

# TALYS-0.64

A nuclear reaction program

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## USER MANUAL

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# Preface

TALYS is a nuclear reaction program created at NRG Petten, the Netherlands and CEA Bruyères-le-Châtel, France. The idea to make TALYS was born in 1998, when we decided to implement our combined knowledge of nuclear reactions into one single software package. Our objective is to provide a complete and accurate simulation of nuclear reactions in the 1 keV-200 MeV energy range, through an optimal combination of reliable nuclear models, flexibility and user-friendliness. TALYS can be used for the analysis of basic scientific experiments or to generate nuclear data for applications.

Like most scientific projects, TALYS is always under development. Nevertheless, at certain moments in time, we freeze a well-defined version of TALYS and subject it to extensive verification and validation procedures. You are now reading the manual of version 0.64, the first version that is released to beta testers.

Many people have contributed to the present state of TALYS: In no particular order, and realizing that we probably forget someone, we thank Jacques Raynal for extending the ECIS-code according to our special wishes and for refusing to retire, Jean-Paul Delaroche and Olivier Bersillon for theoretical support, Emil Betak and Connie Kalbach for input on the pre-equilibrium models, Stéphane Goriely, Pascal Romain and Eric Bauge for specific computational advice, Steven van der Marck for careful reading of this manual, Jura Kopecky and Robin Forrest for testing many of the results of TALYS, and Mark Chadwick, Phil Young and Mike Herman for helpful discussions and for providing us the motivation to compete with their software.

TALYS-0.64 falls in the category of Beta software: This is software that is in the testing stage of its development. Please read the release conditions on the next page. Once the current beta testing phase has ended, we plan a more official release of the code. Although we have invested a lot of effort in the validation of our code, we will not make the mistake to guarantee perfection. Therefore, in exchange for the free use of TALYS: If you find any errors, or in general have any comments, corrections, extensions, questions or advice, we would like to hear about it. You can reach us at **koning@nrg-nl.com**, **stephane.hilaire@cea.fr** and **duijvestijn@nrg-nl.com** if you need one of us personally, but information that is of possible interest to all TALYS users should be send to the mailing list **talys-l@nrg-nl.com**. A webpage for TALYS is foreseen for 2005.

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# TALYS release terms

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In addition to the GNU GPL *terms* we have a few *requests*:

- Please inform (one of) the authors when you distribute TALYS further. We like to keep track of the users.
- When TALYS is used for your reports, publications, etc., please make a proper reference to the code. For TALYS-0.64 this is:  
A.J. Koning, S. Hilaire and M.C. Duijvestijn, “TALYS: Comprehensive nuclear reaction modeling”, *Proceedings of the International Conference on Nuclear Data for Science and Technology - ND2004*, Sep. 26 - Oct. 1, 2004, Santa Fe, USA, to be published.  
where “to be published” should be changed once the full publication details are known.
- Inform us about, or send, extensions you have built into TALYS. Of course, proper credit will be given to the authors of such extensions in future versions of the code.
- Send us a copy/preprint of reports and publications in which TALYS is used.



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# Chapter 1

## Introduction

TALYS is a computer code system for the analysis and prediction of nuclear reactions. The basic objective behind its construction is the simulation of nuclear reactions that involve neutrons, photons, protons, deuterons, tritons,  $^3\text{He}$ - and alpha-particles, in the 1 keV - 200 MeV energy range and for target nuclides of mass 12 and heavier. To achieve this, we have implemented a suite of nuclear reaction models into a single code system. This enables us to evaluate nuclear reactions from the unresolved resonance range up to intermediate energies.

There are two main purposes of TALYS, which are strongly connected. First, it is a *nuclear physics* tool that can be used for the analysis of nuclear reaction experiments. The interplay between experiment and theory gives us insight in the fundamental interaction between particles and nuclei, and precise measurements enable us to constrain our models. In return, when the resulting nuclear models are believed to have sufficient predictive power, they can give an indication of the reliability of measurements. The many examples we present at the end of this manual confirm that this software project would be nowhere without the existing (and future) experimental database.

After the nuclear physics stage comes the second function of TALYS, namely as a *nuclear data* tool: Either in a default mode, when no measurements are available, or after fine-tuning the adjustable parameters of the various reaction models using available experimental data, TALYS can *generate* nuclear data for all open reaction channels, on a user-defined energy and angle grid, beyond the resonance region. The nuclear data libraries that are constructed with these calculated and experimental results provide essential information for existing and new nuclear technologies. Important applications that rely directly or indirectly on data libraries generated by nuclear reaction simulation codes like TALYS are: conventional and innovative power reactors (GEN-IV), accelerator-driven systems and transmutation of radioactive waste, fusion reactors, homeland security, medical isotope production and radiotherapy, oil-well logging, geophysics and astrophysics. Before this release, TALYS has already been used for both basic and applied scientific purposes. A non-exhaustive list of publications that contain an analysis with TALYS is given in Refs. [1]-[30].

The development of TALYS follows the “first completeness, then quality” principle. This should certainly not suggest that we use toy models to arrive at some quick and dirty results. On the contrary, several reaction mechanisms coded in TALYS are based on theoretical models whose implementation is only possible with the current-day computer power. It rather means that, in our quest for completeness, we try to divide our effort equally among all nuclear reaction types. The precise description of *all* possible reaction channels in a single calculational scheme is such an enormous task that we have chosen, to put it bluntly, not to devote several years to the theoretical research and absolutely perfect implementation of one particular reaction channel which accounts for only a few millibarns of the total reaction

cross section. Instead, we aim to enhance the quality of TALYS equally over the whole reaction range and always search for the largest shortcoming that remains after the last improvement. The reward of this approach is that with TALYS we can already cover the whole path from fundamental nuclear reaction models to the creation of complete data libraries for nuclear applications, with the obvious side note that the implemented nuclear models will always need to be upgraded. An additional long-term aim is full transparency of the implemented nuclear models, in other words, an *understandable* source program, and a modular coding structure.

The idea to construct a computer program that gives a simultaneous prediction of many nuclear reaction channels, rather than a very detailed description of only one or a few reaction channels, is not new. Well-known examples of all-in-one codes from the past decades are GNASH [31], ALICE [32], STAPRE [33], and EMPIRE [34]. They have been, and are still, extensively used, not only for academical purposes but also for the creation of the nuclear data libraries that exist around the world. GNASH and EMPIRE are still being maintained and extended by the original authors, whereas various local versions of ALICE and STAPRE exist around the world, all with different extensions and improvements. We note that at the time of this writing, a nuclear model code project is also under development in Los Alamos. TALYS is new in the sense that it has been recently written completely from scratch (with the exception of one very essential module, the coupled-channels code ECIS), using a consistent set of programming procedures.

As specific features of TALYS we mention

- In general, an exact implementation of many of the latest nuclear models for direct, compound, pre-equilibrium and fission reactions.
- A continuous, smooth description of reaction mechanisms over a wide energy range (0.001- 200 MeV) and mass number range ( $12 < A < 339$ ).
- Completely integrated optical model and coupled-channels calculations by the ECIS-97 code [35].
- Incorporation of recent optical model parameterisations for many nuclei.
- Total and partial cross sections, energy spectra, angular distributions, double-differential spectra and recoils.
- Discrete and continuum photon production cross sections.
- Excitation functions for residual nuclide production, including isomeric cross sections.
- An exact modeling of exclusive channel cross sections, e.g.  $(n, 2np)$ , spectra, and recoils.
- Automatic reference to nuclear structure parameters as masses, discrete levels, resonances, level density parameters, deformation parameters, fission barrier and gamma-ray parameters, generally from the IAEA Reference Input Parameter Library [36].
- Various width fluctuation models for binary compound reactions and, at higher energies, multiple Hauser-Feshbach emission until all reaction channels are closed.
- Various phenomenological and microscopic level density models.
- Various fission models to predict cross sections and fission fragment and product yields.
- Models for pre-equilibrium reactions, and multiple pre-equilibrium reactions up to any order.

- Use of systematics if an adequate theory for a particular reaction mechanism is not yet available or implemented, or simply as a predictive alternative for more physical nuclear models.
- Automatic generation of nuclear data in ENDF-6 format (not included in the beta release).
- A transparent source program.
- Input/output communication that is easy to use and understand.
- An extensive user manual.
- A large collection of sample cases.

The central message is that we always provide a complete set of answers for a nuclear reaction, for all open channels and all associated cross sections, spectra and angular distributions. It depends on the current status of nuclear reaction theory, and our ability to model that theory, whether these answers are generated by more or less sophisticated physical methods or by simple systematics. With TALYS, a complete set of cross sections can already be obtained with minimal effort, through a four-line input file of the type:

```
projectile n
element     Fe
mass       56
energy     14.
```

which, if you are only interested in reasonable answers for the most important quantities, will give you all you need. If you want to be more specific on nuclear models, their parameters and the level of output, you simply add some of the more than 150 keywords that can be specified in TALYS. Let us immediately stress that we realize the danger of this approach. This ease of use may give the obviously false impression that one gets a *good* description of *all* the reaction channels, with minimum reaction specification, as if we would have solved virtually all nuclear reaction problems (in which case we would have been famous). Unfortunately, nuclear physics is not that simple. Clearly, many types of nuclear reactions are very difficult to model properly and can not be expected to be covered by simple default values. Moreover, other nuclear reaction codes may outperform TALYS on particular tasks because they were specifically designed for one or a few reaction channels. In this light, Section 8.3 is very important, as it contains many sample cases which should give the user an idea of what TALYS can do. We wish to mention that the above sketched method for handling input files was born out of frustration: We have encountered too many computer codes containing an implementation of beautiful physics, but whose input files are supposed to consist of a large collection of mixed, and intercorrelated, integer and real values, making the threshold to use such codes unnecessarily high.

## 1.1 How to use this manual

Although we would be honored if you would read this manual from the beginning to the end, we can imagine that not all parts are necessary, relevant or suitable to you. For example if you are just an interested physicist who does not own a computer, you may skip

Chapter 2: Installation guide.

while everybody else probably needs Chapter 2. A complete description of all nuclear models and other basic information present in TALYS, as well as the description of the types of cross sections, spectra, angular distributions etc. that can be produced with the code can be found in the next three chapters,

Chapter 3: A general discussion of nuclear reactions and the types of observables that can be obtained.

Chapter 4: A discussion of the theory behind the various nuclear models that are implemented in TALYS.

Chapter 5: A description of the various nuclear structure parameters that are used.

If you are an experienced nuclear model physicist and want to compute your own specific cases directly after a successful installation, then instead of reading chapters 3-5 you may go directly to

Chapter 6: Input description.

People planning to enter the source code for extensions, changes or debugging, may be interested in

Chapter 7: The detailed computational structure of TALYS.

The next chapter we consider to be quite important, since it contains ready to use starting points (sample cases) for your own work. At the same time, it gives an impression of what TALYS can be used for. That and associated matters can be found in

Chapter 8: Output description, sample cases and verification and validation.

Finally, this manual ends with

Chapter 9: Conclusions and ideas for future work.

## Chapter 2

# Installation and getting started

### 2.1 The TALYS package

In what follows we assume TALYS will be installed from a CDROM on a Unix/Linux operating system. The total TALYS package is in the *talys/* directory and contains the following directories and files:

- *README* outlines the contents of the package.
- *talys.setup* is a script that takes care of the installation.
- *source/* contains the source code of TALYS: 254 Fortran subroutines, and the file *talys.cmb*, which contains all variable declarations and common blocks. This includes the file *ecis97t.f*. This is basically Jacques Raynal's code ECIS-97, which we have transformed into a subroutine and slightly modified to generate extra output that is not given by the original version of ECIS.
- *structure/* contains the nuclear structure database in various subdirectories. See Chapter 5 for more information.
- *doc/* contains the documentation: this manual in postscript and pdf format and the description of ECIS-97.
- *samples/* contains the input and output files of the sample cases.

In total, you will need about 300 Mb of free disk space to install TALYS. The code has so far *only* been tested on various Unix/Linux systems, so we can not guarantee that it works on all operating systems. However, the only machine dependences we can think of are the directory separators '/' we use in pathnames that are hardwired in the code, and the handling of various files for calculations that involve natural targets. Also, the output of the execution time in *timer.f* may be machine dependent.

TALYS has been tested for the following compilers and operating systems:

- Fujitsu Fortran90/95 compiler v1.0 on Linux Red Hat 5
- Fujitsu/Lahey Fortran90/95 compiler v6.1 on Linux Red Hat 9
- gnu g77 Fortran77 compiler on all Linux systems

- Workshop 6.2 Fortran77 compiler on the SUN workstation

The code does *not* work with the new GNU g95 Fortran-95 compiler. The reason is that ECIS-97 contains a few peculiarities that are not accepted by g95. The new ECIS-03 code, which we will include in a future version of TALYS, remedies this.

## 2.2 Installation

The installation of TALYS is straightforward. The first step is

- Copy the CDROM to your hard disk.

For a Unix/Linux system, the installation is expected to be handled by the *talys.setup* script, as follows

- edit *talys.setup* and set the first two variables: the name of your compiler and the place where you want to store the TALYS executable.
- **talys.setup**

If this does not work for some reason, we here provide the necessary steps to do the installation manually. For a Unix/Linux system, the following steps should be taken:

- **chmod -R u+rwX talys** to ensure that all directories and files have read and write permission and the directories have execute permission. (These permissions are usually disabled when reading from a CDROM).
- **cd talys/source**
- Ensure that TALYS can read the nuclear structure database. This is done in subroutine *machine.f*. If *talys.setup* has not already replaced the path name in *machine.f*, do it yourself. We think this is the only Unix/Linux machine dependence of TALYS. Apart from a few trivial warning messages for *ecis97t.f*, we expect no complaints from the compiler.
- **f90 -c \*.f**
- **f90 \*.o -o talys**
- **mv talys ~/bin** (assuming you have a *~/bin* directory which contains all executables that can be called from any working directory)

After you or *talys.setup* has completed this, type

- **rehash**, to update your table with commands.

The above commands represent the standard compilation options. Consult the manual of your compiler to get an enhanced performance with optimization flags enabled. The only restriction for compilation is that *ecis97t.f* should *not* be compiled in double precision.

## 2.3 Verification

If TALYS is installed, testing the sample cases is the logical next step. The *samples/* directory contains the script *verify* that runs all the test cases. Each sample case has its own subdirectory, which contains a subdirectory *org/*, where we stored the input files and **our** calculated results, obtained with the Fujitsu/Lahey v6.1 compiler on Linux Red Hat 9. It also contains a subdirectory *new*, where we have stored the input files only and where the *verify* script will produce **your** output files. A full description of the keywords used in the input files is given in Chapter 6. Section 8.3 describes all sample cases in full detail. Note that under Linux/Unix, in each subdirectory a file with differences with our original output is created.

Should you encounter error messages upon running TALYS, like '*killed*' or '*segmentation fault*', then probably the memory of your processor is not large enough (i.e. smaller than 256 Mb). Edit *talys.cmb* and reduce the value of **memorypar**.

## 2.4 Getting started

If you have created your own working directory with an input file named e.g. *input*, then a TALYS calculation can easily be started with:

**talys < input > output**

where the names *input* and *output* are not obligatory: you can use any name for these files.



## Chapter 3

# Nuclear reactions: General approach

An outline of the general theory and modeling of nuclear reactions can be given in many ways. A common classification is in terms of time scales: short reaction times are associated with direct reactions and long reaction times with compound nucleus processes. At intermediate time scales, pre-equilibrium processes occur. An alternative, more or less equivalent, classification can be given with the number of intranuclear collisions, which is one or two for direct reactions, a few for pre-equilibrium reactions and many for compound reactions, respectively. As a consequence, the coupling between the incident and outgoing channels decreases with the number of collisions and the statistical nature of the nuclear reaction theories increases with the number of collisions. Figs. 3.1 and 3.2 explain the role of the different reaction mechanisms during an arbitrary nucleon-induced reaction in a schematic manner. They will all be discussed in this manual.

This distinction between nuclear reaction mechanisms can be obtained in a more formal way by means of a proper division of the nuclear wave functions into open and closed configurations, as detailed for example by Feshbach's many contributions to the field. This is the subject of several textbooks and will not be repeated here. When appropriate, we will return to the most important theoretical aspects of the nuclear models in TALYS in Chapter 4.

When discussing nuclear reactions in the context of a computer code, as in this manual, a different starting point is more appropriate. We think it is best illustrated by Fig. 3.3. A particle incident on a target nucleus will induce several *binary* reactions which are described by the various competing reaction mechanisms that were mentioned above. The end products of the binary reaction are the emitted particle and the corresponding recoiling residual nucleus. In general this is, however, not the end of the process. A total nuclear reaction may involve a whole sequence of residual nuclei, especially at higher energies, resulting from multiple particle emission. All these residual nuclides have their own separation energies, optical model parameters, level densities, fission barriers, gamma strength functions, etc., that must properly be taken into account along the reaction chain. The implementation of this entire reaction chain forms the backbone of TALYS. The program has been written in a way that enables a clear and easy inclusion of all possible nuclear model ingredients for any number of nuclides in the reaction chain. Of course, in this whole chain the target and primary compound nucleus have a special status, since they are subject to *all* reaction mechanisms, i.e. direct, pre-equilibrium, compound and fission and, at low incident energies, width fluctuation corrections in compound nucleus decay. Also, at incident energies below a few MeV, only binary reactions take place and the target and compound nucleus are often the

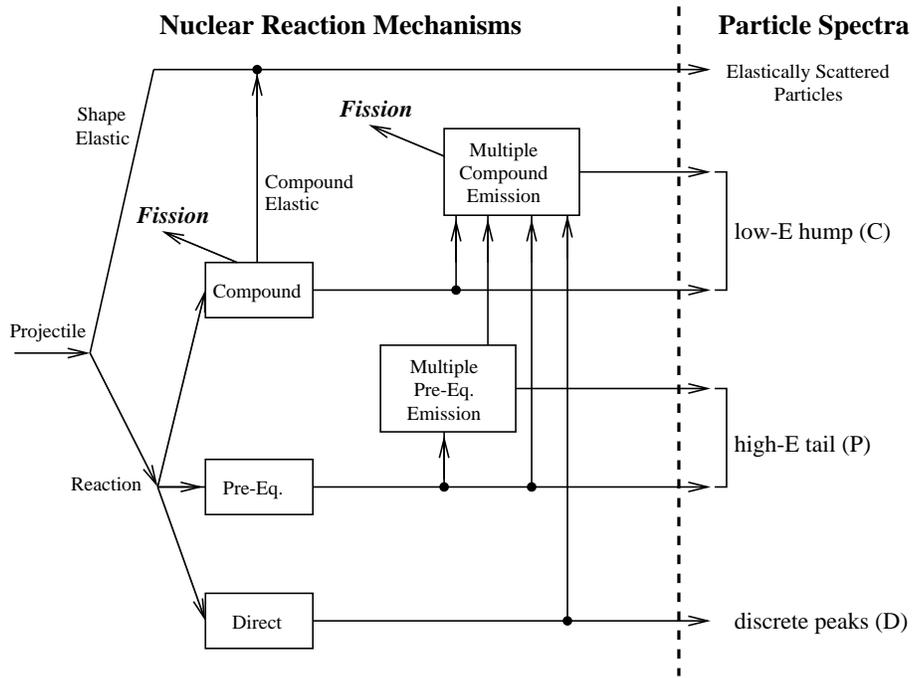


Figure 3.1: The role of direct, pre-equilibrium and compound processes in the description of a nuclear reaction and the outgoing particle spectra. The C, P and D labels correspond to those in Fig. 3.2

