



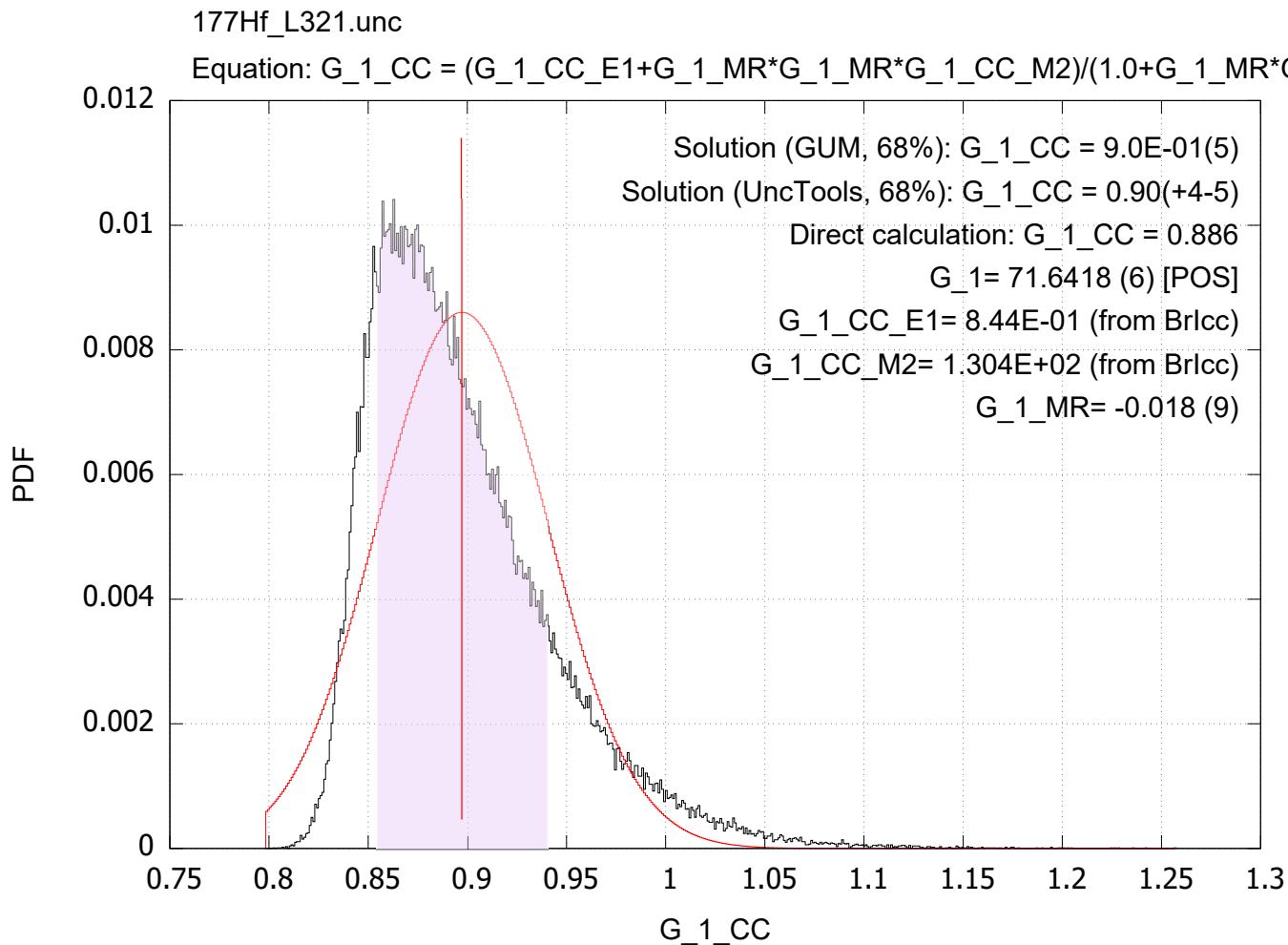
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UncTools (NS_Lib) - treatment of uncertainties using Monte Carlo

T. Kibèdi (ANU)



Experimental quantitates in ENSDF





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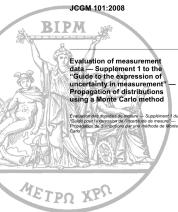
Experimental quantitates in ENSDF

2001TuZZ J.K. Tuli, *A Manual for Preparation of Data Sets*

- Single unsigned number: BR, CC, HF, LOGFT, NB, NP, NR, NT, QP
 - Single signed number: MR, Q-, QA, SN, SP
 - Standard symmetric uncertainty; two character field (ENSDF Manual V.11):
 - an up to two digits integer, up to 99, preferable less than 25
 - LT, GT, LE, GE, AP, CA, S
 - DBR, DCC, DE, DHF, DIA, DIB, DIE, DIP, DNB, DNR, DNP, DNT, DQP, DQ-, DS, DSP, DTI
 - Standard asymmetric uncertainty; two signed integers (ENSDF Manual V.12):
 - DFT, DMR, DT, DNB, DQA
 - Special rules for E, M, J, S, L fields
- Uncertainty propagation in ENSDF codes:
- Gaussian (analytical) method, only valid for small DX/X values
 - For multi-variant functions (Ruler, Gabs, Gtol) difficult / impossible to manage



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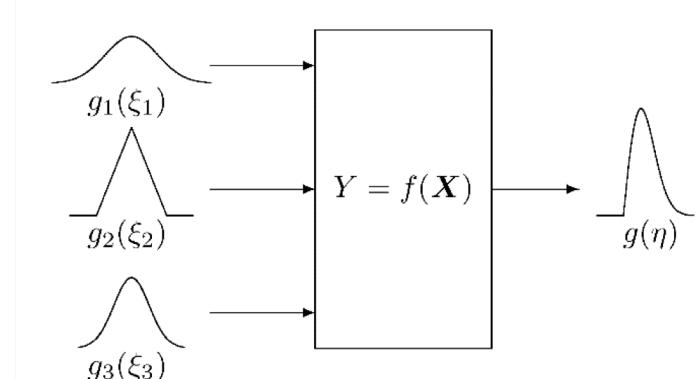
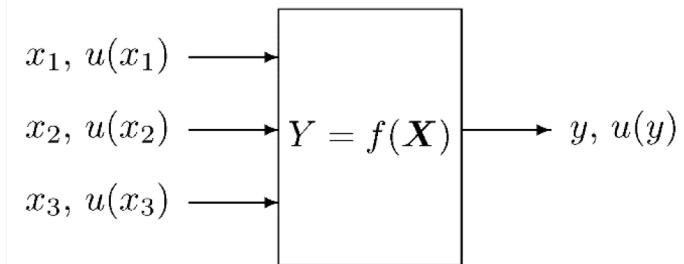
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GUM framework

