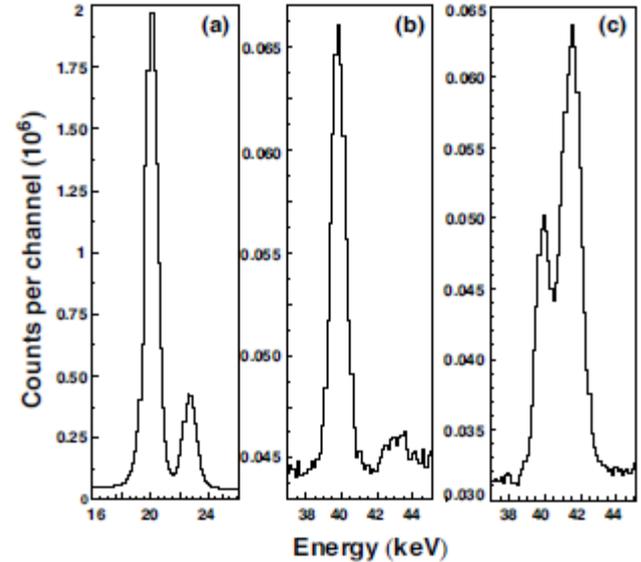
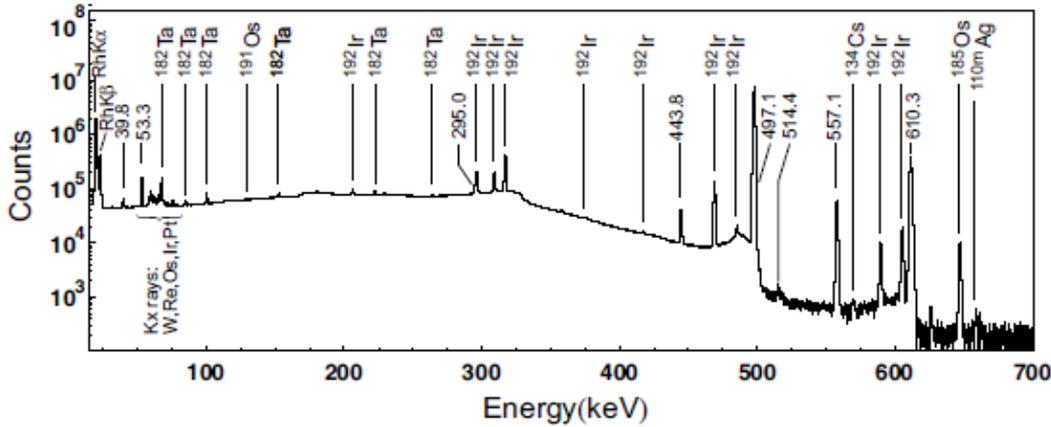
103mRh Analysis

HPGe detector

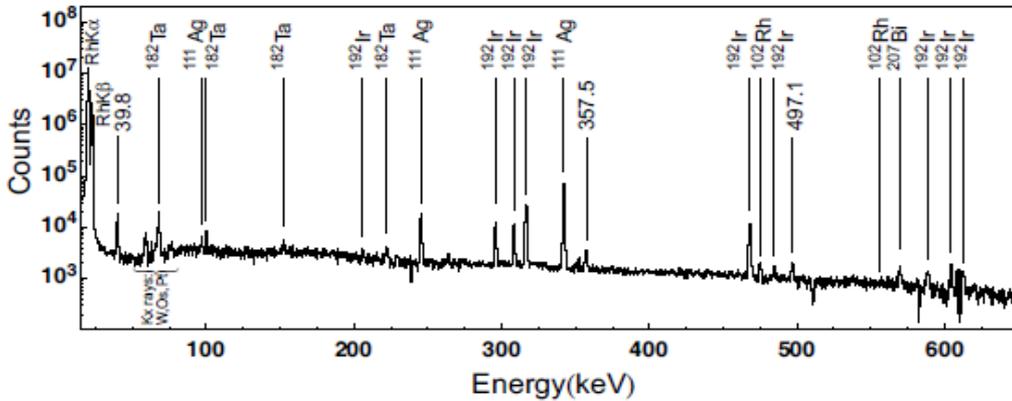
Ru/Cu Source(2): (a) Rh Kx-rays; (b) 39.8-keV γ ray