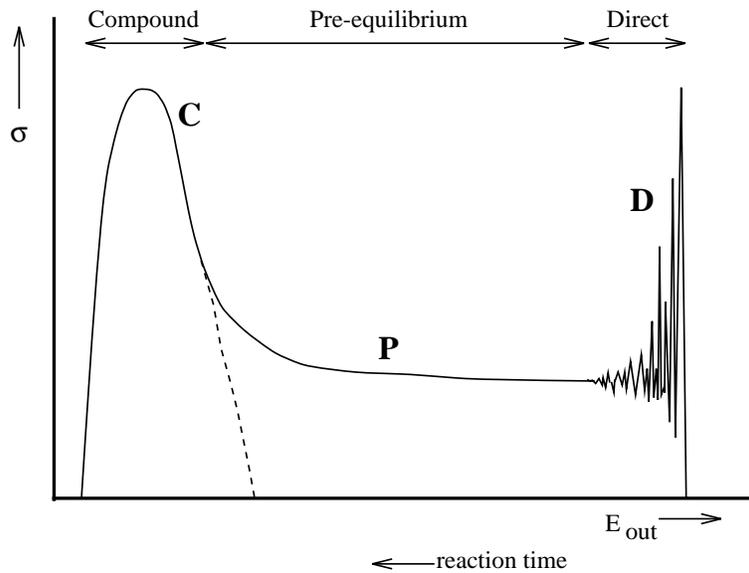


Figure 3.2: Schematical drawing of an outgoing particle spectrum. The energy regions to which direct (D), pre-equilibrium (P) and compound (C) mechanisms contribute are indicated. The dashed curve distinguishes the compound contribution from the rest in the transitional energy region.

only two nuclei involved in the whole reaction. Historically, it is for the binary reactions that most of the theoretical methods have been developed and refined, mainly because their validity, and their relation with nuclear structure, could best be tested with exclusive measurements. In general, however, Fig. 3.3 should serve as the illustration of a total nuclear reaction at any incident energy. The projectile, in this case a neutron, and the target ( $Z_C, N_C - 1$ ) form a compound nucleus ( $Z_C, N_C$ ) with a total energy

$$E^{tot} = E_{CM} + S_n(Z_{CN}, N_{CN}) + E_x^0, \quad (3.1)$$

where  $E_{CM}$  is the incident energy in the CM frame,  $S_n$  is the neutron separation energy of the compound nucleus, and  $E_x^0$  the excitation energy of the target (which is usually zero, i.e. representing the ground state). The compound nucleus is described by a range of possible spin ( $J$ ) and parity ( $\Pi$ ) combinations, which for simplicity are left out of Fig. 3.3. From this state, transitions to all open channels may occur by means of direct, pre-equilibrium and compound processes. The residual nuclei formed by these binary reactions may be populated in the discrete level part and in the continuum part of the available excitation energy range. In Fig. 3.3, we have only drawn three binary channels, namely the ( $Z_C, N_C - 1$ ), ( $Z_C - 1, N_C$ ) and ( $Z_C - 1, N_C - 1$ ) nuclei that result from binary neutron, proton and deuteron emission, respectively. Each nucleus is characterized by a separation energy per possible ejectile. If the populated residual nucleus has a maximal excitation energy  $E_x^{max}(Z, N)$  that is still above the separation energies for one or more different particles for that nucleus, further emission of these particles may occur and nuclei with lower  $Z$  and  $N$  will be populated. At the end of the nuclear reaction (left bottom part of Fig. 3.3), all the reaction population is below the lowest particle separation energy, and the residual nucleus ( $Z_C - z, N_C - n$ ) can only decay to its ground or isomeric states by means of gamma decay. In a computer program, the continuum must be discretized in excitation energy ( $E_x$ ) bins. We have taken these bins equidistant, although we already want to stress the important fact here that the *emission* energy grid for the outgoing particles is non-equidistant in TALYS. After the aforementioned binary reaction, every continuum excitation energy bin will be further depleted by means of particle emission, gamma decay or fission. Computationally, this process starts at the initial compound nucleus and its highest energy bin, i.e. the bin just below  $E_x^{max}(Z_C, N_C) = E^{tot}$ , and subsequently in order of decreasing energy bin/level, decreasing  $N$  and decreasing  $Z$ . Inside each continuum bin, there is an additional loop over all possible  $J$  and  $\Pi$ , whereas for each discrete level,  $J$  and  $\Pi$  have unique values. Hence, a bin/level is characterized by the set  $\{Z, N, E_x, J, \Pi\}$  and by means of gamma or particle emission, it can decay into all accessible  $\{Z', N', E_{x'}, J', \Pi'\}$  bins/levels. In this way, the whole reaction chain is followed until all bins and levels are depleted and thus all channels are closed. In the process, all particle production cross sections and residual production cross sections are accumulated to their final values.

We will now zoom in on the various parts of Fig. 3.3 to describe the various stages of the reaction, depending on the incident energy, and we will mention the nuclear reaction mechanisms that apply.

### 3.1 Reaction mechanisms

In the projectile energy range between 1 keV and several hundreds of MeV, the importance of a particular nuclear reaction mechanism appears and disappears upon varying the incident energy. We will now describe the particle decay scheme that typically applies in the various energy regions. Because of the Coulomb barrier for charged particles, it will be clear that the discussion for low energy reactions usually

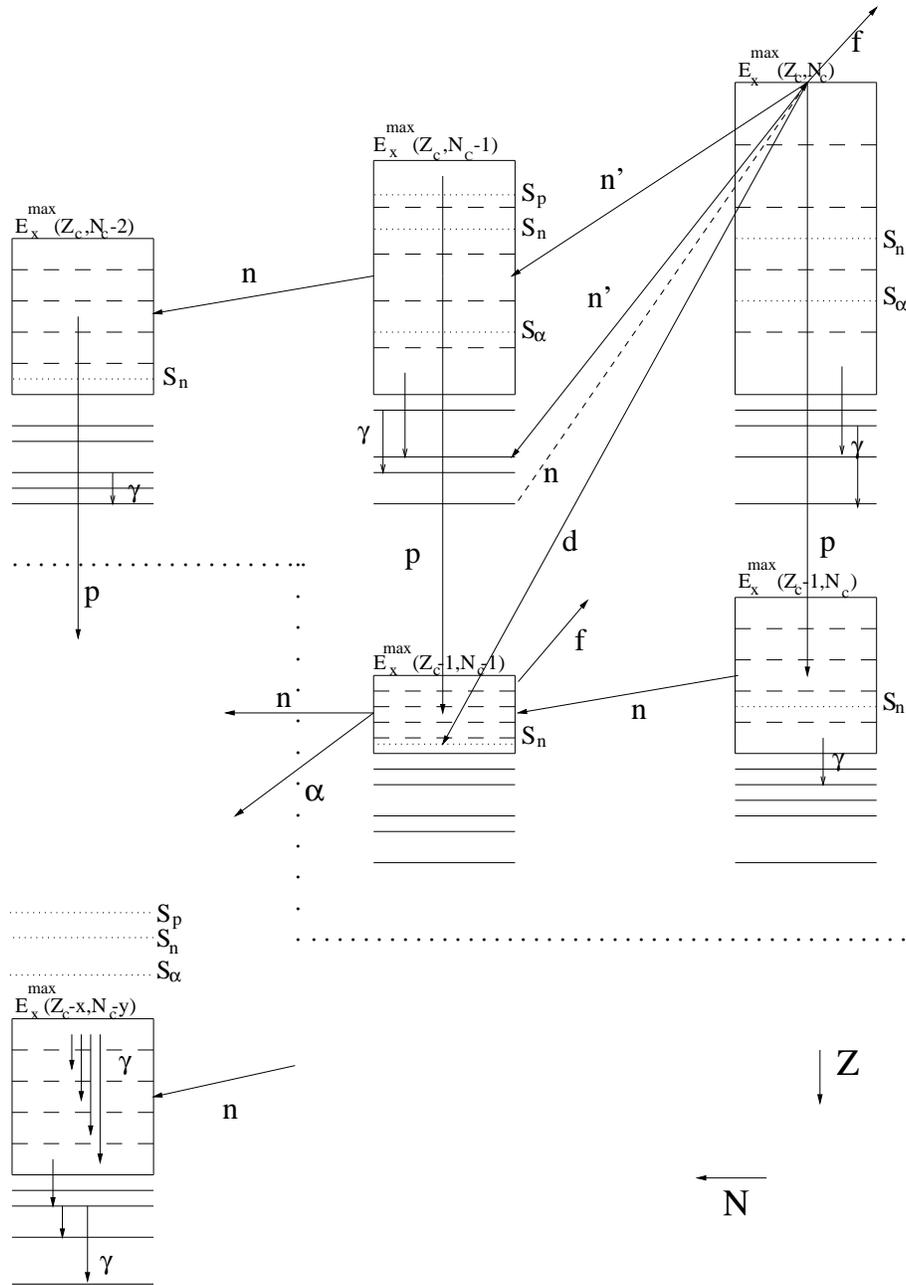


Figure 3.3: Neutron-induced reaction. The dashed arrow represents the incident channel, while the continuous arrows represent the decay possibilities.  $E_x^{max}$  denotes the maximal possible excitation energy of each nucleus and  $S_k$  is the particle separation energy for particle  $k$ . For each nucleus a few discrete levels are drawn, together with a few continuum energy bins. Spin and parity degrees of freedom are left out of this figure for simplicity. Fission is indicated by an  $f$ .

concerns incident neutrons. In general, however, what follows can be generalized to incident charged particles. The energy ranges mentioned in each paragraph heading are just meant as helpful indications, which apply for a typical medium mass nucleus.

### 3.1.1 Low energies

#### Elastic scattering and capture ( $E < 0.2$ MeV)

If the energy of an incident neutron is below the excitation energy of the first inelastic level, and if there are no  $(n, p)$ , etc. reactions that are energetically possible, then the only reaction possibilities are elastic scattering, neutron capture and, for fissile nuclides, fission. At these low energies, only the  $(Z_C, N_C - 1)$  and  $(Z_C, N_C)$  nuclides of Fig. 3.3 are involved, see Fig. 3.4. First, the shape (or direct) elastic scattering cross section can directly be determined from the optical model, which will be discussed in Section 4.1. The compound nucleus, which is populated by a reaction population equal to the reaction cross section, is formed at one single energy  $E^{tot} = E_x^{max}(Z_C, N_C)$  and a range of  $J, \Pi$ -values. This compound nucleus either decays by means of compound elastic scattering back to the initial state of the target nucleus, or by means of neutron capture, after which gamma decay follows to the continuum and to discrete states of the compound nucleus. The competition between the compound elastic and capture channels is described by the compound nucleus theory, which we will discuss in Section 4.5. To be precise, the elastic and capture processes comprise the first *binary* reaction. To complete the description of the total reaction, the excited  $(Z_C, N_C)$  nucleus, which is populated over its whole excitation energy range by the primary gamma emission, must complete its decay. The highest continuum bin is depleted first, for all  $J$  and  $\Pi$ . The subsequent gamma decay increases the population of the lower bins, before the latter are depleted themselves. Also, continuum bins that are above the neutron separation energy  $S_n$  of the compound nucleus contribute to the feeding of the  $(n, \gamma n)$  channel. This results in a weak continuous neutron spectrum, even though the elastic channel is the only true binary neutron channel that is open. The continuum bins and the discrete levels of the compound nucleus are depleted one by one, in decreasing order, until the ground or an isomeric state of the compound nucleus is reached by subsequent gamma decay. If a nuclide is fissile, fission may compete as well, both from the initial compound state  $E_x^{max}(Z_C, N_C)$  and from the continuum bins of the compound nucleus, the latter resulting in a  $(n, \gamma f)$  cross section. Both contributions add up to the so called first-chance fission cross section.

#### Inelastic scattering to discrete states ( $0.2 < E < 4$ MeV)

At somewhat higher incident energies, the first inelastic channels open up, see Fig. 3.5. Reactions to these discrete levels have a compound and a direct component. The former is again described by the compound nucleus theory, while the latter is described by the Distorted Wave Born Approximation (DWBA) for spherical nuclei and by coupled-channels equations for deformed nuclei, see Section 4.2. When the incident energy crosses an inelastic threshold, the compound inelastic contribution rises rapidly and predominates, whereas the direct component increases more gradually. Obviously, the elastic scattering, capture and fission processes described in the previous subsection also apply here. In addition, there is now gamma decay to an isomeric state or the ground state in the target nucleus after inelastic scattering. When there are several, say 10, inelastic levels open to decay, the compound contribution to each individual level is still significant. However, the effect of the width fluctuation correction on the compound

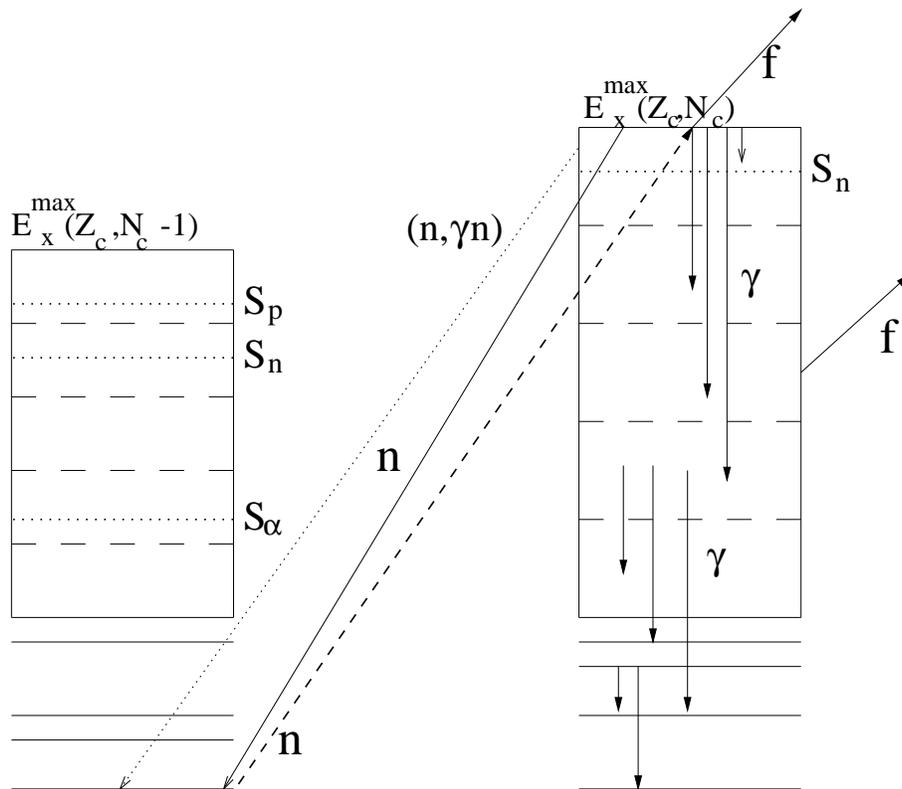


Figure 3.4: Neutron-induced reaction at low energy. The dashed arrow represents the incident channel, while the continuous arrows represents the elastic channel. The only possibilities are elastic scattering and capture of the neutron in the compound nucleus, with subsequent decay to the ground state or an isomeric state of the compound nucleus. A small part of the population may decay to the target nucleus by means of the  $(n, \gamma n)$  channel (dotted arrow). For fissile nuclei, fission may be another open channel.

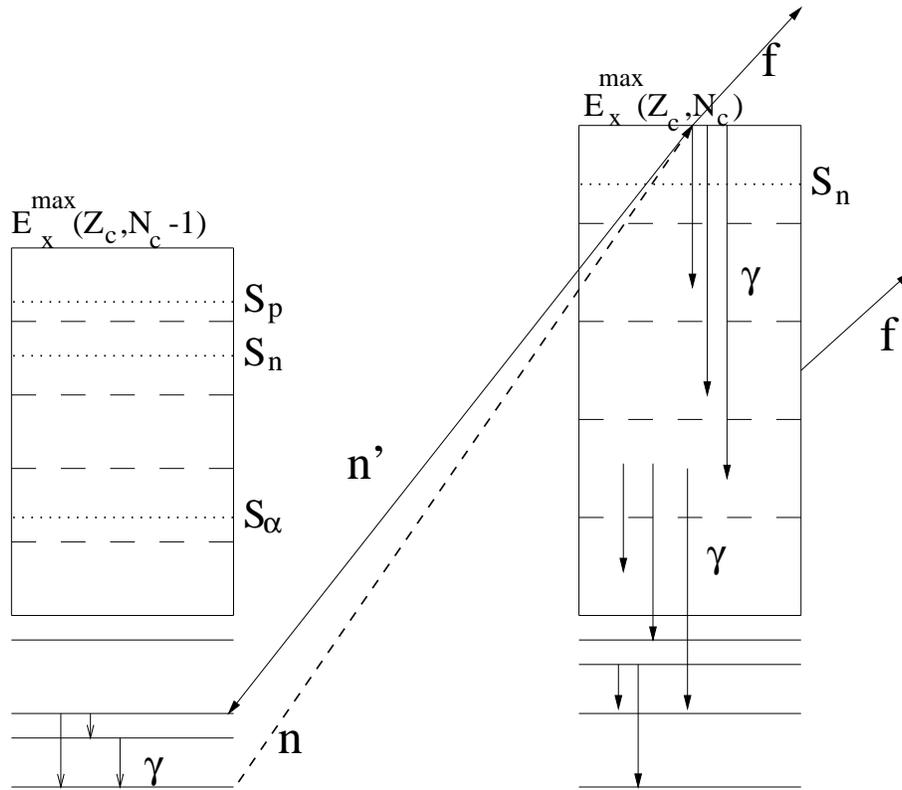


Figure 3.5: Neutron-induced reaction at somewhat higher energy. The dashed arrow represents the incident channel, while the continuous arrows represent the decay possibilities. In addition to the possibilities sketched in the previous figure, there is now inelastic scattering followed by gamma decay in the target nucleus.

cross section is already small in this case, as will be outlined in Section 4.5.

### 3.1.2 High energies

#### Pre-equilibrium reactions ( $E > 4$ MeV)

At higher incident energies, inelastic cross sections to both the discrete states and the continuum are possible, see Fig. 3.3. Like reactions to discrete states, reactions to the continuum also have a compound and a direct-like component. The latter are usually described by pre-equilibrium reactions which, by definition, include direct reactions to the continuum. They will be discussed in Section 4.4. Also non-elastic channels to other nuclides, through charge-exchange, e.g.  $(n, p)$ , and transfer reactions, e.g.  $(n, \alpha)$ , generally open up at these energies, and decay to these nuclides can take place by the same direct, pre-equilibrium and compound mechanisms. Again, the channels described in the previous subsections also apply here. In addition, gamma decay to ground and isomeric states of all residual nuclides occurs. When many channels open up, particle decay to individual states (e.g. compound elastic scattering) rapidly becomes negligible. For the excitation of a discrete state, the direct component now becomes predominant, since that involves no statistical competition with the other channels. At about 15 MeV,

the *total* compound cross section, i.e. summed over all final discrete states and the excited continuum, is however still larger than the summed direct and pre-equilibrium contributions.