Joint Committee for Guides in Metrology (JCGM, 1993) Guide to the Expression of Uncertainty in Measurement

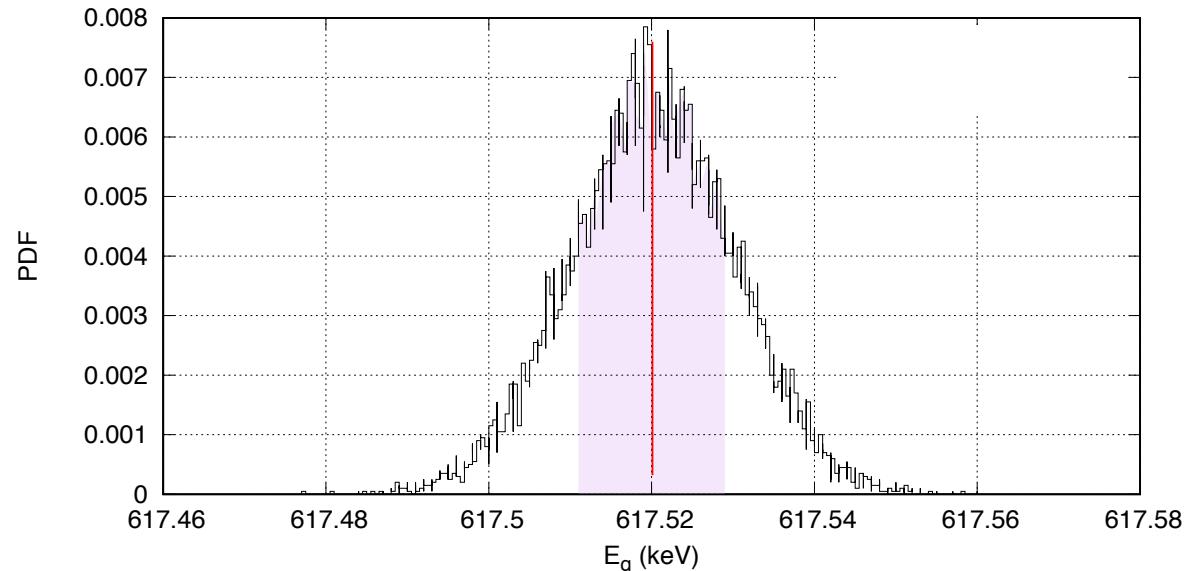
Concept

- Define the output quantity, the quantity required to be measured.
- Decide the input quantities upon which the output quantity depends.
- Develop a model relating the output quantity to these input quantities.
- On the basis of available knowledge assign probability density - Gaussian normal), rectangular (uniform), etc. - to the values of the input quantities.

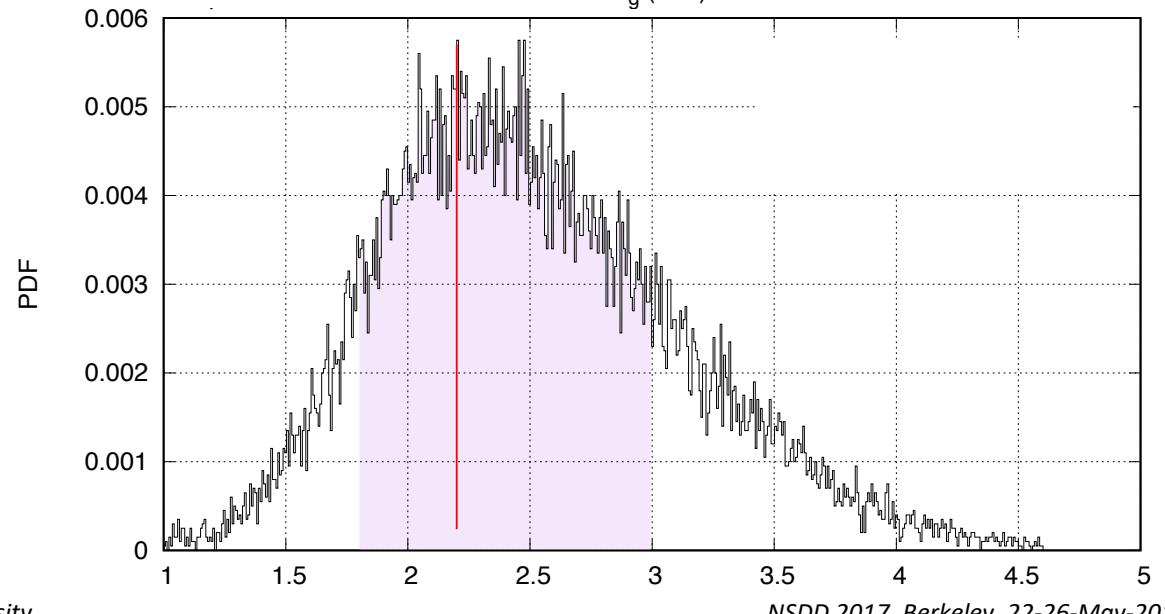


Probability Density Function (PDF)