RuO₂ Source(3): (c) 39.8-keV γ ray + Eu K _{α} contamination

Ru/Cu Source(2): *Impurity analysis spectrum*

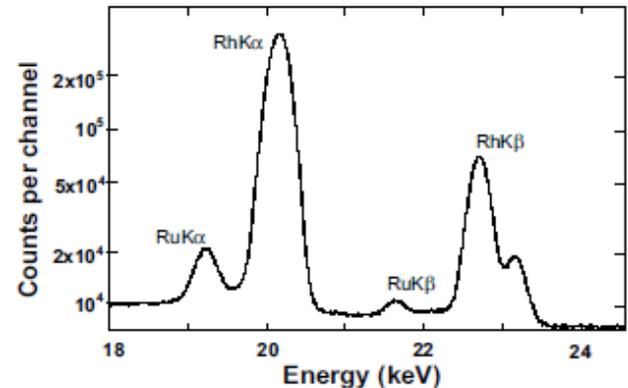


Pd Source(3): *Impurity analysis spectrum*



(Si)Li detector, Ru/Cu Source(2):

Rh Kx-rays with Ru Kx-rays (fluorescence)



^{103m}Rh Results

Weighted average of seven experimental results:

- From Ru run Source(1) and Source(2)

$$\alpha_{K39.8} = 141.1(23) \text{ (rel. unc. 1.6\%)}$$

$$\alpha_{T39.8} = 1428(13), \text{ (rel. unc. 0.9\%)}$$

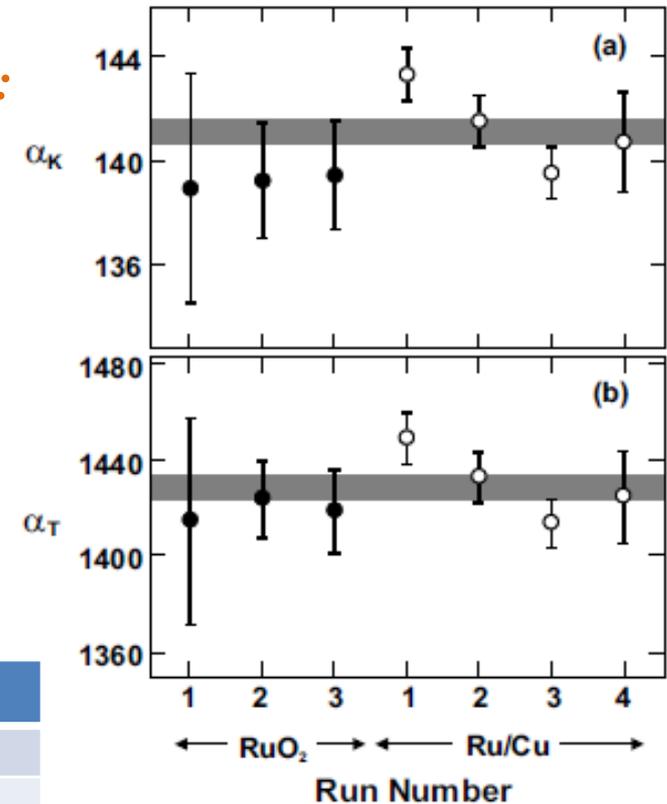
- Pd Source(3)

Consistency check: $^{103}\text{Pd} \varepsilon \quad ? \quad ^{103}\text{Ru} \beta^-$

$$\alpha_K + (1 + \alpha_T)P_{ec,K} : 1383(28) \approx 1369(11)$$

Model	α_K	$\Delta(\%)$	α_T	$\Delta(\%)$
Experiment	141.1(23)		1428(13)	
Theory:				
a) Pure E3				
No vacancy	127.5(1)	+10.7(18)	1388(2)	+2.9(9)
Vacancy(FO)	135.3(1)	+4.3(17)	1404(1)	+1.7(9)
a) E3+M4, $\delta=0.02$ (0.04%)				
No vacancy	131.2(1)	+7.5(18)	1410(2)	+1.3(9)
Vacancy(FO)	139.3(1)	+1.3(17)	1426(1)	+0.1(9)

(a) α_K and (b) α_T from Ru Source(1) and Source(2)



Conclusion:

Small M4 admixture:

-Agreement with theory including the vacancy (FO)

-Disagreement with theory ignoring the vacancy