### Multiple compound emission ( $E > 8$ MeV)

At incident energies above about the neutron separation energy, the residual nuclides formed after the first binary reaction contain enough excitation energy to enable further decay by compound nucleus particle emission or fission. This gives rise to multiple reaction channels such as  $(n, 2n)$ ,  $(n, np)$ , etc. For higher energies, this picture can be generalized to many residual nuclei, and thus more complex reaction channels, as explained in the introduction of this Chapter, see also Fig. 3.3. If fission is possible, this may occur for all residual nuclides, which is known as multiple chance fission. All excited nuclides will eventually decay to their isomeric and ground states.

### Multiple pre-equilibrium emission ( $E > 40$ MeV)

At still higher incident energies, above several tens of MeV, the residual nuclides formed after binary emission may contain so much excitation energy that the presence of further *fast* particles inside the nucleus becomes possible. These can be imagined as strongly excited particle-hole pairs resulting from the first binary interaction with the projectile. The residual system is then clearly non-equilibrated and the excited particle that is high in the continuum may, in addition to the first emitted particle, also be emitted on a short time scale. This so-called multiple pre-equilibrium emission forms an alternative theoretical picture of the intra-nuclear cascade process, whereby now not the exact location and momentum of the particles is followed, but instead the total energy of the system and the number of particle-hole excitations (exciton number). In TALYS, this process can be generalized to any number of multiple pre-equilibrium stages in the reaction by keeping track of all successive particle-hole excitations, see Section 4.6.2. For these incident energies, the binary compound cross section becomes small: the non-elastic cross section is almost completely exhausted by primary pre-equilibrium emission. Again, Fig. 3.3 applies.

## 3.2 Cross section definitions

In TALYS, cross sections for reactions to all open channels are calculated. Although the types of most of these partial cross sections are generally well known, it is appropriate to define them for completeness. This section concerns basically the book-keeping of the various cross sections, including all the sum rules they obey. The particular nuclear models that are needed to obtain them are described in Chapter 4. Thus, we do not yet give the definition of cross sections in terms of more fundamental quantities. Unless otherwise stated, we use incident neutrons as example in what follows and we consider only photons ( $\gamma$ ), neutrons (n), protons (p), deuterons (d), tritons (t), helium-3 particles (h) and alpha particles ( $\alpha$ ) as competing particles. Also, to avoid an overburdening of the notation and the explanation, we will postpone the competition of fission to the last section of this Chapter.

### 3.2.1 Total cross sections

The most basic nuclear reaction calculation is that with the optical model, which will be explained in more detail in Section 4.1. Here, it is sufficient to summarize the relations that can be found in many

nuclear reaction textbooks, namely that the optical model yields the *reaction cross section*  $\sigma_{\text{reac}}$  and, in the case of neutrons, the *total cross section*  $\sigma_{\text{tot}}$  and the *shape-elastic cross section*  $\sigma_{\text{shape-el}}$ . They are related by

$$\sigma_{\text{tot}} = \sigma_{\text{shape-el}} + \sigma_{\text{reac}}. \quad (3.2)$$

If the elastic channel is, besides shape elastic scattering, also fed by compound nucleus decay, the latter component is a part of the reaction cross section and is called the *compound elastic cross section*  $\sigma_{\text{comp-el}}$ . With this, we can define the *total elastic cross section*  $\sigma_{\text{el}}$ ,

$$\sigma_{\text{el}} = \sigma_{\text{shape-el}} + \sigma_{\text{comp-el}}, \quad (3.3)$$

and the *non-elastic cross section*  $\sigma_{\text{non-el}}$ ,

$$\sigma_{\text{non-el}} = \sigma_{\text{reac}} - \sigma_{\text{comp-el}}, \quad (3.4)$$

so that we can combine these equations to give

$$\sigma_{\text{tot}} = \sigma_{\text{el}} + \sigma_{\text{non-el}}. \quad (3.5)$$

The last equation contains the quantities that can actually be measured in an experiment. We also note that the competition between the many compound nucleus decay channels ensures that  $\sigma_{\text{comp-el}}$  rapidly diminishes for incident neutron energies above a few MeV, in which case  $\sigma_{\text{non-el}}$  becomes practically equal to  $\sigma_{\text{reac}}$ .

A further subdivision of the outcome of a nuclear reaction concerns the breakdown of  $\sigma_{\text{non-el}}$ : this cross section contains all the partial cross sections. For this we introduce the exclusive cross sections, from which all other cross sections of interest can be derived.

### 3.2.2 Exclusive cross sections

In this manual, we call a cross section *exclusive* when the outgoing channel is precisely specified by the type and number of outgoing particles (+ any number of photons). Well-known examples are the inelastic or  $(n, n')$  cross section and the  $(n, 2n)$  cross section, which corresponds with two, *and only* two, neutrons (+ accompanying photons) in the outgoing channel. We denote the *exclusive cross section* as  $\sigma^{\text{ex}}(i_n, i_p, i_d, i_t, i_h, i_\alpha)$ , where  $i_n$  stands for the number of outgoing neutrons, etc. In this notation, where the incident particle is assumed implicit, e.g. the  $(n, 2np)$  cross section is given by  $\sigma^{\text{ex}}(2, 1, 0, 0, 0, 0)$ , for which we will also use the shorthand notation  $\sigma_{n,2np}$ . For a non-fissile nucleus, the sum over all exclusive cross sections is equal to the non-elastic cross section

$$\sigma_{\text{non-el}} = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} \sigma^{\text{ex}}(i_n, i_p, i_d, i_t, i_h, i_\alpha), \quad (3.6)$$

provided we impose that  $\sigma^{\text{ex}}(1, 0, 0, 0, 0, 0)$  is the exclusive *inelastic* cross section  $\sigma_{n,n'}$ , i.e. it does not include shape- or compound elastic scattering.

The precise calculation of exclusive cross sections and spectra is a complicated book-keeping problem which, to our knowledge, has not been properly documented. We will describe the exact formalism here. In what follows we use quantities with a prime for daughter nuclides and quantities without a

prime for mother nuclides in a decay chain. Consider an excitation energy bin or discrete level  $E_x$  in a nucleus  $(Z, N)$ . Let  $P(Z, N, E_x)$  represent the population of this bin/level before it decays. Let  $s_k(Z, N, E_x, E_{x'})$  be the part of the population that decays from the  $(Z, N, E_x)$  bin/level to the residual  $(Z', N', E_{x'})$  bin/level, whereby  $(Z, N)$  and  $(Z', N')$  are connected through the particle type  $k$ , with the index  $k$  running from  $\gamma$ -rays up to  $\alpha$ -particles. With these definitions, we can link the various residual nuclides while keeping track of all intermediate particle emissions. A special case for the population is the initial compound nucleus  $(Z_C, N_C)$ , which contains all the initial reaction population at its total excitation energy  $E_x^{max}$  (projectile energy + binding energy), i.e.

$$P(Z_C, N_C, E_x^{max}) = \sigma_{non-el}, \quad (3.7)$$

while all other population bins/levels are zero. For the initial compound nucleus,  $s_k(Z_C, N_C, E_x^{max}, E_{x'})$  represents the binary feeding to the excitation energy bins of the first set of residual nuclides. This term generally consists of direct, pre-equilibrium and compound components.

The population of any bin in the decay chain is equal to the sum of the decay parts for all particles that can reach this bin from the associated mother bins, i.e.

$$P(Z', N', E_{x'}(i')) = \sum_{k=\gamma,n,p,d,t,h,\alpha} \sum_i s_k(Z, N, E_x(i), E_{x'}(i')), \quad (3.8)$$

where the sum over  $i$  runs over discrete level and continuum energy bins in the energy range from  $E_{x'}(i') + S_k$  to  $E_x^{max}(Z, N)$ , where  $S_k$  is the separation energy of particle  $k$  so that the sum only includes decay that is energetically allowed, and  $E_x^{max}(Z, N)$  is the maximum possible excitation energy of the  $(Z, N)$  nucleus. Note again that the particle type  $k$  determines  $(Z, N)$ .

To obtain the exclusive cross sections, we need to start with the initial compound nucleus and work our way down to the last nucleus that can be reached. First, consider a daughter nucleus  $(Z', N')$  somewhere in the reaction chain. We identify all exclusive channels  $(i_n, i_p, i_d, i_t, i_h, i_\alpha)$  that lead to this residual  $(Z', N')$  nucleus, i.e. all channels that satisfy

$$\begin{aligned} i_n + i_d + 2i_t + i_h + 2i_\alpha &= N_C - N' \\ i_p + i_d + i_t + 2i_h + 2i_\alpha &= Z_C - Z'. \end{aligned} \quad (3.9)$$

For each of these channels, the *inclusive* cross section per excitation energy bin  $S$  is equal to the sum of the feeding from all possible mother bins, i.e.

$$\begin{aligned} S(i_n, i_p, i_d, i_t, i_h, i_\alpha, E_{x'}(i')) &= \sum_{k=\gamma,n,p,d,t,h,\alpha} \sum_i \frac{s_k(Z, N, E_x(i), E_{x'}(i'))}{P(Z, N, E_x(i))} \\ \times S(i_n - \delta_{nk}, i_p - \delta_{pk}, i_d - \delta_{dk}, i_t - \delta_{tk}, i_h - \delta_{hk}, i_\alpha - \delta_{\alpha k}, E_x(i)), \end{aligned} \quad (3.10)$$

where we introduce Kronecker delta's, with characters as subscript, as

$$\begin{aligned} \delta_{nk} &= 1 \text{ if } k = n \text{ (neutron)} \\ &= 0, \text{ otherwise} \end{aligned} \quad (3.11)$$

and similarly for the other particles. Note that  $S$  is still inclusive in the sense that it is not yet depleted for further decay. The summation runs over the excitation energies of the mother bin from which decay

into the  $E_{x'}(i')$  bin of the residual nucleus is energetically allowed. Feeding by gamma decay from bins above the  $(Z', N', E_{x'}(i'))$  bin is taken into account by the  $k = \gamma$  term, in which case all of the Kronecker delta's are zero.

With Eq. (3.7) as initial condition, the recursive procedure is completely defined. For a fixed nucleus, Eq. (3.10) is calculated for all excitation energy bins, in decreasing order, until the remaining population is in an isomeric or the ground state of the nucleus. When there is no further decay possible, the exclusive cross section per ground state/isomer, numbered by  $i$ , can be identified,

$$\sigma_i^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha) = S(i_n, i_p, i_d, i_t, i_h, i_\alpha, E_i). \quad (3.12)$$

The total exclusive cross section for a particular channel is then calculated as

$$\sigma^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha) = \sum_{i=0, \text{isomers}} \sigma_i^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha). \quad (3.13)$$

The procedure outlined above automatically sorts and stores all exclusive cross sections, irrespective of the order of particle emission within the reaction chain. For example, the  $(n, np)$  and  $(n, pn)$  channels are automatically added. The above formalism holds *exactly* for an arbitrary number of emitted particles.

We stress that keeping track of the excitation energy  $E_x$  throughout this formalism is essential to get the exact exclusive cross sections for two reasons:

- (i) the exact determination of the branching ratios for exclusive isomeric ratios. The isomeric ratios for different exclusive reactions that lead to the same residual product, e.g.  $(n, np)$  and  $(n, d)$ , both leading to  $(Z_C - 1, N_C - 1)$ , are generally different from each other and thus also from the isomeric ratios of the total residual product. Hence, it would be an approximation to apply isomeric branching ratios for residual products, obtained after the full reaction calculation, a posteriori on the exclusive channels. This is avoided with our method,
- (ii) the exclusive spectra, which we will explain in Section 3.3.2.

Suppose one would only be interested in the total exclusive cross sections of Eq. (3.13), i.e. neither in the exclusive isomeric ratios, nor in the exclusive spectra. Only in that case, a simpler method would be sufficient. Since only the total reaction population that decays from nucleus to nucleus needs to be tracked, the total exclusive cross section for a certain channel is easily determined by subtracting the total ongoing flux from the total feeding flux to this channel. This is described in e.g. Section II.E.f of the GNASH manual[31]. We note that the exact treatment of TALYS does not require a large amount of computing time, certainly not when compared with more time-expensive parts of the full calculation.

When TALYS computes the binary reaction models and the multiple pre-equilibrium and Hauser-Feshbach models, it stores both  $P(Z, N, E_x)$  (through the **popexcl** array) and  $s_k(Z, N, E_x, E_{x'})$  (through the **feedexcl** array) for all residual nuclei and particles. This temporary storage enables us to first complete the full reaction calculation, including all its physical aspects, until all channels are closed. Then, we turn to the exclusive cross section and spectra problem afterwards in a separate subroutine: *channels.f*. It is thus considered as an isolated book-keeping problem.

The total number of different exclusive channels rapidly increases with the number of reaction stages. It can be shown that for  $m$  outgoing particles (i.e. reaction stages) which can be of  $k$  different types, the

maximum number of exclusive cross sections is  $\binom{m+k-1}{m}$ . In general, we include neutrons up to alpha-particles as competing particles, i.e.  $k = 6$ , giving  $\binom{m+5}{m}$  possible exclusive channels, or 6, 21, 56 and 126, respectively, for the first 4 stages. This clarifies why exclusive channels are usually only of interest for only a few outgoing particles (the ENDF format for evaluated data libraries includes reactions up to 4 particles). At higher energies, and thus more outgoing particles, exclusive cross sections lose their relevance and the cross sections per channel are usually accumulated in the total particle production cross sections and residual production cross sections. Certainly at higher energies, this apparent loss of information is no longer an issue, since the observable quantities to which nuclear models can be tested are of a cumulative nature anyway, when many particles are involved.

In TALYS, the cumulated particle production cross sections and residual production cross sections are always *completely* tracked down until all residual nuclides have decayed to an isomer or the ground state, regardless of the incident energy, whereas exclusive cross sections are only tracked up to a user-defined depth. To elucidate this important point we discuss the low and the high energy case. For low energies, say up to 20 MeV, keeping track of the exclusive cross section is important from both the fundamental and the applied point of view. It can be imagined that in a  $(n, np)$  measurement both the emitted neutron and proton have been measured in the detector. Hence the cross section is *not* the same as that of an activation measurement of the final residual nucleus, since the latter would also include a contribution from the  $(n, d)$  channel. Another example is the  $(n, 2n)$  channel, distinguished from the  $(n, n')$  or the general  $(n, xn)$  cross section, which is of importance in some integral reactor benchmarks. If, on the other hand, we encounter in the literature a cross section of the type  $^{120}\text{Sn}(p, 7p18n)^{96}\text{Ru}$ , we can be sure that the residual product  $^{96}\text{Ru}$  was measured and not the indicated number of neutrons and protons in a detector. The  $(p, 7p18n)$  symbol merely represents the number of neutron and proton units, while other light ions are generally included in the emission channel. Hence, for high energies the outcome of a nuclear reaction is usually tracked in parallel by two sets of quantities: the  $(proj, xn), \dots (proj, x\alpha)$  particle production cross sections and spectra, and the residual production cross sections. These will be exactly defined in the next sections.

### 3.2.3 Binary cross sections

Some of the exclusive channels need, and get, more attention than others. The exclusive binary cross sections, for reactions that are characterized by one, and only one, particle out, are special in the sense that they comprise both discrete and continuous energy transitions. Inelastic scattering can occur through both direct collective and compound transitions to the first few excited levels and through pre-equilibrium and compound reactions to the continuum. Let us assume that for a target nucleus the basic structure properties (spin, parity, deformation parameters) of the first  $N$  levels are known. Then, the *inelastic cross section*,  $\sigma_{n,n'}$  is the sum of a *total discrete inelastic cross section*  $\sigma_{n,n'}^{disc}$  and a *continuum inelastic cross section*  $\sigma_{n,n'}^{cont}$

$$\sigma_{n,n'} = \sigma_{n,n'}^{disc} + \sigma_{n,n'}^{cont}, \quad (3.14)$$

where  $\sigma_{n,n'}^{disc}$  is the sum over the inelastic cross sections for all the individual discrete states

$$\sigma_{n,n'}^{disc} = \sum_{i=1}^N \sigma_{n,n'}^i. \quad (3.15)$$

A further breakdown of each term is possible by means of reaction mechanisms. The inelastic cross section for each individual state  $i$  has a direct and a compound contribution:

$$\sigma_{n,n'}^i = \sigma_{n,n'}^{i,direct} + \sigma_{n,n'}^{i,comp}, \quad (3.16)$$

where the direct component comes from DWBA or coupled-channels calculations. Similarly, for the inelastic scattering to the continuum we can consider a pre-equilibrium and a compound contribution

$$\sigma_{n,n'}^{cont} = \sigma_{n,n'}^{PE} + \sigma_{n,n'}^{cont,comp}. \quad (3.17)$$

The set of definitions (3.14-3.17) can be given in a completely analogous way for the other binary channels  $\sigma_{n,p}$ , i.e.  $\sigma^{ex}(0, 1, 0, 0, 0, 0)$ ,  $\sigma_{n,d}$ ,  $\sigma_{n,t}$ ,  $\sigma_{n,h}$  and  $\sigma_{n,\alpha}$ . For the depletion of the reaction population that goes into the pre-equilibrium channels, which will be discussed in Section 4.4, it is helpful to define here the *total discrete direct cross section*,

$$\sigma^{disc,direct} = \sum_i \sum_{k=n',p,d,t,h,\alpha} \sigma_{n,k}^{i,direct}. \quad (3.18)$$

Finally, we also consider an alternative division for the non-elastic cross section. It is equal to the sum of the *inclusive* binary cross sections

$$\sigma_{non-el} = \sum_{k=\gamma,n',p,d,t,h,\alpha} \sigma_{n,k}^{inc,bin}, \quad (3.19)$$

where again at the present stage of the outline we do not consider fission and ejectiles heavier than  $\alpha$ -particles. This is what we actually use in the inclusive nuclear reaction calculations. With the direct, pre-equilibrium and compound models, several residual nuclides can be formed after the binary reaction, with a total population per nucleus that is equal to the terms of Eq. (3.19). The residual nuclides then decay further until all channels are closed. Note that  $\sigma^{inc,bin}$  is not a “true” cross section in the sense of a quantity for a final combination of a product and light particle(s).