Symmetric Normal
Distribution:
 $E_\gamma = 617.520(10)$ keV



Asymmetric normal
distribution:
 $MR=+2.2(+8-4)$



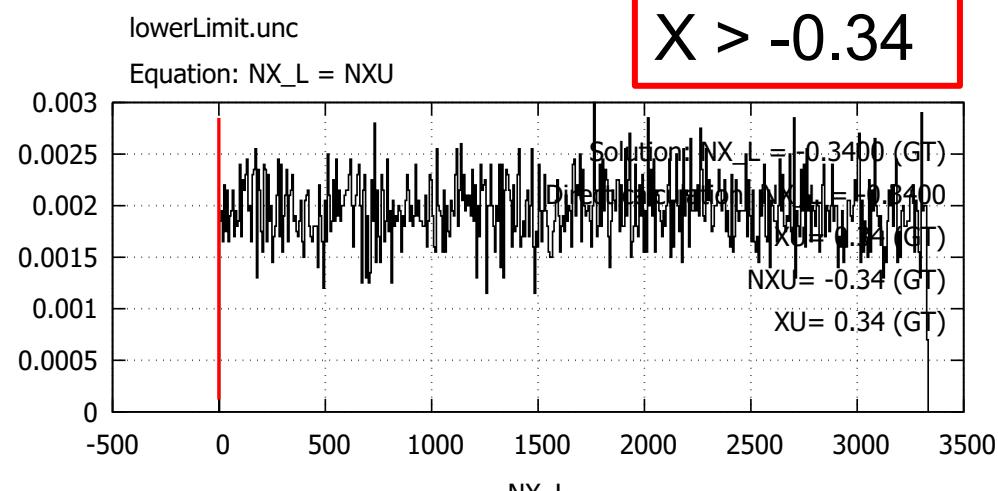
Probability Density Function (PDF)

Limits

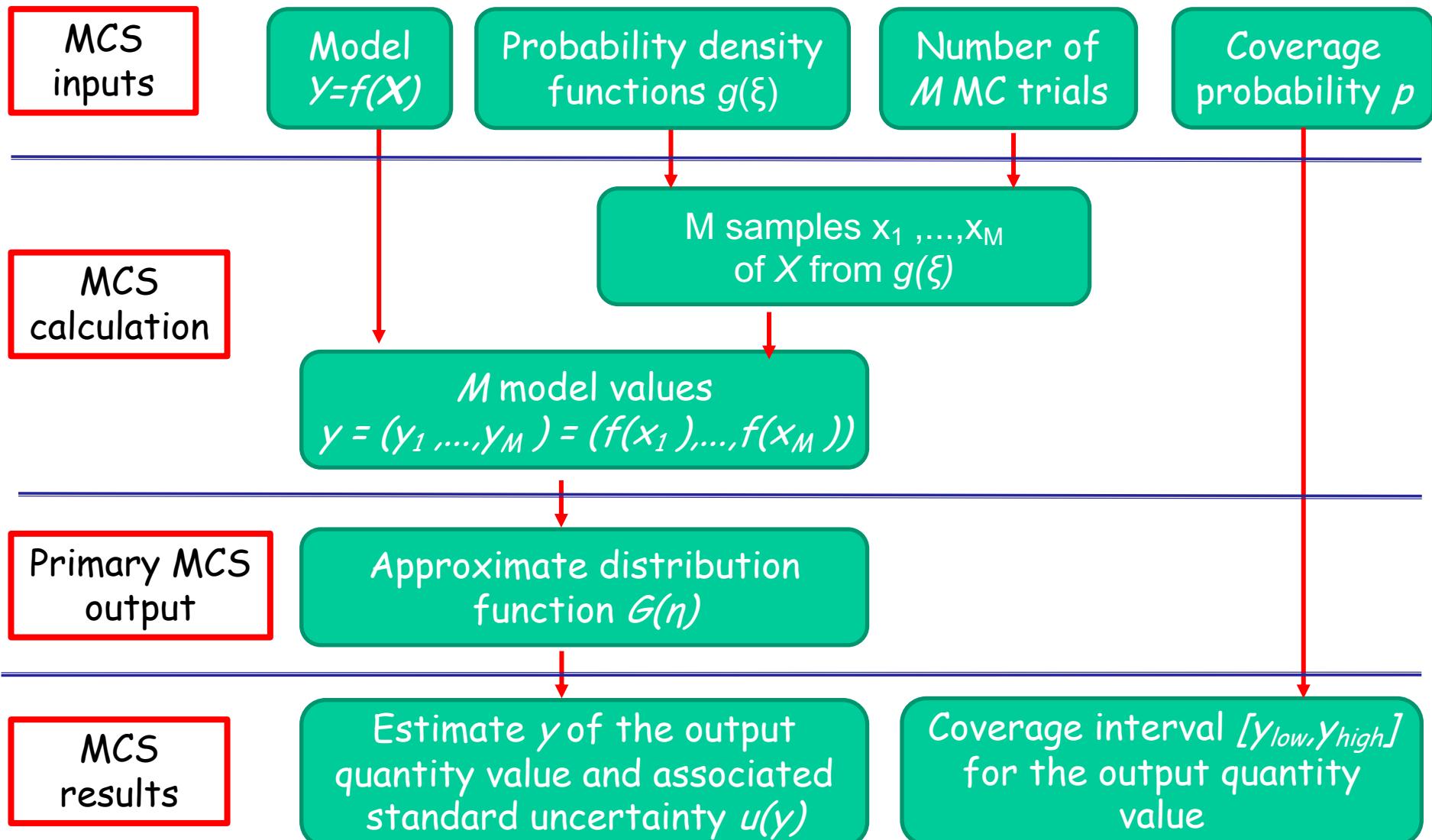
	Limit	Range	Range Used in MC
UPPER	<0.5	[0 : +0.5]	[0 : +0.5]
	<+0.5	[-infinity : +0.5]	[-4999.5:+0.5]
	<-0.5	[-infinity : -0.5]	[-5000.5:-0.5]
LOWER	>0.5	[+0.5:+infinity]	[+0.5:+5000.5]
	>+0.5	[+0.5:+infinity]	[+0.5:+5000.5]
	>-0.5	[-0.5:+infinity]	[-0.5:+4999.5]

PDF uniform over the entire range

- Infinite range: **PDF = Zero**
- Replace infinity with a sufficiently large range:
Infinity \sim **10000 Limit value^{PDF}**



Monte Carlo simulations to obtain the output quantity





Estimate of the output quantity

After M draws model values obtained as (JCGM 101:2008 7.6)

$$y_r = f(X_r), r=1, 2, \dots, M$$

Average:

$$\tilde{y} = \frac{1}{M} \sum_{r=1}^M y_r$$

Standard deviation:

GUM solution

$$u^2(\tilde{y}) = \frac{1}{M-1} \sum_{r=1}^M (y_r - \tilde{y})^2$$

NOTE: \tilde{y} may not agree $f(X)$, where X is the best parameter values!c

Balraj Singh (26-May-2012)

One question: ^{211}Po : 34(5) keV gamma: I am now assigning (E4) based on model considerations. When I run interactive BrIcc, total $CC=4.\text{E}6$ (8). Does it mean $4(8)\text{E-6}$ or $4.0(8)\text{E}6$? Seems former is the case since when I run BrIcc on 29, 34 and 39 keV, I get values from $1.4\text{E}6$ to $14\text{E}6$, but I think the nomenclature needs some clarification. When researchers quote numbers in papers like $4.(8)$, they generally imply $4.0(8)$.