### 3.2.4 Total particle production cross sections

Especially for incident energies higher than about 10 MeV, it is appropriate to define the composite or *total neutron production cross section*,  $\sigma_{n,xn}$ . It can be expressed in terms of the exclusive cross sections as follows

$$\sigma_{n,xn} = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} i_n \sigma^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha), \quad (3.20)$$

i.e. in the more common notation,

$$\sigma_{n,xn} = \sigma_{n,n'} + 2\sigma_{n,2n} + \sigma_{n,np} + 2\sigma_{n,2np} + \dots \quad (3.21)$$

Again,  $\sigma_{n,xn}$  is not a true cross section since the incident and outgoing channels are not exactly defined by its individual reaction components. (Contrary to our definition, in some publications  $\sigma_{n,xn}$  is used to indicate activation measurements of a whole string of isotopes (e.g.  $^{202-208}\text{Pb}$ ) in which case  $x$  is a

number that varies case by case. In our work, this is called an exclusive cross section). The *neutron multiplicity*, or *yield*,  $Y_n$  is defined as

$$Y_n = \frac{\sigma_{n,xn}}{\sigma_{non-el}}. \quad (3.22)$$

Similarly, the *total proton production cross section*,  $\sigma_{n,xp}$  is defined as

$$\sigma_{n,xp} = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} i_p \sigma^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha), \quad (3.23)$$

and the proton multiplicity, or yield,  $Y_p$  is defined as

$$Y_p = \frac{\sigma_{n,xp}}{\sigma_{non-el}}, \quad (3.24)$$

and similarly for the other particles. We note that we do not, in practice, use Eq. (3.20) to calculate the composite particle production cross section. Instead, we first calculate the inclusive binary cross section of Eq. (3.19) and then, during the depletion of each residual nucleus by further decay we directly add the reaction flux, equal to the  $s_k(Z, N, E_x, E_{x'})$  term of Eq. (3.8), to  $\sigma_{n,xn}$ ,  $\sigma_{n,xp}$ , etc. This procedure has already been sketched in the multiple decay scheme at the beginning of this Chapter. In the output of TALYS, we include Eq. (3.20) only as a numerical check. For a few outgoing particles Eq. (3.20) should exactly hold. For higher energies and thus more outgoing particles (typically more than 4, see the **maxchannel** keyword on page 124) the exclusive cross sections are no longer tracked by TALYS and Eq. (3.20) can no longer be expected to hold numerically. Remember, however, that we always calculate the total particle production cross sections, irrespective of the number of outgoing particles, since we continue the multiple emission calculation until all residual nuclides are in their isomeric or ground states.

### 3.2.5 Residual production cross sections

We can define another important type of derived cross section using the exclusive cross section, namely the residual production cross section  $\sigma_{prod}$ . All exclusive cross sections with the same number of neutron and proton units in the outgoing channel sum up to the same residual nucleus production cross section for the final nucleus  $(Z, N)$ , i.e.

$$\sigma_{prod}(Z, N) = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} \sigma^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha) \delta_N \delta_Z, \quad (3.25)$$

where the Kronecker delta's are defined by

$$\begin{aligned} \delta_N &= 1 \text{ if } i_n + i_d + 2i_t + i_h + 2i_\alpha = N_C - N \\ &= 0 \text{ otherwise} \\ \delta_Z &= 1 \text{ if } i_p + i_d + i_t + 2i_h + 2i_\alpha = Z_C - Z \\ &= 0 \text{ otherwise,} \end{aligned} \quad (3.26)$$

where the first compound nucleus that is formed from the projectile and target nucleus is denoted by  $(Z_C, N_C)$ . As an example, consider the  $n + {}^{56}\text{Fe} \rightarrow {}^{54}\text{Mn} + x$  reaction. The exclusive cross sections that

add up to the  $^{54}\text{Mn}$  production cross section are  $\sigma_{n,2np}$ ,  $\sigma_{n,nd}$ , and  $\sigma_{n,t}$ , or  $\sigma^{ex}(2, 1, 0, 0, 0, 0)$ ,  $\sigma^{ex}(1, 0, 1, 0, 0, 0)$ , and  $\sigma^{ex}(0, 0, 0, 1, 0, 0)$ , respectively.

Since all exclusive cross sections contribute to the residual production cross section for one nuclide ( $Z, N$ ) only, Eq. (3.6) automatically implies

$$\sigma_{non-el} = \sum_Z \sum_N \sigma_{prod}(Z, N). \quad (3.27)$$

Similar to Eq. (3.13), Eq. (3.25) is separated per isomer

$$\sigma_{prod,i}(Z, N) = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} \sigma_i^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha) \delta_N \delta_Z, \quad (3.28)$$

and the equivalent of Eq. (3.13) is

$$\sigma_{prod}(Z, N) = \sum_{i=0, isomers} \sigma_{prod,i}(Z, N). \quad (3.29)$$

Also here, we do not calculate  $\sigma_{prod}$  and  $\sigma_{prod,i}$  using Eqs. (3.25) and (3.28), although optionally TALYS includes it as a numerical check in the output for residual nuclides close to the target. Analogous to the total particle production, we determine the residual production cross section, for both the isomers and the ground state, after the complete decay of each nucleus by means of an inclusive calculation.

### 3.3 Spectra and angular distributions

In addition to cross sections, TALYS also predicts energy spectra, angular distributions and energy-angle distributions.

#### 3.3.1 Discrete angular distributions

The elastic angular distribution  $\frac{d\sigma^{el}}{d\Omega}$  has a direct and a compound component:

$$\frac{d\sigma^{el}}{d\Omega} = \frac{d\sigma^{shape-el}}{d\Omega} + \frac{d\sigma^{comp-el}}{d\Omega}, \quad (3.30)$$

where the shape-elastic part comes directly from the optical model while the compound part comes from compound nucleus theory, namely Eq. (4.140). An analogous relation holds for inelastic scattering to a single discrete state  $i$

$$\frac{d\sigma_{n,n'}^i}{d\Omega} = \frac{d\sigma_{n,n'}^{i,direct}}{d\Omega} + \frac{d\sigma_{n,n'}^{i,compound}}{d\Omega}, \quad (3.31)$$

where the direct component comes from DWBA or coupled-channels calculations. For charge exchange, we can write

$$\frac{d\sigma_{n,p}^i}{d\Omega} = \frac{d\sigma_{n,p}^{i,direct}}{d\Omega} + \frac{d\sigma_{n,p}^{i,compound}}{d\Omega} \quad (3.32)$$

and analogous expressions can be written for the other binary reactions ( $n, d$ ), etc.

Of course, the integration over solid angle of every angular distribution defined here must be equal to the corresponding cross section, e.g.

$$\sigma_{n,n'}^{i,direct} = \int d\Omega \frac{d\sigma_{n,n'}^{i,direct}}{d\Omega}. \quad (3.33)$$

In the output of TALYS, we use a representation in terms of outgoing angle and one in terms of Legendre coefficients, i.e. Eq. (3.30) can also be written as

$$\frac{d\sigma^{el}}{d\Omega} = \sum_L (C_L^{shape-el} + C_L^{comp-el}) P_L(\cos \Theta), \quad (3.34)$$

where  $P_L$  are Legendre polynomials. For inelastic scattering we have

$$\frac{d\sigma_{n,n'}^i}{d\Omega} = \sum_L (C_L^{i,direct} + C_L^{i,comp}) P_L(\cos \Theta), \quad (3.35)$$

and similarly for the other binary channels. The Legendre expansion is required for the storage of the results in ENDF data libraries.

### 3.3.2 Exclusive spectra

An exclusive spectrum is not only specified by the exact number of emitted particles, but also by their outgoing energies.

In TALYS, exclusive spectra are calculated in the same loops that take care of the exclusive cross sections. The inclusive continuum spectra are obtained by taking the derivative of the inclusive cross sections per excitation energy of Eq. (3.10) with respect to the outgoing particle energy  $E_{k'}$ ,

$$E_{k'} = E_x - E_{x'}(i') - S_{k'}, \quad (3.36)$$

where  $S_{k'}$  is the separation energy for outgoing particle  $k'$ . Note that since the inclusive cross section per excitation energy  $S$  depends on  $E_{k'}$  via  $s_k$ , the product rule of differentiation applies to Eq. (3.10). Therefore, the inclusive spectrum per excitation energy for an outgoing particle  $k'$  of a given  $(i_n, i_p, i_d, i_t, i_h, i_\alpha)$  channel is

$$\begin{aligned} \frac{dS}{dE_{k'}}(i_n, i_p, i_d, i_t, i_h, i_\alpha, E_{x'}(i')) &= \sum_{k=\gamma,n,p,d,t,h,\alpha} \sum_i \\ &\left[ \frac{s_k(Z, N, E_x(i), E_{x'}(i'))}{P(Z, N, E_x(i))} \frac{dS}{dE_{k'}}(i_n - \delta_{nk}, i_p - \delta_{pk}, i_d - \delta_{dk}, i_t - \delta_{tk}, i_h - \delta_{hk}, i_\alpha - \delta_{\alpha k}, E_x(i)) \right. \\ &\left. + \delta_{kk'} \frac{ds_k(Z, N, E_x(i), E_{x'}(i'))}{dE_{k'}} \frac{S(i_n - \delta_{nk}, i_p - \delta_{pk}, i_d - \delta_{dk}, i_t - \delta_{tk}, i_h - \delta_{hk}, i_\alpha - \delta_{\alpha k}, E_x(i))}{P(Z, N, E_x(i))} \right], \end{aligned} \quad (3.37)$$

where, as initial condition, the derivatives of  $s_k(Z_C, N_C, E_x^{max}, E_{x'}(i'))$  are the binary emission spectra. The first term on the right-hand side corresponds to the spectrum of the feeding channel and the second term denotes the contribution of the last emitted particle. The calculation of Eq. (3.37) can be done

simultaneously with the exclusive cross section calculation, i.e. we follow exactly the same recursive procedure. The final exclusive spectrum for outgoing particle  $k'$  is given by

$$\frac{d\sigma^{ex}}{dE_{k'}}(i_n, i_p, i_d, i_t, i_h, i_\alpha) = \sum_{i=0, \text{isomers}} \frac{dS}{dE_{k'}}(i_n, i_p, i_d, i_t, i_h, i_\alpha, E_i), \quad (3.38)$$

The terms on the right hand side are the exclusive spectra per ground state or isomer. The latter naturally result from our method, even though only the total exclusive spectra of the left hand side are of interest.

We stress that for a given  $(i_n, i_p, i_d, i_t, i_h, i_\alpha)$  channel, Eq. (3.37) is calculated for *every* outgoing particle  $k'$  (i.e. n, p, d, t, h and  $\alpha$ ). Hence, e.g. the  $(n, 2np\alpha)$  channel is characterized by only one exclusive cross section,  $\sigma_{n,2np\alpha}$ , but by three spectra, one for outgoing neutrons, protons and alpha's, respectively, whereby all three spectra are constructed from components from the first up to the fourth particle emission (i.e. the  $\alpha$  can have been emitted in each of the four stages). In practice, this means that all spectra have a first order pre-equilibrium component (and for higher energies also higher order pre-equilibrium components), and a compound component from multiple emission. Upon integration over outgoing energy, the exclusive cross sections may be obtained,

$$\sigma^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha) = \frac{1}{i_n + i_p + i_d + i_t + i_h + i_\alpha} \sum_{k'=n,p,d,t,h,\alpha} \int dE_{k'} \frac{d\sigma^{ex}}{dE_{k'}}(i_n, i_p, i_d, i_t, i_h, i_\alpha). \quad (3.39)$$

### 3.3.3 Binary spectra

Similar to the cross sections, the exclusive spectra determine various other specific spectra of interest. The exclusive *inelastic spectrum* is a special case of Eq. (3.38)

$$\frac{d\sigma_{n,n'}}{dE_{n'}} = \frac{d\sigma^{ex}}{dE_{n'}}(1, 0, 0, 0, 0, 0). \quad (3.40)$$

Since Eq. (3.37) represents an energy spectrum, it includes by definition only continuum transitions, i.e. it does not include the binary reactions to discrete states. Hence, upon integration, Eq. (3.40) only gives the continuum inelastic cross section of Eq. (3.14):

$$\sigma_{n,n'}^{cont} = \int dE_{n'} \frac{d\sigma_{n,n'}}{dE_{n'}}. \quad (3.41)$$

Similar relations hold for the binary  $(n, p)$ ,  $(n, d)$ ,  $(n, t)$ ,  $(n, h)$  and  $(n, \alpha)$  spectra. The contributions to the binary spectra generally come from pre-equilibrium and continuum compound spectra.

### 3.3.4 Total particle production spectra

Similar to the total particle production cross sections, the *composite* or *total neutron spectrum* can be expressed in terms of exclusive spectra as follows

$$\frac{d\sigma_{n,xn}}{dE_{n'}} = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} \frac{d\sigma^{ex}}{dE_{n'}}(i_n, i_p, i_d, i_t, i_h, i_\alpha), \quad (3.42)$$

i.e. in the other notation,

$$\frac{d\sigma_{n,xn}}{dE_{n'}} = \frac{d\sigma_{n,n'}}{dE_{n'}} + \frac{d\sigma_{n,2n}}{dE_{n'}} + \frac{d\sigma_{n,np}}{dE_{n'}} + \frac{d\sigma_{n,2np}}{dE_{n'}} + \dots \quad (3.43)$$

Similar relations hold for the  $(n, xp)$ , etc. spectra. Note that, in contrast with Eq. (3.20), the multiplicity is already implicit in the exclusive spectra.

Again, in practice we do not use Eq. (3.42) to calculate the composite spectra but instead add the  $ds_k(Z, N, E_x, E_{x'})/dE_{k'}$  term that appears in Eq. (3.37) to the composite spectra while depleting all nuclides in an inclusive calculation. We do use Eq. (3.42) as a numerical check in the case of a few outgoing particles. Finally, integration of the total neutron spectrum and addition of the binary discrete cross section gives the total particle production cross section

$$\sigma_{n,xn} = \int dE_{n'} \frac{d\sigma_{n,xn}}{dE_{n'}} + \sigma_{n,n'}^{disc}, \quad (3.44)$$

and similarly for the other particles.

### 3.3.5 Double-differential cross sections

The generalization of the exclusive spectra to angular dependent cross sections is done by means of the exclusive double-differential cross sections

$$\frac{d^2\sigma^{ex}}{dE_{k'}d\Omega}(i_n, i_p, i_d, i_t, i_h, i_\alpha), \quad (3.45)$$

which are obtained by either physical models or systematics. Integration over angles yields the exclusive spectrum

$$\frac{d\sigma^{ex}}{dE_{k'}}(i_n, i_p, i_d, i_t, i_h, i_\alpha) = \int d\Omega \frac{d^2\sigma^{ex}}{dE_{k'}d\Omega}(i_n, i_p, i_d, i_t, i_h, i_\alpha). \quad (3.46)$$

The other relations are analogous to those of the spectra, e.g. the inelastic double-differential cross section for the continuum is

$$\frac{d^2\sigma_{n,n'}}{dE_{n'}d\Omega} = \frac{d^2\sigma^{ex}}{dE_{n'}d\Omega}(1, 0, 0, 0, 0, 0), \quad (3.47)$$

and the total neutron double-differential cross section can be expressed as

$$\frac{d^2\sigma_{n,xn}}{dE_{n'}d\Omega} = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} \frac{d^2\sigma^{ex}}{dE_{n'}d\Omega}(i_n, i_p, i_d, i_t, i_h, i_\alpha). \quad (3.48)$$

For the *exclusive* calculation, the angular information is only tracked for the first particle emission. The reason is that for incident energies up to about 20 to 30 MeV, only the first emitted particle deviates from an isotropic angular distribution. Multiple compound emission to the continuum is essentially isotropic. The isotropic contribution to the exclusive double-differential spectrum is then simply determined by the part of the corresponding cross section that comes from Hauser-Feshbach decay. At higher incident energies, where the approximation of only one forward-peaked particle becomes incorrect, the interest in exclusive spectra, or for that matter, the computational check of Eq. (3.48), is no longer there. The presence of multiple pre-equilibrium emission at energies above several tens of MeV requires that we include angular information for every emitted particle in the *total* double-differential cross section, i.e. the left-hand side of Eq. (3.48). Again, this is all tracked correctly in the full inclusive calculation.

### 3.4 Fission cross sections

For clarity, we have kept the fission channel out of the discussion so far. The generalization to a picture in which fission is possible is however not too difficult. For fissile nuclides, the first expression that needs generalization is that of the non-elastic cross section expressed as a sum of exclusive cross sections, Eq. (3.6). It should read

$$\sigma_{non-el} = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} \sigma^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha) + \sigma_f, \quad (3.49)$$

where the *total fission* cross section  $\sigma_f$  is the sum over exclusive fission cross sections

$$\sigma_f = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} \sigma_f^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha), \quad (3.50)$$

where  $\sigma_f^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha)$  represents the cross section for fissioning *after* the emission of  $i_n$  neutrons,  $i_p$  protons, etc. Well-known special cases are  $\sigma_{n,f} = \sigma_f^{ex}(0, 0, 0, 0, 0, 0)$ ,  $\sigma_{n,nf} = \sigma_f^{ex}(1, 0, 0, 0, 0, 0)$  and  $\sigma_{n,2nf} = \sigma_f^{ex}(2, 0, 0, 0, 0, 0)$ , which are also known as first-chance, second-chance and third-chance fission cross section, respectively. Eq. (3.50) is more general in the sense that it also includes cases where particles other than neutrons can be emitted before the residual nucleus fissions, e.g.  $(n, npf)$ , which may occur at higher incident energies.

The generalization of the non-elastic cross section of Eq. (3.19) is

$$\sigma_{non-el} = \sum_{k=\gamma, n', p, d, t, h, \alpha} \sigma_{n,k}^{inc, bin} + \sigma_f^{bin}, \quad (3.51)$$

where  $\sigma_f^{bin}$  represents fission from the initial compound state (i.e. excluding  $(n, \gamma f)$  processes).

Analogous to Eq. (3.25), we can define a cross section for each fissioning residual product

$$\sigma_{prod}^{fis}(Z, N) = \sum_{i_n=0}^{\infty} \sum_{i_p=0}^{\infty} \sum_{i_d=0}^{\infty} \sum_{i_t=0}^{\infty} \sum_{i_h=0}^{\infty} \sum_{i_\alpha=0}^{\infty} \sigma_f^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha) \delta_N \delta_Z. \quad (3.52)$$

At higher energies, the meaning of  $\sigma_{prod}^{fis}(Z, N)$  is more relevant than the exclusive fission cross sections. Consequently, for the total fission cross section we have

$$\sigma_f = \sum_Z \sum_N \sigma_{prod}^{fis}(Z, N). \quad (3.53)$$

What remains to be explained is how  $\sigma_f^{ex}$  is computed. First, we need to add to Eq. (3.8) a term we denote by  $s_f(Z, N, E_x(i))$ , which is the part of the population that fissions from the  $(Z, N, E_x(i))$  bin. Hence, for fissile nuclides we have

$$P(Z, N, E_x(i)) = s_f(Z, N, E_x(i)) + \sum_{k=\gamma, n, p, d, t, h, \alpha} \sum_i s_k(Z, N, E_x(i), E_{x'}(i')). \quad (3.54)$$

where in this case the sum over  $i$  runs over discrete levels and continuum bins from 0 to  $E_x(i) - S_k$ . The exclusive fission cross section  $\sigma_f^{ex}$  is

$$\sigma_f^{ex}(i_n, i_p, i_d, i_t, i_h, i_\alpha) = \sum_i \frac{s_f(Z, N, E_x(i))}{P(Z, N, E_x(i))} S(i_n, i_p, i_d, i_t, i_h, i_\alpha, E_x(i)). \quad (3.55)$$

where  $i$  runs from 0 to  $E_x^{max}(Z, N)$ . The rest of the calculation of the exclusive particle cross section proceeds exactly as before. Eq. (3.10) is now automatically depleted from the fission cross section (3.55), in the sense that the  $s_k$  terms alone, summed over  $\gamma$  and particles only, no longer add up to the population  $P$ .