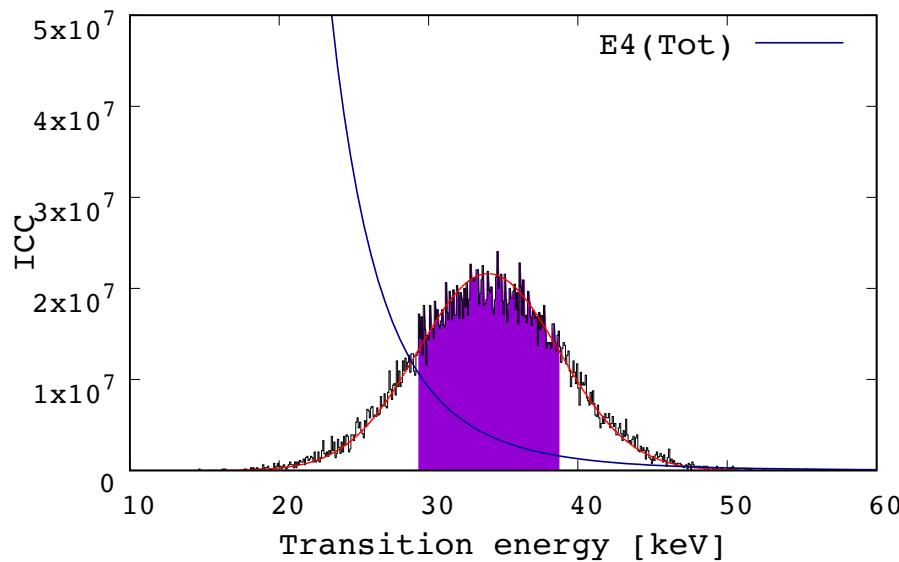
$BrIcc\ ^{211}\text{Po}$ 34(5) keV E4 $CC=4.\text{E}6$ $DCC=8.\text{E}6$

$DICC=ICC(E), ICC(E-DE), ICC(E+DE)$

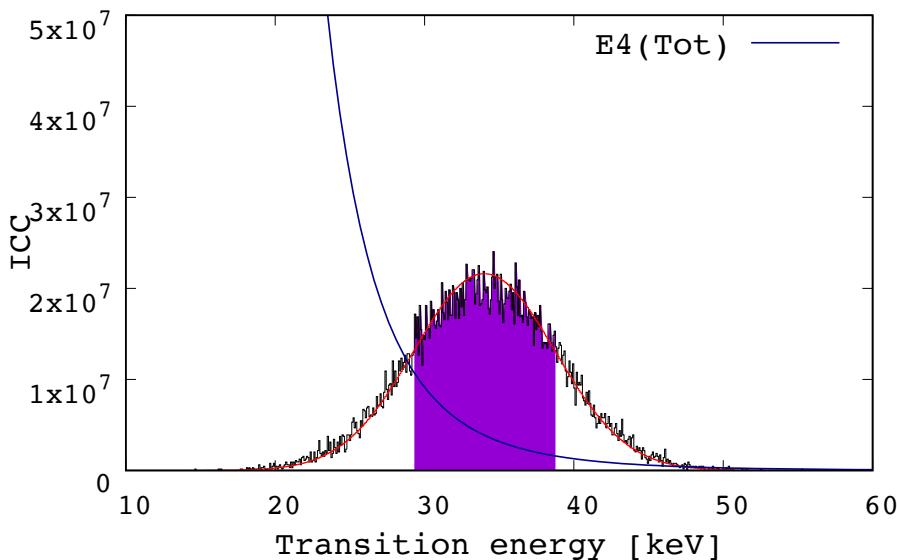
$3.9\text{E+6}, \quad 1.2\text{E+7}, \quad 1.5\text{E+6}$

$BrIcc\ ^{211}Po\ 34(5)\ keV\ E4$

$DICC=ICC(E),\ ICC(E-DE),\ ICC(E+DE)$
 $3.9E+6,\quad 1.2E+7,\quad 1.5E+6$



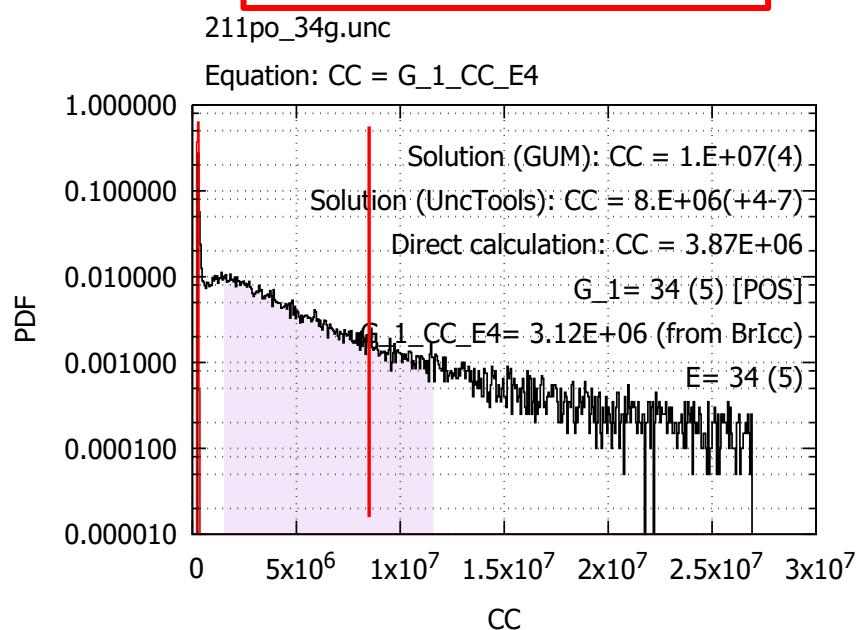
$BrIcc$ ^{211}Po 34(5) keV E4
 $DICC=ICC(E), ICC(E-DE), ICC(E+DE)$
 $3.9E+6, \quad 1.2E+7, \quad 1.5E+6$



Same uncertainty propagation used across the ENSDF codes!

$BrIcc:$
 $CC=4.E6 (8)$

$GUM (68\%):$
 $CC=1.E7(4)$



$UncTools:$
 $CC=8.(+4-7)E+6$

Mixed ICC with limit on MR

BrIcc ^{111}AG $70.44(5)$ keV M1+E2, MR: 0.12 LE

BrIcc v2.3b (16-Dec-2014) Z= 47 Egamma= 70.44 5 keV			Multipolarity= M1+E2		22:42:05 24-May-2017
	M1+E2 Mixed		Mixing ratio= 0.12 LE		
Shell	M1	E2	Icc	dIcc	dIccDMRL dIccDMRH
K	9.869E-01	3.445E+00	1.004E+00	2.250E-02	1.745E-02 1.745E-02
L-tot	1.233E-01	1.298E+00	1.317E-01	8.546E-03	8.340E-03 8.340E-03
K/L	8.002E+00	2.654E+00	7.628E+00	5.237E-01	
M-tot	2.349E-02	2.565E-01	2.514E-02	1.691E-03	1.654E-03 1.654E-03
L/M	5.251E+00	5.062E+00	5.237E+00	4.896E-01	
N-tot	4.058E-03	4.069E-02	4.318E-03	2.671E-04	2.600E-04 2.600E-04
L/N	3.039E+01	3.191E+01	3.049E+01	2.734E+00	
O-tot	1.860E-04	4.678E-04	1.880E-04	3.328E-06	2.000E-06 2.000E-06
L/O	6.631E+02	2.776E+03	7.004E+02	4.712E+01	
Tot	1.138E+00	5.041E+00	1.166E+00	3.224E-02	2.770E-02 2.770E-02

CC=1.17(4)

$$\alpha = \left[\frac{\alpha(\pi L) + \delta^2 \alpha(\pi' L')}{1 + \delta^2} + \alpha(\pi L) \right] \times 0.5,$$

$$\Delta\alpha_{DMR_H} = \Delta\alpha_{DMR_L} = \left| \frac{\alpha(\pi L) + \delta^2 \alpha(\pi' L')}{1 + \delta^2} - \alpha(\pi L) \right| \times 0.5.$$

$$\Delta\alpha_{DE_H} = \alpha(E_\gamma + \Delta E_H) - \alpha(E_\gamma),$$

$$\Delta\alpha_{DE_L} = \alpha(E_\gamma - \Delta E_L) - \alpha(E_\gamma).$$

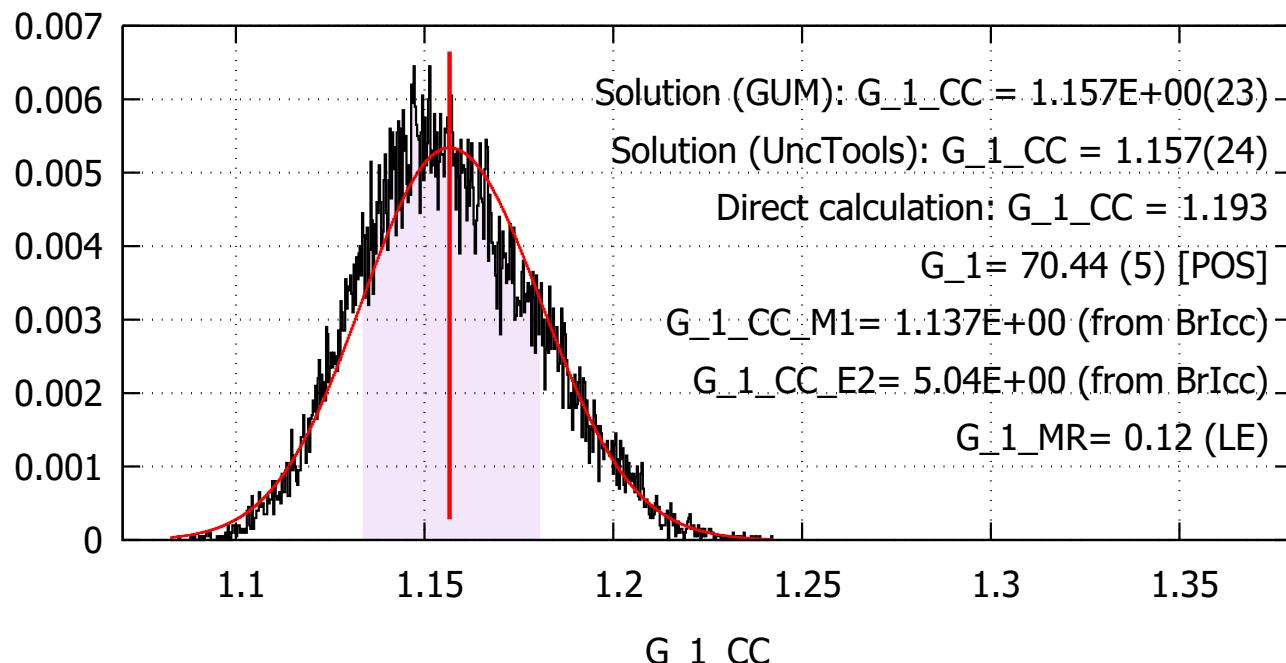
Mixed ICC with limit on MR

$BrIcc^{111}Ag \ 70.44(5) \text{ keV } M1+E2, MR: 0.12 \text{ LE}$

BrIcc
CC=1.17(4)

111Ag_70G.unc

Equation: $G_1_CC = (G_1_CC_M1 + G_1_MR * G_1_MR * G_1_CC_E2) / (1 + G_1_MR * G_1_MR)$



GUM
CC=1.157(23)