Finally, the exclusive fission cross sections are also accompanied by spectra. For example, the first two neutrons emitted in the  $(n, 2nf)$  channel (third-chance fission) are described by an outgoing neutron spectrum. The exclusive spectrum of outgoing particle  $k'$  in a fission channel is

$$\frac{d\sigma_f^{ex}}{dE_{k'}}(i_n, i_p, i_d, i_t, i_h, i_\alpha) = \sum_i \frac{s_f(Z, N, E_x(i))}{P(Z, N, E_x(i))} \frac{dS}{dE_{k'}}(i_n, i_p, i_d, i_t, i_h, i_\alpha), \quad (3.56)$$

while the exclusive particle spectra are again described by Eq. (3.37). For double-differential spectra, the usual generalization holds. We also repeat here that the total (observable) fission cross section is always calculated by letting reaction population go into the fission channel from each  $(Z, N, E_x, J, \Pi)$  channel until all nuclides have ended up in their ground or isomeric state, irrespective of the user request for an exclusive channel calculation.

## 3.5 Recoils

### 3.5.1 Qualitative analysis

In a nuclear reaction code, the calculations are usually performed in the center of mass (CM) frame, while the experimental data are obtained in the Laboratory (LAB) frame. It is therefore necessary to perform a transformation either by (i) expressing the experimental data in the CM frame or by (ii) expressing the CM model results in the LAB frame. Of course, the cross sections are the same in both frames, but the spectra are certainly different. The best example is given by the elastic peak in an emission spectrum which is a Dirac delta peak in the CM frame and rather looks like a Gaussian when measured experimentally. The reason for this, apart from the fact that the projectile beam is not perfectly mono-energetic, is that the composite system has a velocity in the LAB frame before decay occurs. Consequently if one considers the emission of an ejectile with a well defined energy in the CM frame, the ejectile energy in the LAB frame will not be unique because of all the CM emission angles. More precisely, a maximum ejectile energy will be obtained when the emission occurs at  $0^\circ$ , and a minimum will be obtained at  $180^\circ$ , together with all the intermediate situations. Dealing with this situation is simple if only one nucleus decays, but if two particles are sequentially emitted, the first emission probabilities create a velocity distribution of the residual nuclei in the LAB frame. One must first loop over these velocities before one can compute the secondary emission.

### 3.5.2 General method

As mentioned in section 3.2.2, in TALYS each nucleus that can decay is described by an array  $P(Z, N, E_x)$  which gives the population in a bin/level with excitation energy  $E_x$  of the nucleus  $(Z, N)$ . A special case is the initial compound nucleus which contains all the initial reaction population at its total excitation energy  $E_x^{max}$ . For the kinematics of the binary reactions, it is necessary to keep track of the velocities and moving directions of these nuclei in the LAB frame, so that we can reconstruct the LAB spectra from the

decays in the CM frame. We therefore have to add in principle three dimensions to the  $P$  array. The first one to keep track of the recoil energy, and the two other ones for the emission angles. However, such book-keeping would become very time consuming, especially for high energies.

Hence, we only take into account the recoil energies and the usual  $\Theta$  angle and define another array  $P_{rec}(Z, N, E_x, E_r, \Theta_r)$  which indicates the fraction of the total population  $P(Z, N, E_x)$  moving with the kinetic energy  $E_r$  in the direction  $\Theta_r$  with respect to the beam direction in the LAB frame. Obviously,

$$P(Z, N, E_x) = \sum_{E_r \text{ bins}} \sum_{\Theta_r \text{ bins}} P_{rec}(Z, N, E_x, E_r, \Theta_r). \quad (3.57)$$

Again, the initial compound nucleus ( $Z_C, N_C$ ) is a special one. Its kinetic energy  $E_r^0$  in the LAB frame is unique and is given by

$$E_r^0 = \sqrt{(E_p^2 + 2M_p E_p + M_C^2)} - M_C, \quad (3.58)$$

where  $E_p$  is the projectile kinetic energy in the LAB,  $M_p$  the projectile mass and  $M_C$  the compound nucleus mass, and it moves in the beam direction (i.e.  $0^\circ$ ). Before any emission is calculated, the initial reaction population is stored in the array element  $P_{rec}(Z_c, N_c, E_x^{max}, E_r^0, 0)$ . As explained before, the population of the residual nuclei bins are calculated by looping over all possible ejectiles, emission energies and angles in the CM frame. Therefore, each time we decay from a mother bin to a residual bin, we know exactly what fraction of the total bin population is emitted in a given CM (energy,angle) bin. We then simply couple the CM emission energies and angles with the CM kinetic energy and moving direction in the LAB frame to determine simultaneously the ejectile double-differential spectrum in the LAB and the residual nucleus population in the corresponding LAB (energy,angle) bin. This may seem simple from a qualitative point of view, it is however not trivial to implement numerically and can be time consuming.

### 3.5.3 Quantitative analysis

From now on, for simplicity, we assume that the kinematics of the binary reactions can be considered as a classical process, i.e. we exclude  $\gamma$  decay and relativistic kinematics in the recoil calculation. We here consider the emission of a given ejectile from a given energy bin  $i$  of the decaying nucleus ( $Z, N$ ) which moves with a given velocity  $v_{cm}$  (or kinetic energy  $E_{cm}$ ) in the direction  $\Theta_{cm}$  with respect to the beam direction. The total population that is going to decay is  $P(Z, N, E_i)$  and the fraction of this population moving with the velocity  $v_{cm}$  in the direction  $\Theta_{cm}$  is given by  $P_{rec}(Z, N, E_i, E_{cm}, \Theta_{cm})$ . We can determine the total emitted flux for a given emission energy and a given emission angle in the CM frame. In practice, we rather decay from a initial bin to a residual bin in a given angular bin in the CM frame. If recoil effects are neglected we directly derive from such a decay an energy bin  $[E_{low}^{CM}, E_{up}^{CM}]$  and an angular bin  $[\Theta_{low}^{CM}, \Theta_{up}^{CM}]$  in which the total flux  $\Phi_{ej}^{CM}$  is emitted. Accounting for recoil effects requires an intermediate step to share the available energy  $\Delta E$  (difference between the energy bins of the initial nucleus and final nucleus) among the ejectile with mass  $m_{ej}$  and the residual nucleus with mass  $M_R$ .

To do this, we use the classical relation

$$\vec{v}_{ej}^{LAB} = \vec{v}_{cm} + \vec{v}_{ej}^{CM}, \quad (3.59)$$

which connects the LAB velocity  $\vec{v}_{ej}^{LAB}$  of the ejectile with its velocity  $\vec{v}_{ej}^{CM}$  in the CM frame and the CM frame velocity  $\vec{v}_{cm}$ . We need to connect  $\vec{v}_{ej}^{CM}$  with  $\Delta E$ .

This can be done upon writing

$$\Delta E = \frac{1}{2}m_{ej}(\vec{v}_{ej}^{CM})^2 + \frac{1}{2}M_R(\vec{v}_R^{CM})^2, \quad (3.60)$$

where  $\vec{v}_R^{CM}$  is the residual nucleus velocity in the CM frame, and using the relation

$$m_{ej}\vec{v}_{ej}^{CM} + m_R\vec{v}_R^{CM} = \vec{0}. \quad (3.61)$$

Combining (3.60) and (3.61) yields

$$v_{ej}^{CM} = \sqrt{2\frac{M_R}{m_{ej}(m_{ej} + M_R)}\Delta E}, \quad (3.62)$$

which reduces to the classical relation

$$v_{ej}^{CM} = \sqrt{\frac{2\Delta E}{m_{ej}}}, \quad (3.63)$$

if recoil effects are neglected (i.e. in the limit  $M_R \rightarrow +\infty$ ).

Once this connection is established, Eq. (3.59) is used to determine the velocity and angle of both the emitted light particle and the residual nucleus by simple projections on the LAB axis.

Hence, given a decay situation in the CM frame, we can reconstruct both the energy and angle of emission in the LAB frame. We now have to determine the link between the double-differential decay characteristics in both frames. The solution is well known (see Ref. [37] for instance) and consists of using a Jacobian which accounts for the modification of an elementary solid angle  $d\Omega$  in the CM frame when going into the LAB frame. However, in TALYS we have to employ another method because we do not generally calculate decays for well defined energies and angles but rather for a given energy bin and angular bin. Moreover, since we do not account for the azimuthal angle, we may also encounter some problems when calculating recoil for secondary emission. Indeed, only the first binary process has the azimuthal symmetry with respect to the beam direction.

### 3.5.4 The recoil treatment in TALYS

The way the double-differential spectra are calculated by TALYS in the LAB frame from those obtained in the CM frame is illustrated in Fig. 3.6. As stressed in Chapter 3, the emission energy grid for the outgoing particles is non-equidistant. Moreover, one has to keep in mind that the total flux  $\Phi(i, j)$  in an energy-angular bin  $(i, j)$  is connected with the double differential cross section  $xs(i, j)$  by

$$\Phi(i, j) = xs(i, j)\Delta E(i)\Delta\cos\Theta(j). \quad (3.64)$$

Consequently, it is appropriate to locate the grid points using an energy-cosine grid. As an example, in Fig. 3.6, we consider the decay in the CM bin defined by the energy interval [2, 3] and the cosine interval [0.25, 0.5] (black region). We assume that the decay occurs from a composite system moving with a kinetic energy of 1 MeV in the direction  $45^\circ$  with respect to the initial beam direction. The mass of the

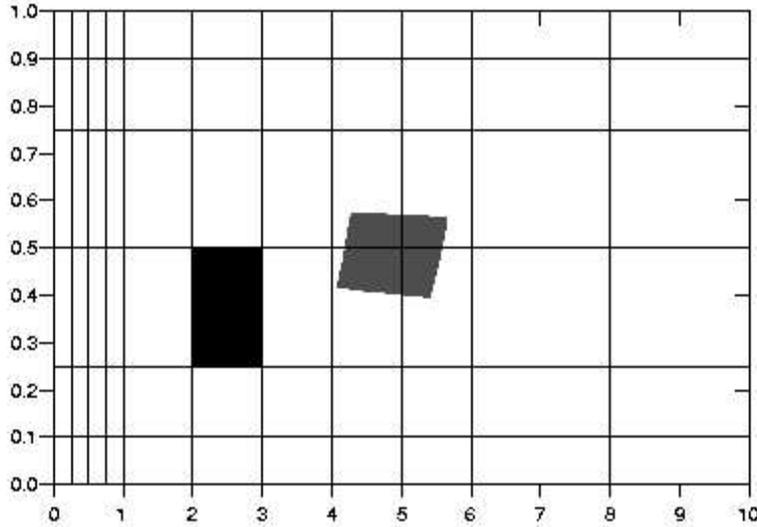


Figure 3.6: CM and LAB double-differential spectra in TALYS.

ejectile is assumed to be  $m_e = 1$  arb.unit, and that of the composite system 20 arb.unit. In that case, the region reached by the ejectile is a slightly deformed trapezoid (gray region) which covers several bins. Therefore, if the emitted flux is located in a single bin in the CM, it must be distributed over several bins when going to the LAB frame. This is the key problem to be solved in TALYS. To solve this problem, we need to make assumptions to be able (i) to calculate the area covered in the LAB frame (gray region) and (ii) the way this global area is distributed over the bins it partially covers. The assumption made in TALYS consists of neglecting the deformation of the boundaries of the grey area and assuming this area to be a trapezoid. In other words, we make the assumption that a triangle in the CM frame is transformed into a triangle when going in the LAB. This is helpful since the area of a triangle is given by a simple analytic expression as function of the coordinates of the summits of the triangle. Therefore, we divide the starting CM bins into two triangles to determine the two triangles obtained in the LAB frame. With such a method, the whole problem can be solved and the decay calculated in the CM frame can be transformed to the LAB frame without any further approximations.

However, in practice, coupling the angular direction (in the LAB) of the nucleus that decays with the ejectile emission angle in the CM frame, while neglecting the azimuthal angle, gives double differential ejectile spectra in the LAB which are generally not correct. In fact, we believe that it is better not to account for the angular distribution of the decaying nucleus unless both  $\Theta$  and  $\phi$  are explicitly treated. Fortunately, the final angular distribution of the recoiling nucleus is seldom of interest.

### 3.5.5 Method of average velocity

As mentioned above, we do not loop over the angular distribution of the decaying nucleus. This is equivalent to replacing the array  $P_{rec}(Z, N, E_i, E_r, \Theta_r)$  by  $P_{rec}(Z, N, E_i, E_r)$ . Then, we only have to keep track of the velocities of the nucleus that is going to decay, i.e. we have to loop over the  $E_r$  bins to reconstruct both the ejectile and residual nuclei spectra. Another approximation that we have implemented as an option (**recoilaverage y**) consists of using an average velocity before this reconstruction, a method first applied by Chadwick et al. [38, 39]. This approach avoids the loop over the  $E_r$  bins altogether and reduces the calculation time. However, for high energies, this might be too crude an approximation.

### 3.5.6 Approximative recoil correction for binary ejectile spectra

Maybe you are not interested in a full recoil calculation, but merely want to correct the outgoing particle spectra for the recoil of the nucleus. In that case you may use the following method which is implemented in TALYS for just that purpose and which is outlined below.

The assumptions are made that (i) only binary emission takes place, and that (ii) emission only occurs under  $0^\circ$ . Hence, this approximation is basically expected to be valid for angle-integrated spectra only. The CM to LAB conversion of the ejectile spectra takes under these conditions the following simple form:

$$E_{ej}^{lab} = \frac{M_R}{M_C} \Delta E + \frac{m_{ej} M_p}{M_C^2} E_p + 2 \sqrt{\frac{m_{ej} M_R M_p}{M_C^3} E_p \Delta E}, \quad (3.65)$$

in which  $E_{ej}^{lab}$  is the LAB ejectile energy. This correction is applied to the *full* ejectile spectrum including the multiple emission contributions. Hence, the approximation is rather crude. It saves, however, a lot of computer time. Since the high-energy tail originates completely from binary emission, this tail is correctly converted to the LAB system. Furthermore, the correction is small at low energies where the largest contributions from multiple emission reside.

## Chapter 4

# Nuclear models

Fig. 4.1 gives an overview of the nuclear models that are included in TALYS. They can generally be categorized into optical, direct, pre-equilibrium, compound and fission models, all driven by a comprehensive database of nuclear structure and model parameters. We will first describe the optical model and the various models for direct reactions that are used. Next, we give an outline of the various pre-equilibrium models that are included. Then, we describe compound nucleus models for both binary and multiple emission, and level densities, which are important ingredients of pre-equilibrium and compound models. Finally, we give an outline of the fission models.

### 4.1 Optical model

The central assumption underlying the optical model is that the complicated interaction between an incident particle and a nucleus can be represented by a complex mean-field potential, which divides the reaction flux into a part covering shape elastic scattering and a part describing all competing non-elastic channels. Solving the Schrödinger equation numerically with this complex potential yields a wealth of valuable information. First, it returns a prediction for the basic observables, namely the elastic angular distribution and polarisation, the reaction and total cross section and, for low energies, the  $s$ ,  $p$ -wave strength functions and the potential scattering radius  $R'$ . The essential value of a good optical model is that it can reliably predict these quantities for energies and nuclides for which no measurements exist. Also, the quality of the not directly observable quantities that are provided by the optical model has an equally important impact on the evaluation of the various reaction channels. Well-known examples are transmission coefficients, for compound nucleus and multi-step compound decay, and the distorted wave functions that are used for direct inelastic reactions and for transitions to the continuum that describe statistical multi-step direct reactions. Also, the reaction cross sections that are calculated with the optical model are crucial for the semi-classical pre-equilibrium models.

All optical model calculations are performed by ECIS-97 [35], which is used as a subroutine in TALYS.

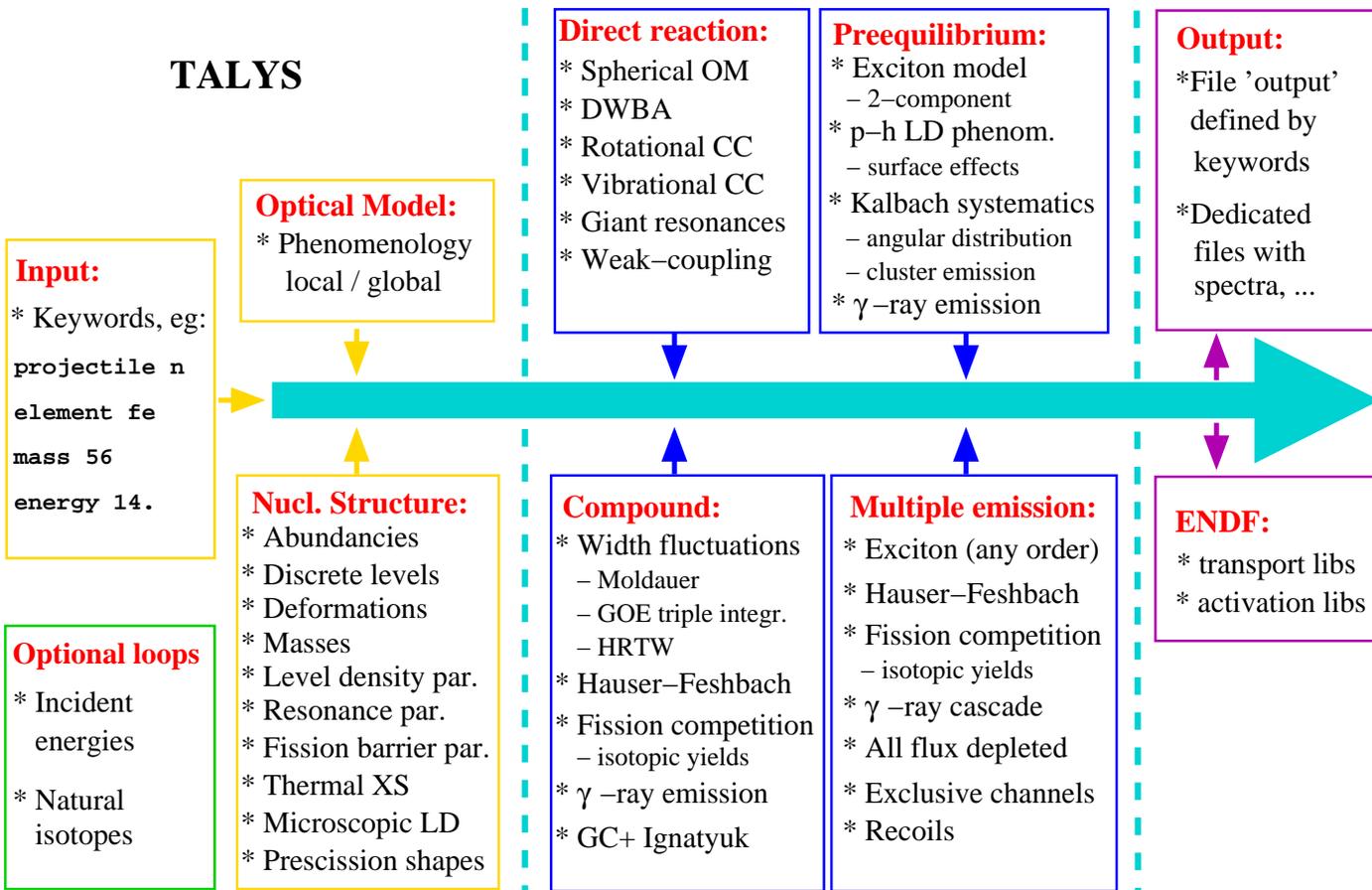


Figure 4.1: Nuclear models in TALYS

### 4.1.1 Spherical OMP: Neutrons and protons

The default optical model potentials (OMP) used in TALYS are the local and global parameterisations of Koning and Delaroche [40].