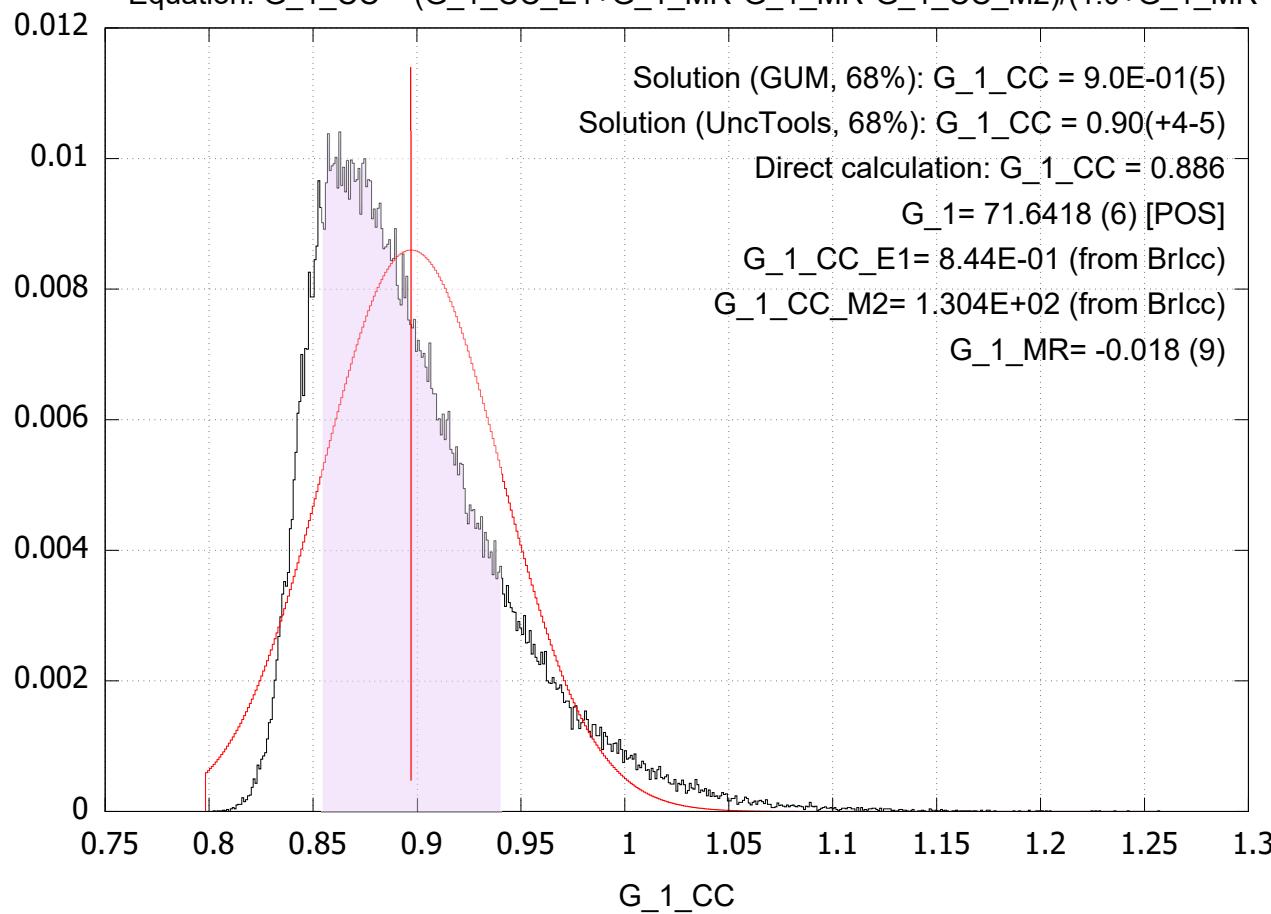
UncTools
CC=1.157(24)

Mixed ICC with limit on MR

$BrIcc^{177}\text{Hf}$ $71.6418(6)$ keV E1+M2, MR: $-0.018(9)$

177Hf_L321.unc

Equation: $G_{_1_CC} = (G_{_1_CC_E1} + G_{_1_MR} * G_{_1_CC_M2}) / (1.0 + G_{_1_MR} * G_{_1_MR})$



BrIcc
CC=0.89(6)

GUM
CC=0.90(5)

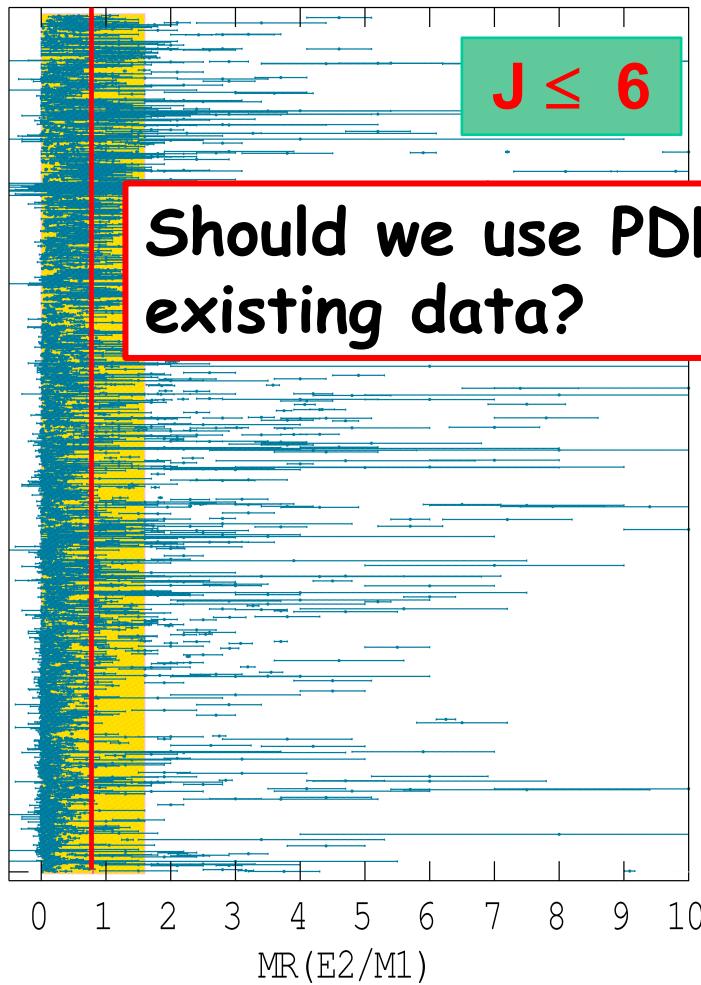
UncTools
CC=0.90(+4-5)