The phenomenological OMP for nucleon-nucleus scattering,  $\mathcal{U}$ , is defined as:

$$\begin{aligned} \mathcal{U}(r, E) = & -\mathcal{V}_V(r, E) - i\mathcal{W}_V(r, E) - i\mathcal{W}_D(r, E) \\ & + \mathcal{V}_{SO}(r, E) \cdot \mathbf{1} \cdot \boldsymbol{\sigma} + i\mathcal{W}_{SO}(r, E) \cdot \mathbf{1} \cdot \boldsymbol{\sigma} + \mathcal{V}_C(r), \end{aligned} \quad (4.1)$$

where  $\mathcal{V}_{V,SO}$  and  $\mathcal{W}_{V,D,SO}$  are the real and imaginary components of the volume-central ( $V$ ), surface-central ( $D$ ) and spin-orbit ( $SO$ ) potentials, respectively.  $E$  is the LAB energy of the incident particle in MeV. All components are separated in energy-dependent well depths,  $V_V$ ,  $W_V$ ,  $W_D$ ,  $V_{SO}$ , and  $W_{SO}$ , and energy-independent radial parts  $f$ , namely

$$\begin{aligned} \mathcal{V}_V(r, E) &= V_V(E) f(r, R_V, a_V), \\ \mathcal{W}_V(r, E) &= W_V(E) f(r, R_V, a_V), \\ \mathcal{W}_D(r, E) &= -4a_D W_D(E) \frac{d}{dr} f(r, R_D, a_D), \\ \mathcal{V}_{SO}(r, E) &= V_{SO}(E) \left( \frac{\hbar}{m_\pi c} \right)^2 \frac{1}{r} \frac{d}{dr} f(r, R_{SO}, a_{SO}), \\ \mathcal{W}_{SO}(r, E) &= W_{SO}(E) \left( \frac{\hbar}{m_\pi c} \right)^2 \frac{1}{r} \frac{d}{dr} f(r, R_{SO}, a_{SO}). \end{aligned} \quad (4.2)$$

The form factor  $f(r, R_i, a_i)$  is a Woods-Saxon shape

$$f(r, R_i, a_i) = (1 + \exp[(r - R_i)/a_i])^{-1}, \quad (4.3)$$

where the geometry parameters are the radius  $R_i = r_i A^{1/3}$ , with  $A$  being the atomic mass number, and the diffuseness parameters  $a_i$ . For charged projectiles, the Coulomb term  $\mathcal{V}_C$ , as usual, is given by that of a uniformly charged sphere

$$\begin{aligned} \mathcal{V}_C(r) &= \frac{Zze^2}{2R_C} \left( 3 - \frac{r^2}{R_C^2} \right), \quad \text{for } r \leq R_C \\ &= \frac{Zze^2}{r}, \quad \text{for } r \geq R_C, \end{aligned} \quad (4.4)$$

with  $Z(z)$  the charge of the target (projectile), and  $R_C = r_C A^{1/3}$  the Coulomb radius.

The functional forms for the potential depths depend on  $(E - E_f)$ , where  $E_f$ , the Fermi energy in MeV, is defined as the energy halfway between the last occupied and the first unoccupied shell of the nucleus. For incident neutrons,

$$E_f^n = -\frac{1}{2}[S_n(Z, N) + S_n(Z, N + 1)], \quad (4.5)$$

with  $S_n$  the neutron separation energy for a nucleus with proton number  $Z$  and neutron number  $N$ , while for incident protons

$$E_f^p = -\frac{1}{2}[S_p(Z, N) + S_p(Z + 1, N)], \quad (4.6)$$

with  $S_p$  the proton separation energy. We use the mass table of the nuclear structure database to obtain the values of the separation energies.

Our OMP parameterisation for either incident neutrons or protons is

$$\begin{aligned}
V_V(E) &= v_1[1 - v_2(E - E_f) + v_3(E - E_f)^2 - v_4(E - E_f)^3] \\
W_V(E) &= w_1 \frac{(E - E_f)^2}{(E - E_f)^2 + (w_2)^2} \\
r_V &= \text{constant} \\
a_V &= \text{constant} \\
W_D(E) &= d_1 \frac{(E - E_f)^2}{(E - E_f)^2 + (d_3)^2} \exp[-d_2(E - E_f)] \\
r_D &= \text{constant} \\
a_D &= \text{constant} \\
V_{SO}(E) &= v_{so1} \exp[-v_{so2}(E - E_f)] \\
W_{SO}(E) &= w_{so1} \frac{(E - E_f)^2}{(E - E_f)^2 + (w_{so2})^2} \\
r_{SO} &= \text{constant} \\
a_{SO} &= \text{constant} \\
r_C &= \text{constant},
\end{aligned} \tag{4.7}$$

where  $E_f = E_f^n$  for incident neutrons and  $E_f = E_f^p$  for incident protons. Here  $E$  is the incident energy in the LAB system. This representation is valid for incident energies from 1 keV up to 200 MeV. Note that  $V_V$  and  $W_V$  share the same geometry parameters  $r_V$  and  $a_V$ , and likewise for the spin-orbit terms.

In general, all parameters appearing in Eq. (4.7) differ from nucleus to nucleus. When enough experimental scattering data of a certain nucleus is available, a so called local OMP can be constructed. TALYS retrieves all the parameters  $v_1, v_2$ , etc. of these local OMPs automatically from the nuclear structure and model parameter database, see the next Chapter, which contains the same information as the various tables of Ref. [40]. If a local OMP parameterisation is not available in the database, the built-in global optical models are automatically used, which can be applied for any  $Z, A$  combination. A flag exists (the **localomp** keyword) to overrule the local OMP by the global OMP. The global neutron OMP, validated for  $0.001 \leq E \leq 200$  MeV and  $24 \leq A \leq 209$ , is given by

$$\begin{aligned}
V_V(E) &= v_1^n [1 - v_2^n (E - E_f^n) + v_3^n (E - E_f^n)^2 - v_4^n (E - E_f^n)^3] \\
W_V(E) &= w_1^n \frac{(E - E_f^n)^2}{(E - E_f^n)^2 + (w_2^n)^2} \\
r_V &= 1.3039 - 0.4054A^{-1/3} \\
a_V &= 0.6778 - 1.487 \cdot 10^{-4} A \\
W_D(E) &= d_1^n \frac{(E - E_f^n)^2}{(E - E_f^n)^2 + (d_3^n)^2} \exp[-d_2^n (E - E_f^n)] \\
r_D &= 1.3424 - 0.01585A^{1/3} \\
a_D &= 0.5446 - 1.656 \cdot 10^{-4} A
\end{aligned}$$

$$\begin{aligned}
V_{SO}(E) &= v_{so1}^n \exp[-v_{so2}^n (E - E_f^n)] \\
W_{SO}(E) &= w_{so1}^n \frac{(E - E_f^n)^2}{(E - E_f^n)^2 + (w_{so2}^n)^2} \\
r_{SO} &= 1.1854 - 0.647A^{-1/3} \\
a_{SO} &= 0.59,
\end{aligned} \tag{4.8}$$

where the units are in fm and MeV and the parameters for the potential depths and  $E_f^n$  are given in Table 4.1.

The global proton OMP is given by

$$\begin{aligned}
V_V(E) &= v_1^p [1 - v_2^p (E - E_f^p) + v_3^p (E - E_f^p)^2 - v_4^p (E - E_f^p)^3] \\
&\quad + \bar{V}_C \cdot v_1^p [v_2^p - 2v_3^p (E - E_f^p) + 3v_4^p (E - E_f^p)^2] \\
W_V(E) &= w_1^p \frac{(E - E_f^p)^2}{(E - E_f^p)^2 + (w_2^p)^2} \\
r_V &= 1.3039 - 0.4054A^{-1/3} \\
a_V &= 0.6778 - 1.487 \cdot 10^{-4} A \\
W_D(E) &= d_1^p \frac{(E - E_f^p)^2}{(E - E_f^p)^2 + (d_3^p)^2} \exp[-d_2^p (E - E_f^p)] \\
r_D &= 1.3424 - 0.01585A^{1/3} \\
a_D &= 0.5187 + 5.205 \cdot 10^{-4} A \\
V_{SO}(E) &= v_{so1}^p \exp[-v_{so2}^p (E - E_f^p)] \\
W_{SO}(E) &= w_{so1}^p \frac{(E - E_f^p)^2}{(E - E_f^p)^2 + (w_{so2}^p)^2} \\
r_{SO} &= 1.1854 - 0.647A^{-1/3} \\
a_{SO} &= 0.59 \\
r_C &= 1.198 + 0.697A^{-2/3} + 12.994A^{-5/3},
\end{aligned} \tag{4.9}$$

where the parameters for the potential depths,  $\bar{V}_C$  and  $E_f^p$  are given in Table 4.2. The functional form of the proton global OMP differs from the neutron global OMP only by the Coulomb correction term in  $V_V(E)$ .

The spherical optical model described above provides the transmission coefficients, DWBA cross sections, total and elastic cross sections, etc., mentioned in the beginning of this section. For deformed nuclides, strongly coupled collective levels need to be included. This will be explained in Section 4.2 on direct reactions.

#### 4.1.2 Spherical OMP: Complex particles

For deuterons, tritons, Helium-3 and alpha particles, we use a simplification of the folding approach of Watanabe [41], see Ref. [42]. We take the nucleon OMPs described in the previous section, either local or global, as the basis for these complex particle potentials.

$v_1^n$	$= 59.30 - 21.0(N - Z)/A - 0.024A$	MeV
$v_2^n$	$= 0.007228 - 1.48 \cdot 10^{-6} A$	MeV <sup>-1</sup>
$v_3^n$	$= 1.994 \cdot 10^{-5} - 2.0 \cdot 10^{-8} A$	MeV <sup>-2</sup>
$v_4^n$	$= 7 \cdot 10^{-9}$	MeV <sup>-3</sup>
$w_1^n$	$= 12.195 + 0.0167A$	MeV
$w_2^n$	$= 73.55 + 0.0795A$	MeV
$d_1^n$	$= 16.0 - 16.0(N - Z)/A$	MeV
$d_2^n$	$= 0.0180 + 0.003802/(1 + \exp[(A - 156.)/8.])$	MeV <sup>-1</sup>
$d_3^n$	$= 11.5$	MeV
$v_{so1}^n$	$= 5.922 + 0.0030A$	MeV
$v_{so2}^n$	$= 0.0040$	MeV <sup>-1</sup>
$w_{so1}^n$	$= -3.1$	MeV
$w_{so2}^n$	$= 160.$	MeV
$E_f^n$	$= -11.2814 + 0.02646A$	MeV

Table 4.1: Potential depth parameters and Fermi energy for the neutron global OMP of Eq. (4.8).

$v_1^p$	$= 59.30 + 21.0(N - Z)/A - 0.024A$	MeV
$v_2^p$	$= 0.007067 + 4.23 \cdot 10^{-6} A$	MeV <sup>-1</sup>
$v_3^p$	$= 1.729 \cdot 10^{-5} + 1.136 \cdot 10^{-8} A$	MeV <sup>-2</sup>
$v_4^p$	$= v_4^n$	MeV <sup>-3</sup>
$w_1^p$	$= 14.667 + 0.009629A$	MeV
$w_2^p$	$= w_2^n$	MeV
$d_1^p$	$= 16.0 + 16.0(N - Z)/A$	MeV
$d_2^p$	$= d_2^n$	MeV <sup>-1</sup>
$d_3^p$	$= d_3^n$	MeV
$v_{so1}^p$	$= v_{so1}^n$	MeV
$v_{so2}^p$	$= v_{so2}^n$	MeV <sup>-1</sup>
$w_{so1}^p$	$= w_{so1}^n$	MeV
$w_{so2}^p$	$= w_{so2}^n$	MeV
$E_f^p$	$= -8.4075 + 0.01378A$	MeV
$\bar{V}_C$	$= 1.73 \cdot Z \cdot A^{-1/3} / r_C$	MeV

Table 4.2: Potential depth parameters and Fermi energy for the proton global OMP of Eq. (4.9). The parameter values for neutrons are given in Table 4.1.  $\bar{V}_C$  appears in the Coulomb correction term  $\Delta V_C(E)$ , of the real central potential.

### Deuterons

For deuterons, the real central potential depth at incident energy  $E$  is

$$V_V^{deuteron}(E) = V_V^{neutron}(E/2) + V_V^{proton}(E/2), \quad (4.10)$$

and similarly for  $W_V$  and  $W_D$ . For the spin-orbit potential depth we have

$$V_{SO}^{deuteron}(E) = (V_{SO}^{neutron}(E) + V_{SO}^{proton}(E))/2, \quad (4.11)$$

and similarly for  $W_{SO}$ . For the radius and diffuseness parameter of the real central potential we have

$$\begin{aligned} r_V^{deuteron} &= (r_V^{neutron} + r_V^{proton})/2, \\ a_V^{deuteron} &= (a_V^{neutron} + a_V^{proton})/2, \end{aligned} \quad (4.12)$$

and similarly for the geometry parameters of the other potentials.

Note that several of these formulae are somewhat more general than necessary, since the nucleon potentials mostly have geometry parameters, and also potential depths such as  $V_{SO}$ , which are equal for neutrons and protons ( $a_D$  is an exception). The general formulae above have been implemented to also account for other potentials, if necessary.

### Tritons

For tritons, the real central potential depth at incident energy  $E$  is

$$V_V^{triton}(E) = 2V_V^{neutron}(E/3) + V_V^{proton}(E/3), \quad (4.13)$$

and similarly for  $W_V$  and  $W_D$ . For the spin-orbit potential depth we have

$$V_{SO}^{triton}(E) = (V_{SO}^{neutron}(E) + V_{SO}^{proton}(E))/6, \quad (4.14)$$

and similarly for  $W_{SO}$ . For the radius and diffuseness parameter of the real central potential we have

$$\begin{aligned} r_V^{triton} &= (2r_V^{neutron} + r_V^{proton})/3, \\ a_V^{triton} &= (2a_V^{neutron} + a_V^{proton})/3, \end{aligned} \quad (4.15)$$

and similarly for the geometry parameters of the other potentials.

### Helium-3

For Helium-3, the real central potential depth at incident energy  $E$  is

$$V_V^{Helium-3}(E) = V_V^{neutron}(E/3) + 2V_V^{proton}(E/3), \quad (4.16)$$

and similarly for  $W_V$  and  $W_D$ . For the spin-orbit potential depth we have

$$V_{SO}^{Helium-3}(E) = (V_{SO}^{neutron}(E) + V_{SO}^{proton}(E))/6, \quad (4.17)$$

and similarly for  $W_{SO}$ . For the radius and diffuseness parameter of the real central potential we have

$$\begin{aligned} r_V^{Helium-3} &= (r_V^{neutron} + 2r_V^{proton})/3, \\ a_V^{Helium-3} &= (a_V^{neutron} + 2a_V^{proton})/3, \end{aligned} \quad (4.18)$$

and similarly for the geometry parameters of the other potentials.

### Alpha particles

For alpha's, the real central potential depth at incident energy  $E$  is

$$V_V^{alphas}(E) = 2V_V^{neutron}(E/4) + 2V_V^{proton}(E/4), \quad (4.19)$$

and similarly for  $W_V$  and  $W_D$ . For the spin-orbit potential depth we have

$$V_{SO}^{alphas}(E) = W_{SO}^{alphas}(E) = 0. \quad (4.20)$$

For the radius and diffuseness parameter of the real central potential we have

$$\begin{aligned} r_V^{alphas} &= (r_V^{neutron} + r_V^{proton})/2, \\ a_V^{alphas} &= (a_V^{neutron} + a_V^{proton})/2, \end{aligned} \quad (4.21)$$

and similarly for the geometry parameters of the other potentials.

### 4.1.3 Systematics for non-elastic cross sections

Since the reaction cross sections for complex particles as predicted by the OMP have not been tested and rely on a relatively simple folding model, we added a possibility to estimate the non-elastic cross sections from empirical expressions. The adopted *tripathi.f* subroutine that provides this does not coincide with the published expression as given by Tripathi et al. [43], but checking our results with the published figures of Ref. [43] made us decide to adopt this empirical model as an option. We generally use it for deuterons up to alpha-particles. A high-quality OMP for complex particles would make this option redundant.

## 4.2 Direct reactions

Various models for direct reactions are included in the program: DWBA for (near-)spherical nuclides, coupled-channels for deformed nuclides, the weak-coupling model for odd nuclei, and also a giant resonance contribution in the continuum. In all cases, TALYS drives the ECIS-97 code to perform the calculations. The results are presented as discrete state cross sections and angular distributions, or as contributions to the continuum.

### 4.2.1 Deformed nuclei: Coupled-channels

The formalism outlined in the previous section works, theoretically, for nuclides which are spherical and, in practice, for nuclides which are not too strongly deformed. In general, however, the more general coupled-channels method should be invoked to describe simultaneously the elastic scattering channel and the low-lying states which are, due to their collective nature, strongly excited in inelastic scattering. These collective excitations can be described as the result of static or dynamic deformations, which cause the homogeneous neutron-proton fluid to rotate or vibrate. The associated deformation parameters can be predicted from a (semi-)microscopic model or can be derived from an analysis of the experimental angular distributions.

The coupled-channels formalism for scattering and reaction studies is well known and will not be described in this manual. For a detailed presentation, we refer to Ref. [44]. We will only state the main aspects here to put the formalism into practice. Refs. [45] and [46] have been used as guidance. In general various different channels, usually the ground state and several inelastic states, are included in a coupling scheme while the associated coupled equations are solved. In ECIS-97, this is done in a so called sequential iterative approach [35]. Besides Ref. [35], Ref. [47] is also recommended for more insight in the use of the ECIS code.

Various collective models for deformed nuclei exist. Note that the spherical optical model of Eq. (4.2) is described in terms of the nuclear radius  $R_i = r_i A^{1/3}$ . For deformed nuclei, this expression is generalized to include collective motions. Various models have been implemented in ECIS-97, which enables us to cover many nuclides of interest. We will describe the ones that can be invoked by TALYS. The collective models are automatically applied upon reading the deformation parameter database, see Section 5.5.

### Symmetric rotational model

In the symmetric rotational model, the radii of the different terms of the OMP are expressed as

$$R_i = r_i A^{1/3} \left[ 1 + \sum_{\lambda=2,4,\dots} \beta_\lambda Y_\lambda^0(\Omega) \right], \quad (4.22)$$

where the  $\beta_\lambda$ 's are permanent, static deformation parameters, and the  $Y$  functions are spherical harmonics. The quadrupole deformation  $\beta_2$  plays a leading role in the interaction process. Higher order deformations  $\beta_\lambda$  (with  $\lambda = 4, 6, \dots$ ) are systematically smaller in magnitude than  $\beta_2$ . The inclusion of  $\beta_4$  and  $\beta_6$  deformations in coupled-channels calculations produces changes in the predicted observables, but in general, only  $\beta_2$  and  $\beta_4$  are important in describing inelastic scattering to the first few levels in a rotational band. For even-even nuclides like  $^{184}\text{W}$  and  $^{232}\text{Th}$ , the symmetric rotational model provides a good description of the lowest  $0^+$ ,  $2^+$ ,  $4^+$  (and often  $6^+$ ,  $8^+$ , etc.) rotational band. The nuclear model and parameter database of TALYS specifies whether a rotational model can be used for a particular nucleus, together with the included levels and deformation parameters. Either a deformation parameter  $\beta_\lambda$  or a deformation length  $\delta_\lambda = \beta_\lambda r_i A^{1/3}$  may be given. The latter one is generally recommended since it has more physical meaning than  $\beta_\lambda$  and should not depend on incident energy (while  $r_i$  may, in some optical models, depend on energy). We take  $\delta_\lambda$  equal for the three OMP components  $V_V$ ,  $W_V$  and  $W_D$  and take the spin-orbit potential undeformed. The same holds for the vibrational and other collective models.