Mixed ICC - MR unknown

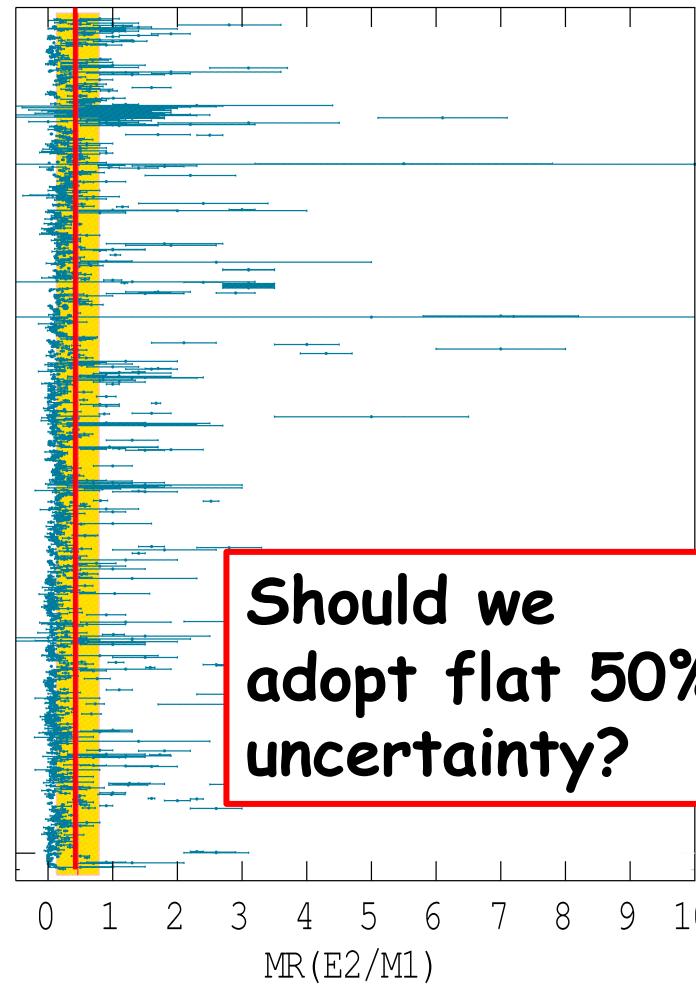
*BrIcc: MR=1.00 FOR E2/M1, MR=1.00 FOR E3/M2 AND
MR=0.10 FOR THE OTHER MULTIPOLARITIES*

*MC uncertainty propagation: What is the uncertainty on
the assumed values?*

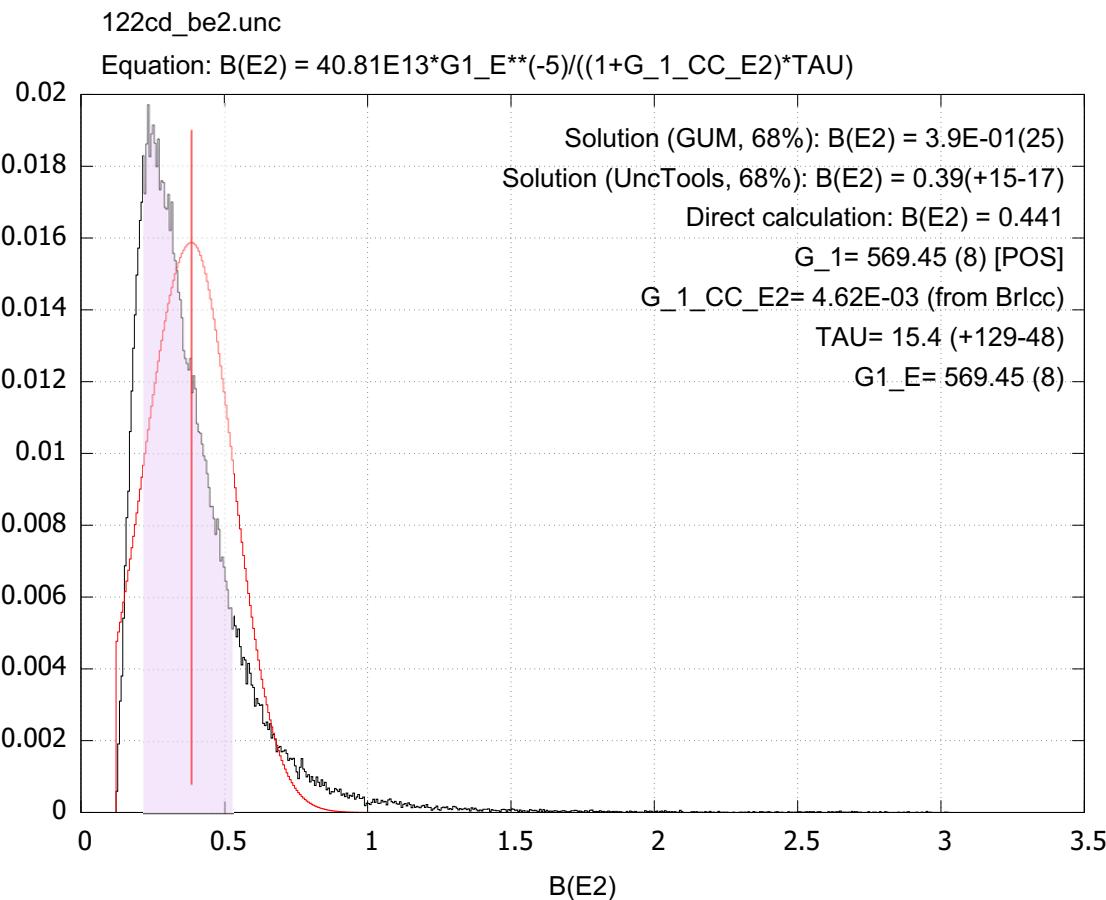
MR(E2/M1): N=4894; LWM=0.80(80)



MR(E2/M1): N=1530; LWM=0.46(33)



^{122}Cd $\tau=15.4(+129-48)$ ps; $569.45(8)$ keV E2 (2016Pr01)