### Harmonic vibrational model

A vibrational nucleus possesses a spherically symmetric ground state. Its excited states undergo shape oscillations about the spherical equilibrium model. In the harmonic vibrational model, the radii of the different terms of the OMP are expressed as

$$R_i = r_i A^{1/3} \left[ 1 + \sum_{\lambda\mu} \alpha_{\lambda\mu} Y_\lambda^\mu(\Omega) \right], \quad (4.23)$$

where the  $\alpha_{\lambda,\mu}$  operators can be related to the coupling strengths  $\beta_\lambda$ , describing the vibration amplitude with multipolarity  $\lambda$ . Expanding the OMP to first or second order with this radius gives the OMP expressions for the excitation of one-phonon (first order vibrational model) and two-phonon (second order vibrational model) states [35]. For vibrational nuclei, the minimum number of states to couple is two. For even-even nuclei, we generally use the  $(0^+, 2^+)$  coupling, where the  $2^+$  level is a one-quadrupole phonon excitation. The level scheme of a vibrational nucleus (e.g.  $^{110}\text{Pd}$ ) often consists of a one-phonon state ( $2^+$ ) followed by a  $(0^+, 2^+, 4^+)$  triplet of two-phonon states. When this occurs, all levels are included in the coupling scheme with the associated deformation length  $\delta_2$  (or deformation parameter  $\beta_2$ ). If the  $3^-$  and  $5^-$  states are strongly collective excitations, that is when  $\beta_3$  and  $\beta_5$  are larger than 0.1, these levels may also be included in the coupling scheme. An example is  $^{120}\text{Sn}$  [48], where the low lying  $(0^+, 2^+, 3^-, 4^+, 5^-)$  states can all be included as one-phonon states in a single coupling scheme.

### Vibration-rotational model

For certain nuclides, the level scheme consists not only of one or more rotational bands, but also of one or more vibrational bands that can be included in the coupling scheme. An example is  $^{238}\text{U}$ , where many vibrational bands can be coupled. In Chapter 5 on nuclear model parameters, it is explained how such calculations are automatically performed by TALYS. Depending on the number of levels included, the calculations can be time-consuming.

### Asymmetric rotational model

In the asymmetric rotational model, in addition to the spheroidal equilibrium deformation, the nucleus can oscillate such that ellipsoidal shapes are produced. In this model the nucleus has rotational bands built on the statically deformed ground state and on the  $\gamma$ -vibrational state. The radius is now angular dependent,

$$R_i(\Theta) = r_i A^{1/3} \left[ 1 + \beta_2 \cos \gamma Y_2^0(\Omega) + \sqrt{\frac{1}{2}} \beta_2 \sin \gamma (Y_2^2(\Omega) + Y_2^{-2}(\Omega)) + \beta_4 Y_4^0(\Omega) \right], \quad (4.24)$$

where we restrict ourselves to a few terms. The deformation parameters  $\beta_2$ ,  $\beta_4$  and  $\gamma$  need to be specified.  $^{24}\text{Mg}$  is an example of a nucleus that can be analyzed with the asymmetric rotational model. Mixing between bands is not yet automated as an option in TALYS.

## 4.2.2 Distorted Wave Born Approximation

The Distorted Wave Born Approximation (DWBA) is only valid for small deformations. Until the advent of the more general coupled-channels formalism, it was the commonly used method to describe inelastic scattering, for both weakly and strongly coupled levels. Nowadays, we see DWBA as a first order vibrational model for small deformation, with only a single iteration to be performed for the coupled-channels solution. (See, however Satchler [49] for the exact difference between this so called distorted wave method and DWBA). The interaction between the projectile and the target nucleus is modeled by the derivative of the OMP for elastic scattering times a strength parameter. The latter, the deformation parameter  $\beta_\lambda$ , is then often used to vary the overall magnitude of the cross section (which is proportional to  $\beta_\lambda^2$ ).

In TALYS, we use DWBA

- (a) if a deformed OMP is not available. This applies for the spherical OMPs mentioned in the previous Section, which are all based on elastic scattering observables only. Hence, if we have not constructed a coupled-channels potential, TALYS will automatically use (tabulated or systematic) deformation parameters for DWBA calculations.
- (b) if a deformed OMP is used for the first excited states only. For the levels that do not belong to that basic coupling scheme, e.g. for the many states at somewhat higher excitation energy, we use DWBA with (very) small deformation parameters.

### 4.2.3 Odd nuclei: Weak coupling

Direct inelastic scattering off odd- $A$  nuclei can be described by the weak-coupling model [50], which assumes that a valence particle or hole interacts only weakly with a collective core excitation. Hence the model implies that the nucleon inelastic scattering by the odd- $A$  nucleus is very similar to that by the even core alone, i.e. the angular distributions have a similar shape. Let  $L$  be the spin of the even core state, and  $J_0$  and  $J$  the spin of the ground and excited state, respectively, of the odd- $A$  nucleus, resulting from the angular momentum coupling. Then, the spins  $J$  of the multiplet states in the odd- $A$  nucleus range from  $|L - J_0|$  to  $(L + J_0)$ . If the strength of the inelastic scattering is characterized by the square of the deformation parameters  $\beta_{L,J}^2$ , then the sum of all  $\beta_{L,J}^2$  or  $\sigma(E)$  for the transitions in the odd- $A$  nucleus should be equal to the value  $\beta_L^2$  or  $\sigma(E)$  for the single transition in the even core nucleus:

$$\sum_J \beta_{L,J}^2 = \beta_L^2, \quad \sum_J \sigma_{J_0 \rightarrow J} = \sigma_{0 \rightarrow L}, \quad (4.25)$$

where the symbol  $0 \rightarrow L$  indicates a transition between the ground state to the excited state with spin  $L$  in the even core nucleus. The deformation parameters  $\beta_{L,J}^2$  are now given by

$$\beta_{L,J}^2 = \frac{2J + 1}{(2J_0 + 1)(2L + 1)} \beta_L^2. \quad (4.26)$$

In practice, the DWBA cross sections are calculated for the real mass of the target nucleus and at the exact excitation energies of the odd- $A$  states, but for the even-core spin  $L$  and with deformation parameters  $\beta_{L,J}$ .

We stress that our weak-coupling model is not full-proof. First of all, there are always two choices for the even-even core. The default used in TALYS (by means of the keyword **core -1**) is to use the even-even core obtained by subtracting a nucleon, but the other choice (**core 1**), to obtain the even-even core by adding a nucleon, may sometimes be more appropriate. The next uncertainty is the choice of levels in the odd- $A$  core. We select the levels that are closest to the excitation energy of the even-spin state of the even-even core. Again, this may not always be the most appropriate choice. A future option is to designate these levels manually.

### 4.2.4 Giant resonances

The high-energy part of the continuum spectra are generally described by pre-equilibrium models. These models are essentially of a single-particle nature. Upon inspection of continuum spectra, some structure

in the high-energy tail is observed that can not be accounted for by the smooth background of the single-particle pre-equilibrium model. For example, many 14 MeV inelastic neutron spectra show a little hump at excitation energies around 6-10 MeV. This structure is due to collective excitations of the nucleus that are known as giant resonances [51, 52]. We use a macroscopic, phenomenological model to describe giant resonances in the inelastic channel. For each multipolarity, an energy weighted sum rule (EWSR)  $S_\ell$  applies,

$$S_\ell = \sum_i E_{\ell,i} \beta_{\ell,i}^2 = 57.5 A^{-5/3} l(l+1) \text{ MeV}, \quad (4.27)$$

where  $E_{\ell,i}$  is the excitation energy of the  $i$ -th state with multipolarity  $\ell$ . The summation includes all the low-lying collective states, for each  $\ell$ , that have already been included in the coupled-channels or DWBA formalism. The EWSR thus determines the remaining collective strength that is spread over the continuum. Our treatment is phenomenological in the sense that we perform a DWBA calculation with ECIS-97 for each giant resonance state and spread the cross section over the continuum with a Gaussian distribution. The central excitation energy for these states and the spreading width is different for each multipolarity and has been empirically determined. For the giant monopole resonance (GMR) EWSR we have

$$S_0 = 23 A^{-5/3} \text{ MeV}, \quad (4.28)$$

with excitation energy and width

$$E_{0,GMR} = 18.7 - 0.025 A \text{ MeV}, \quad \Gamma_{GMR} = 3 \text{ MeV}. \quad (4.29)$$

The EWSR for the giant quadrupole resonance (GQR) is

$$S_2 = 575 A^{-5/3} \text{ MeV}, \quad (4.30)$$

with

$$E_{0,GQR} = 65 A^{-1/3} \text{ MeV}, \quad \Gamma_{GQR} = 85 A^{-2/3} \text{ MeV}. \quad (4.31)$$

The EWSR for the giant octupole resonance is

$$S_3 = 1208 A^{-5/3} \text{ MeV}, \quad (4.32)$$

which has a low-energy (LEOR) and a high-energy (HEOR) component. Following Kalbach [52], we assume

$$S_{3,LEOR} = 0.3 S_3, \quad S_{3,HEOR} = 0.7 S_3, \quad (4.33)$$

with excitation energy and width

$$E_{0,LEOR} = 31 A^{-1/3} \text{ MeV}, \quad \Gamma_{LEOR} = 5 \text{ MeV}, \quad (4.34)$$

and

$$E_{0,HEOR} = 115 A^{-1/3} \text{ MeV}, \quad \Gamma_{HEOR} = 9.3 - A/48 \text{ MeV}, \quad (4.35)$$

respectively. We also take as width for the actual Gaussian distribution  $\Gamma_{Gauss} = 0.42 \Gamma_\ell$ .

The contribution from giant resonances is automatically included in the total inelastic cross section. The effect is most noticeable in the single- and double-differential energy spectra.

### 4.3 Gamma-ray transmission coefficients

Gamma-ray transmission coefficients are important for the description of the gamma emission channel in nuclear reactions. This is an almost universal channel since gamma rays, in general, may accompany emission of any other emitted particle. Like the particle transmission coefficients that emerge from the optical model, gamma-ray transmission coefficients enter the Hauser-Feshbach model for the calculation of the competition of photons with other particles.

The gamma-ray transmission coefficient for multipolarity  $\ell$  of type  $X$  (where  $X = M$  or  $E$ ) is given by

$$T_{X\ell}(E_\gamma) = 2\pi f_{X\ell}(E_\gamma) E_\gamma^{2\ell+1}, \quad (4.36)$$

where  $E_\gamma$  denotes the gamma energy and  $f_{X\ell}(E_\gamma)$  is the energy-dependent gamma-ray strength function.

#### 4.3.1 Gamma-ray strength functions

We have included two models for the gamma-ray strength function. The first is the so-called Brink-Axel option [53], in which a standard Lorentzian form describes the giant dipole resonance shape, i.e.

$$f_{X\ell}(E_\gamma) = K_{X\ell} \frac{\sigma_{X\ell} E_\gamma \Gamma_{X\ell}^2}{(E_\gamma^2 - E_{X\ell}^2)^2 + E_\gamma^2 \Gamma_{X\ell}^2}, \quad (4.37)$$

where  $\sigma_{X\ell}$ ,  $E_{X\ell}$  and  $\Gamma_{X\ell}$  are the strength, energy and width of the giant resonance, respectively, and

$$K_{X\ell} = \frac{1}{(2\ell + 1)\pi^2 \hbar^2 c^2}. \quad (4.38)$$

At present, we use the Brink-Axel option for all transition types other than  $E1$ . For  $E1$  radiation, the default option used in TALYS is the generalized Lorentzian form of Kopecky and Uhl [54],

$$f_{E1}(E_\gamma, T) = K_{E1} \left[ \frac{E_\gamma \tilde{\Gamma}_{E1}(E_\gamma)}{(E_\gamma^2 - E_{E1}^2)^2 + E_\gamma^2 \tilde{\Gamma}_{E1}(E_\gamma)^2} + \frac{0.7 \Gamma_{E1} 4\pi^2 T^2}{E_{E1}^3} \right] \sigma_{E1} \Gamma_{E1}, \quad (4.39)$$

where the energy-dependent damping width  $\tilde{\Gamma}(E_\gamma)$  is given by

$$\tilde{\Gamma}_{E1}(E_\gamma) = \Gamma_{E1} \frac{E_\gamma^2 + 4\pi^2 T^2}{E_{E1}^2}, \quad (4.40)$$

and  $T$  is the nuclear temperature given by

$$T = \sqrt{\frac{S_n - E_\gamma}{a(S_n)}}, \quad (4.41)$$

where  $S_n$  is the neutron separation energy and  $a$  the level density parameter at  $S_n$ .

For  $E1$ -transitions, GDR parameters for various individual nuclides exist. These are stored in the nuclear structure database of TALYS, see Chapter 5. Certain nuclides have a splitted GDR, i.e. a second set of Lorentzian parameters. For these cases, the incoherent sum of two strength functions is taken.

For all transitions other than  $E1$ , systematic formulae compiled by Kopecky [36], for the resonance parameters are used. For  $E1$  transitions for which no tabulated data exist, we use

$$\sigma_{E1} = 1.2 \times 120NZ/(A\pi\Gamma_{E1}) \text{ mb}, \quad E_{E1} = 31.2A^{-1/3} + 20.6A^{-1/6} \text{ MeV}, \quad \Gamma_{E1} = 0.026E_{E1}^{1.91} \text{ MeV}. \quad (4.42)$$

For  $E2$  transitions we use

$$\sigma_{E2} = 0.00014Z^2 E_{E2}/(A^{1/3}\Gamma_{E2}) \text{ mb}, \quad E_{E2} = 63.A^{-1/3} \text{ MeV}, \quad \Gamma_{E2} = 6.11 - 0.012A \text{ MeV}. \quad (4.43)$$

For multipole radiation higher than  $E2$ , we use

$$\sigma_{E\ell} = 8.10^{-4}\sigma_{E(\ell-1)}, \quad E_{E\ell} = E_{E(\ell-1)} \quad \Gamma_{E\ell} = \Gamma_{E(\ell-1)}, \quad (4.44)$$

For  $M1$  transitions we use

$$f_{M1} = 1.58A^{0.47} \text{ at } 7 \text{ MeV}, \quad E_{M1} = 41.A^{-1/3} \text{ MeV}, \quad \Gamma_{M1} = 4 \text{ MeV}, \quad (4.45)$$

where Eq. (4.37) thus needs to be applied at 7 MeV to obtain the  $\sigma_{M1}$  value. For multipole radiation higher than  $M1$ , we use

$$\sigma_{M\ell} = 8.10^{-4}\sigma_{M(\ell-1)}, \quad E_{M\ell} = E_{M(\ell-1)} \quad \Gamma_{M\ell} = \Gamma_{M(\ell-1)}, \quad (4.46)$$

For all cases, the systematics can be overruled with user-defined input parameters.

### 4.3.2 Renormalisation of gamma-ray strength functions

At sufficiently low incident neutron energies, the average radiative capture width  $\Gamma_\gamma$  is due entirely to the  $s$ -wave interaction, and it is  $\Gamma_\gamma$  at the neutron separation energy  $S_n$  that is often used to renormalize gamma-ray transmission coefficients [55]. The  $\Gamma_\gamma$  values are, when available, read from our nuclear structure database. For nuclides for which no experimental value is available, we use an interpolation table by Kopecky [56] for  $40 < A < 250$ , the simple form

$$\Gamma_\gamma = 1593/A^2 \text{ eV}, \quad (4.47)$$

for  $A > 250$ , while we apply no gamma renormalization for  $A < 40$ .

The  $s$ -wave radiation width may be obtained by integrating the gamma-ray transmission coefficients over the density of final states that may be reached in the first step of the gamma-ray cascade. The normalisation is then carried out as follows

$$\frac{2\pi\Gamma_\gamma}{D_0} = G_{norm} \sum_J \sum_\Pi \sum_{X\ell} \sum_{I'=|J-\ell|}^{J+\ell} \sum_{\Pi'} \int_0^{S_n} dE_\gamma T_{X\ell}(E_\gamma) \rho(S_n - E_\gamma, I', \Pi') f(X, \Pi', \ell), \quad (4.48)$$

where  $D_0$  is the average resonance spacing and  $\rho$  is the level density. The  $J, \Pi$  sum is over the compound nucleus states with spin  $J$  and parity  $\Pi$  that can be formed with  $s$ -wave incident particles, and  $I', \Pi'$  denote the spin and parity of the final states. The multipole selection rules are  $f(E, \Pi', \ell) = 1$  if  $\Pi = \Pi'(-1)^\ell$ ,  $f(M, \Pi', \ell) = 1$  if  $\Pi = \Pi'(-1)^{\ell+1}$ , and 0 otherwise. It is understood that the integral over  $dE_\gamma$  includes a summation over discrete states.  $G_{norm}$  is the normalisation factor that ensures the

equality (4.48). In practice, the transmission coefficients (4.36) are thus multiplied by  $G_{norm}$  before they enter the nuclear reaction calculation.  $G_{norm}$  can be specified by the user. The default is the value returned by Eq. (4.48). If  $G_{norm} = 1$  is specified, no normalisation is carried out and strength functions purely determined from giant resonance parameters are taken. Other values can be entered for  $G_{norm}$ , e.g. for fitting of the neutron capture cross section. Normalisation per multipolarity can be performed by adjusting the  $\sigma_{X\ell}$  values in the input, see Chapter 6.

### 4.3.3 Photoabsorption cross section

TALYS requires photo-absorption cross sections for photo-nuclear reactions and for pre-equilibrium gamma-ray emission. Following Chadwick et al. [57], the photo-absorption cross section is given by

$$\sigma_{abs}(E_\gamma) = \sigma_{GDR}(E_\gamma) + \sigma_{QD}(E_\gamma). \quad (4.49)$$

The GDR component is related to the strength functions outlined above. It is given by

$$\sigma_{GDR}(E_\gamma) = \sum_i \sigma_{E1} \frac{(E_\gamma \Gamma_{E1,i})^2}{(E_\gamma^2 - E_{E1,i}^2)^2 + E_\gamma^2 \Gamma_{E1,i}^2}, \quad (4.50)$$

where the parameters were specified in the previous subsection. The sum over  $i$  is over the number of parts into which the GDR is split.

The quasi-deuteron component  $\sigma_{QD}$  is given by

$$\sigma_{QD}(E_\gamma) = L \frac{NZ}{A} \sigma_d(E_\gamma) f(E_\gamma). \quad (4.51)$$

Here,  $\sigma_d(E_\gamma)$  is the experimental deuteron photo-disintegration cross section, parameterized as

$$\sigma_d(E_\gamma) = 61.2 \frac{(E_\gamma - 2.224)^{3/2}}{E_\gamma^3}, \quad (4.52)$$

for  $E_\gamma > 2.224$  MeV and zero otherwise. The so-called Levinger parameter is  $L = 6.5$  and the Pauli-blocking function is approximated by the polynomial expression

$$f(E_\gamma) = 8.3714 \cdot 10^{-2} - 9.8343 \cdot 10^{-3} E_\gamma + 4.1222 \cdot 10^{-4} E_\gamma^2 - 3.4762 \cdot 10^{-6} E_\gamma^3 + 9.3537 \cdot 10^{-9} E_\gamma^4 \quad (4.53)$$

for  $20 < E_\gamma < 140$  MeV,

$$f(E_\gamma) = \exp(-73.3/E_\gamma) \quad (4.54)$$

for  $E_\gamma < 20$  MeV, and

$$f(E_\gamma) = \exp(-24.2348/E_\gamma) \quad (4.55)$$

for  $E_\gamma > 140$  MeV.