2016Pr01
 $B(E2)=0.44(20) e^2 b^2$

GUM
 $B(E2)=0.38(24)$

UncTools
 $B(E2)=0.38(+15-17)$

Directly calculated
 $B(E2)=0.441$

TRuler - transition strength

Table 1 (continued)

E_i [keV]	$T_{1/2}^{\text{exp}}$	K_i^π [\hbar]	J_f^π [\hbar]	K_f^π [\hbar]	$\sigma\lambda$	E_γ [keV]	I_γ	α_T	Γ_γ [eV]	F_w	ν	f_v
^{244}Cm ($Z = 96, N = 148$)												
1040.188 (12)	34 (2) ms	6 ⁺	8 ⁺	0 ⁺	E2	538.400 (16)	1.0 (3)	4.95E–02	9 (3)E–17	3.8 (12)E+10	4	440 (30)
			6 ⁺	0 ⁺	M1 + E2	743.971 (5)	100 (1)	7.70E–02	$ \delta = 0.92(8)$			
				M1					4.7 (5)E–15	1.81 (18)E+12	5	283 (6)
				E2					4.0 (4)E–15	4.2 (5)E+9	4	254 (7)
			4 ⁺	0 ⁺	E2	897.848 (7)	44.9 (6)	1.70E–02	3.90 (23)E–15	1.09 (7)E+10	4	323 (5)

Furthermore, the strength $|M|^2$ of an individual transition in single-particle (Weisskopf) units (W.u.) is related to its widths, lifetimes and B values, and to the inverse of its hindrance factor (F_W) by:

$$|M|^2 \text{ (W.u.)} = \Gamma_\gamma / \Gamma_W = \tau_W / \tau_\gamma = B_\gamma \downarrow / B_{sp} \downarrow = 1 / F_W. \quad (14)$$

For transitions that are (in principle) forbidden, the degree of K forbiddenness, ν , is defined as:

$$\nu = \Delta K - \lambda, \quad (15)$$

where $\Delta K = |K_i - K_f|$ is the difference between the K quantum numbers of the initial and final states, and λ is the multipole order of the transition. The reduced hindrance per degree of K forbiddenness is given by:

$$f_\nu = F_W^{\frac{1}{\nu}}. \quad (16)$$

TRuler - transition strength

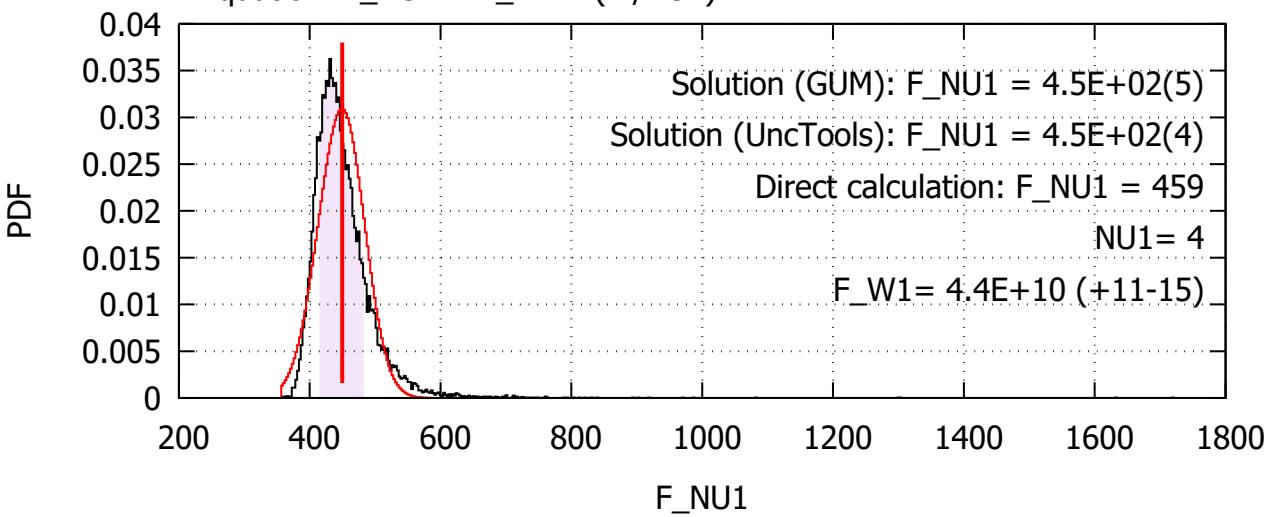
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F.G. Kondev et al. / Atomic Data and Nuclear Data Tables 103–104 (2015) 50–105

Table 1 (continued)

E_i [keV]	$T_{1/2}^{\text{exp}}$	K_i^π [\hbar]	J_f^π [\hbar]	K_f^π [\hbar]	$\sigma\lambda$	E_γ [keV]	I_γ	α_T	Γ_γ [eV]	F_w	v	f_v
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			6 ⁺	0 ⁺	M1 + E2	743.971 (5)	100 (1)	7.70E-02	$ \delta = 0.92(8)$			
					M1				4.7 (5)E-15	1.81 (18)E+12	5	283 (6)
					E2				4.0 (4)E-15	4.2 (5)E+9	4	254 (7)
			4 ⁺	0 ⁺	E2	897.848 (7)	44.9 (6)	1.70E-02	3.90 (23)E-15	1.09 (7)E+10	4	323 (5)

244Cm_1040.unc

Equation: $F_{\text{NU1}} = F_{\text{W1}}^{**}(1./\text{NU1})$ 

2015Ko14 (Python)
 $f_v = 440(30)$

GUM
 $f_v = 4.5 (5)\text{E}+2$

UncTools
 $f_v = 4.5 (4)\text{E}+2$

Directly calculated
 $f_v = 4.59\text{E}+2?????$



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Proposal of propagation uncertainties including limits using MC

Advantage

- Consistent treatment of all cases, much simpler program logic (no more jungle of IF statements)
- Sound statistical approach even for larger relative uncertainties and limits

Disadvantage

- CPU intensive
- Mean value may not agree with directly calculated value

Questions/Problems

- Sampled / output values could be nonphysical: $T_{1,2}=0.15(7)$ ns
- Some uncertainties in ENSDF expected to be symmetrical (DBR, DCC, DE, DHF, DIA, DIB, DIE, DIP, DNB, DNR, DNP, DNT, DQP, DQ-, DS, DSP, DTI)