## 4.4 Pre-equilibrium reactions

It is now well-known that the separation of nuclear reaction mechanisms into direct and compound is too simplistic. As Fig. 3.2 shows, the cross section as predicted by the pure compound process is too small with respect to measured continuum spectra, and the direct processes described in the previous section only excite the discrete levels at the highest outgoing energies. Furthermore, the measured angular distributions in the region between direct and compound are anisotropic, indicating the existence of a memory-preserving, direct-like reaction process. Apparently, as an intermediate between the two extremes, there exists a reaction type that embodies both direct- and compound-like features. These reactions are referred to as *pre-equilibrium*, *precompound* or, when discussed in a quantum-mechanical context, *multi-step processes*. Pre-equilibrium emission takes place after the first stage of the reaction but long before statistical equilibrium of the compound nucleus is attained. It is imagined that the incident particle step-by-step creates more complex states in the compound system and gradually loses its memory of the initial energy and direction. Pre-equilibrium processes cover a sizeable part of the reaction cross section for incident energies between 10 and (at least) 200 MeV. Pre-equilibrium reactions have been modeled both classically and quantum-mechanically and both are included in TALYS.

### 4.4.1 Exciton model

In the exciton model (see Refs. [3, 58, 59] for extensive reviews), the nuclear state is characterized at any moment during the reaction by the total energy  $E^{tot}$  and the total number of particles above and holes below the Fermi surface. Particles ( $p$ ) and holes ( $h$ ) are indiscriminately referred to as excitons. Furthermore, it is assumed that all possible ways of sharing the excitation energy between different particle-hole configurations with the same exciton number  $n = p + h$  have equal a-priori probability. To keep track of the evolution of the scattering process, one merely traces the temporal development of the exciton number, which changes in time as a result of intranuclear two-body collisions. The basic starting point of the exciton model is a time-dependent master equation, which describes the probability of transitions to more and less complex particle-hole states as well as transitions to the continuum (emission). Upon integration over time, the energy-averaged emission spectrum is obtained. These assumptions makes the exciton model amenable for practical calculations. The price to be paid, however, is the introduction of a free parameter, namely the average matrix element of the residual two-body interaction, occurring in the transition rates between two exciton states. When this matrix element is properly parameterized, a very powerful model is obtained.

Qualitatively, the equilibration process of the excited nucleus is imagined to proceed as follows, see Fig. 4.2. After entering the target nucleus, the incident particle collides with one of the nucleons of the Fermi sea, with depth  $E_F$ . The formed state with  $n = 3$  (2p1h), in the case of a nucleon-induced reaction, is the first that is subject to particle emission, confirming the picture of the exciton model as a compound-like model rather than a direct-like model. Subsequent interactions result in changes in the number of excitons, characterized by  $\Delta n = +2$  (a new particle-hole pair) or  $\Delta n = -2$  (annihilation of a particle-hole pair) or  $\Delta n = 0$  (creation of a different configuration with the same exciton number). In the first stage of the process, corresponding to low exciton numbers, the  $\Delta n = +2$  transitions are predominant. Apart from transitions to more complex or less complex exciton states, at any stage there is a non-zero probability that a particle is emitted. Should this happen at an early stage, it is intuitively clear

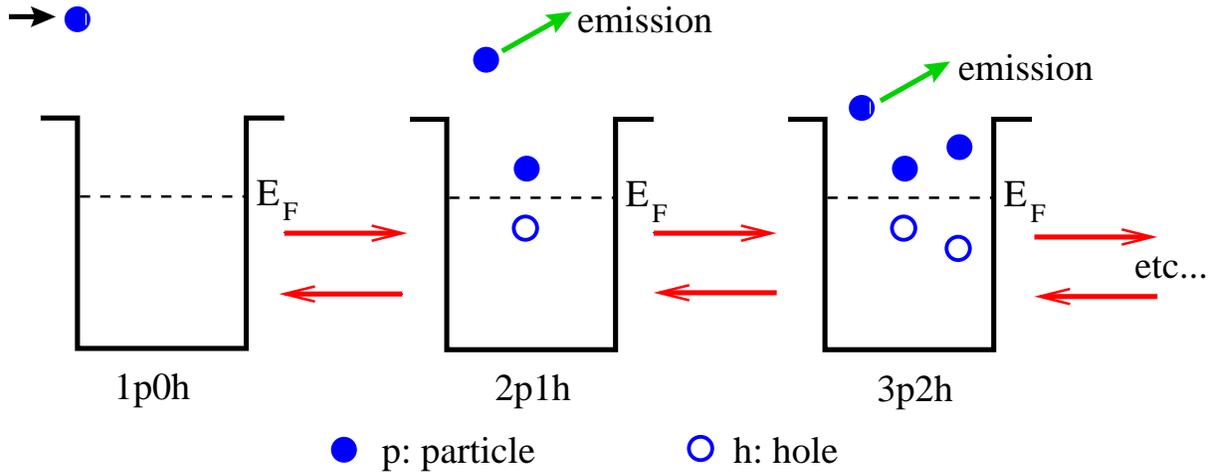


Figure 4.2: Reaction flow in exciton model

that the emitted particle retains some “memory” of the incident energy and direction: the hypothesis of a fully equilibrated compound nucleus is not valid. This phase is called the pre-equilibrium phase, and it is responsible for the experimentally observed high-energy tails and forward-peaked angular distributions. If emission does not occur at an early stage, the system eventually reaches a (quasi-) equilibrium. The equilibrium situation, corresponding to high exciton numbers, is established after a large number of interactions, i.e. after a long lapse of time, and the system has “forgotten” about the initial state. Accordingly, this stage may be called the compound or evaporation stage. Hence, in principle the exciton model enables to compute the emission cross sections in a unified way, without introducing adjustments between equilibrium and pre-equilibrium contributions. However, in practical cases it turns out that it is simpler and even more accurate to distinguish between a pre-equilibrium and an equilibrium phase and to perform the latter with the usual Hauser-Feshbach formalism. This is the approach followed in TALYS.

Two versions of the exciton model are implemented in TALYS: The default is the two-component model in which the neutron or proton types of particles and holes are followed throughout the reaction. We describe this model first, and then discuss the simpler, and more generally known, one-component model which is also implemented as an option. The following Section contains basically the most important equations of the recent exciton model study of [3].

### Two-component exciton model

In the following reaction equations, we use a notation in which  $p_\pi$  ( $p_\nu$ ) is the proton (neutron) particle number and  $h_\pi$  ( $h_\nu$ ) the proton (neutron) hole number. From this, we define the proton exciton number  $n_\pi = p_\pi + h_\pi$  and the neutron exciton number  $n_\nu = p_\nu + h_\nu$ . From this, we can construct the charge-independent particle number  $p = p_\pi + p_\nu$ , the hole number  $h = h_\pi + h_\nu$  and the exciton number  $n = n_\pi + n_\nu$ .

The temporal development of the system can be described by a master equation, describing the gain and loss terms for a particular class of exciton states, see [3]. Integrating the master equation over time up to the equilibration time  $\tau_{eq}$  yields the mean lifetime of the exciton state  $\tau$  that can be used to calculate the

differential cross section [60]. The primary pre-equilibrium differential cross section for the emission of a particle  $k$  with emission energy  $E_k$  can then be expressed in terms of  $\tau$ , the composite-nucleus formation cross section  $\sigma^{\text{CF}}$ , and an emission rate  $W_k$ ,

$$\begin{aligned} \frac{d\sigma_k^{\text{PE}}}{dE_k} &= \sigma^{\text{CF}} \sum_{p_\pi=p_\pi^0}^{p_\pi^{\text{max}}} \sum_{p_\nu=p_\nu^0}^{p_\nu^{\text{max}}} W_k(p_\pi, h_\pi, p_\nu, h_\nu, E_k) \tau(p_\pi, h_\pi, p_\nu, h_\nu) \\ &\times P(p_\pi, h_\pi, p_\nu, h_\nu), \end{aligned} \quad (4.56)$$

where the factor  $P$  represents the part of the pre-equilibrium population that has survived emission from the previous states and now passes through the  $(p_\pi, h_\pi, p_\nu, h_\nu)$  configurations, averaged over time. Expressions for all quantities appearing in this expression will be detailed in the rest of this Section. The initial proton and neutron particle numbers are  $p_\pi^0 = Z_p$ , and  $p_\nu^0 = N_p$ , respectively with  $Z_p$  ( $N_p$ ) the proton (neutron) number of the projectile. For any exciton state in the reaction process,  $h_\pi = p_\pi - p_\pi^0$  and  $h_\nu = p_\nu - p_\nu^0$ , so that for primary pre-equilibrium emission the initial hole numbers are  $h_\pi^0 = h_\nu^0 = 0$ . For e.g. a neutron-induced reaction, the initial exciton number is given by  $n^0 = n_\nu^0 = 1$  ( $0p_\pi 0h_\pi 1p_\nu 0h_\nu$ ), but only pre-equilibrium gamma emission can occur from this state (nucleon emission from this state is essentially elastic scattering and this is already covered by the optical model). Particle emission only occurs from  $n = 3$  ( $2p1h$ ) and higher exciton states. We use a hardwired value of  $p_\pi^{\text{max}} = p_\nu^{\text{max}} = 6$  as the upper limit of the summation, see [3]. We use the never-come-back approximation, i.e. throughout the cascade one neglects the interactions that decrease the exciton number, although the adopted solution of Eq. (4.56) does include transitions that convert a proton particle-hole pair into a neutron pair and vice versa. The maximum values  $p_\pi^{\text{max}}$  and  $p_\nu^{\text{max}}$  thus entail an automatic separation of the pre-equilibrium population and the compound nucleus population. The latter is then handled by the more adequate Hauser-Feshbach mechanism. We now discuss the various ingredients of Eq. (4.56).

**A. Reaction cross sections** The basic feeding term for pre-equilibrium emission is the compound formation cross section  $\sigma^{\text{CF}}$ , which is given by

$$\sigma^{\text{CF}} = \sigma_{\text{reac}} - \sigma_{\text{direct}}, \quad (4.57)$$

where the reaction cross section  $\sigma_{\text{reac}}$  is directly obtained from the optical model and  $\sigma_{\text{direct}}$  is the sum of the cross sections for direct reactions to discrete states  $\sigma^{\text{disc.direct}}$  as defined in Eq. (3.18), and for giant resonances, see Section 4.2.4.

**B. Emission rates and particle-hole state densities** The emission rate  $W_k$  has been derived by Cline and Blann [61] from the principle of microreversibility, and can easily be generalized to a two-component version [62]. The emission rate for an ejectile  $k$  with relative mass  $\mu_k$  and spin  $s_k$  is

$$\begin{aligned} W_k(p_\pi, h_\pi, p_\nu, h_\nu, E_k) &= \frac{2s_k + 1}{\pi^2 \hbar^3} \mu_k E_k \sigma_{k,\text{inv}}(E_k) \\ &\times \frac{\omega(p_\pi - Z_k, h_\pi, p_\nu - N_k, h_\nu, E^{\text{tot}} - E_k)}{\omega(p_\pi, h_\pi, p_\nu, h_\nu, E^{\text{tot}})}, \end{aligned} \quad (4.58)$$

where  $\sigma_{k,\text{inv}}(E_k)$  is the inverse reaction cross section, again calculated with the optical model,  $Z_k$  ( $N_k$ ) is the charge (neutron) number of the ejectile and  $E^{\text{tot}}$  is the total energy of the composite system.

For the particle-hole state density  $\omega(p_\pi, h_\pi, p_\nu, h_\nu, E_x)$  we use the expression of Běták and Dobeš [62, 63]. Their formula is based on the assumption of equidistant level spacing and is corrected for the effect of the Pauli exclusion principle and for the finite depth of the potential well. The two-component particle-hole state density is

$$\begin{aligned} \omega(p_\pi, h_\pi, p_\nu, h_\nu, E_x) &= \frac{g_\pi^{n_\pi} g_\nu^{n_\nu}}{p_\pi! h_\pi! p_\nu! h_\nu! (n-1)!} (U - A(p_\pi, h_\pi, p_\nu, h_\nu))^{n-1} \\ &\times f(p, h, U, V), \end{aligned} \quad (4.59)$$

where  $g_\pi$  and  $g_\nu$  are the single-particle state densities,  $A$  the Pauli correction,  $f$  the finite well function, and  $U = E_x - P_{p,h}$  with  $P_{p,h}$  Fu's pairing correction [64],

$$\begin{aligned} P_{p,h} &= \Delta - \Delta \left[ 0.996 - 1.76 \left( \frac{n}{n_{\text{crit}}} \right)^{1.6} \left( \frac{E_x}{\Delta} \right)^{0.68} \right]^2 \\ &\text{if } E_x/\Delta \geq 0.716 + 2.44 \left( \frac{n}{n_{\text{crit}}} \right)^{2.17}, \\ &= \Delta \text{ otherwise,} \end{aligned} \quad (4.60)$$

with

$$n_{\text{crit}} = 2gT_{\text{crit}} \ln 2, \quad (4.61)$$

where  $T_{\text{crit}} = 2\sqrt{\Delta/\frac{1}{4}g}/3.5$  and  $g = g_\pi + g_\nu$ . The pairing energy  $\Delta$  for total level densities is given by

$$\Delta = \chi \frac{12}{\sqrt{A}}, \quad (4.62)$$

where here  $A$  is the mass number and  $\chi = 0, 1$  or  $2$  for odd-odd, odd or even-even nuclei. The Pauli correction term is given by

$$\begin{aligned} A(p_\pi, h_\pi, p_\nu, h_\nu) &= \frac{[\max(p_\pi, h_\pi)]^2}{g_\pi} + \frac{[\max(p_\nu, h_\nu)]^2}{g_\nu} \\ &- \frac{p_\pi^2 + h_\pi^2 + p_\pi + h_\pi}{4g_\pi} - \frac{p_\nu^2 + h_\nu^2 + p_\nu + h_\nu}{4g_\nu}. \end{aligned} \quad (4.63)$$

For the single-particle state densities we take

$$g_\pi = Z/15, \quad g_\nu = N/15, \quad (4.64)$$

which is, through the relationship  $g = a\pi^2/6$ , in line with the values for our total level density parameter  $a$ , see Eq. (4.204), and also provides a globally better description of spectra than the generally adopted  $g = A/13$ .

The finite well function  $f(p, h, E_x, V)$  accounts for the fact that a hole cannot have an energy below that of the bottom of the potential well depth  $V$ . It is given by

$$f(p, h, E_x, V) = 1 + \sum_{i=1}^h (-1)^i \binom{h}{i} \left[ \frac{E_x - iV}{E_x} \right]^{n-1} \Theta(E_x - iV), \quad (4.65)$$

where  $\Theta$  is the unit step function. Note that  $f$  is different from 1 only for excitation energies greater than  $V$ . In the original version of Běták and Dobeš,  $V$  is given by the depth  $E_f$  of the Fermi well. This was generalized by Kalbach [65, 52] to obtain an effective method to include surface effects in the first stage of the interaction, leading to a harder pre-equilibrium spectrum. For the first stage the maximum depth of the hole should be significantly reduced, since in the surface region the potential is shallower than in the interior. This automatically leaves more energy to be adopted by the excited particle, yielding more emission at the highest outgoing energies. We use the following functional form for  $V$  in terms of the projectile energy  $E_p$  and the mass  $A$ ,

$$\begin{aligned} V &= 22 + 16 \frac{E_p^4}{E_p^4 + (450/A^{1/3})^4} \text{ MeV for } h = 1 \text{ and incident protons,} \\ V &= 12 + 26 \frac{E_p^4}{E_p^4 + (245/A^{1/3})^4} \text{ MeV for } h = 1 \text{ and incident neutrons,} \\ V &= E_f = 38 \text{ MeV for } h > 1. \end{aligned} \quad (4.66)$$

See Ref. [3] for a further justification of this parameterisation.

**C. Lifetimes** The lifetime  $\tau$  of exciton state  $(p_\pi, h_\pi, p_\nu, h_\nu)$  in Eq. (4.56) is defined as the inverse sum of the total emission rate and the various internal transition rates,

$$\begin{aligned} \tau(p_\pi, h_\pi, p_\nu, h_\nu) &= [\lambda_\pi^+(p_\pi, h_\pi, p_\nu, h_\nu) + \lambda_\nu^+(p_\pi, h_\pi, p_\nu, h_\nu) \\ &+ \lambda_{\pi\nu}^0(p_\pi, h_\pi, p_\nu, h_\nu) + \lambda_{\nu\pi}^0(p_\pi, h_\pi, p_\nu, h_\nu) + W(p_\pi, h_\pi, p_\nu, h_\nu)]^{-1}, \end{aligned} \quad (4.67)$$

where  $\lambda_\pi^+$  ( $\lambda_\nu^+$ ) is the internal transition rate for proton (neutron) particle-hole pair creation,  $\lambda_{\pi\nu}^0$  ( $\lambda_{\nu\pi}^0$ ) is the rate for the conversion of a proton (neutron) particle-hole pair into a neutron (proton) particle-hole pair, and  $\lambda_\pi^-$  ( $\lambda_\nu^-$ ) is the rate for particle-hole annihilation. These transition rates will be discussed in Sec. 4.4.1. The total emission rate  $W$  is the integral of Eq. (4.58) over all outgoing energies, summed over all outgoing particles,

$$W(p_\pi, h_\pi, p_\nu, h_\nu) = \sum_{k=\gamma,n,p,d,t,h,\alpha} \int dE_k W_k(p_\pi, h_\pi, p_\nu, h_\nu, E_k). \quad (4.68)$$

The final ingredient of the exciton model equation, Eq. (4.56), is the part of the pre-equilibrium population  $P$  that has survived emission from all previous steps and has arrived at the exciton state  $(p_\pi, h_\pi, p_\nu, h_\nu)$ . The expression for  $P$  is somewhat more complicated than that of the depletion factor that appears in the one-component exciton model [59]. For two components, contributions from both particle creation *and* charge exchange reactions need to be taken into account, whereas transitions that do not change the exciton number cancel out in the one-component model.

For the  $(p_\pi, h_\pi, p_\nu, h_\nu)$  state,  $P$  is given by a recursive relation:

$$\begin{aligned} P(p_\pi, h_\pi, p_\nu, h_\nu) &= P(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu) \Gamma_\pi^+(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu) & (A) \\ &+ P(p_\pi, h_\pi, p_\nu - 1, h_\nu - 1) \Gamma_\nu^+(p_\pi, h_\pi, p_\nu - 1, h_\nu - 1) & (B) \\ &+ [P(p_\pi - 2, h_\pi - 2, p_\nu + 1, h_\nu + 1) \Gamma_\pi^+(p_\pi - 2, h_\pi - 2, p_\nu + 1, h_\nu + 1) \\ &+ P(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu) \Gamma_\nu^+(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu)] \end{aligned}$$

$$\begin{aligned}
& \times \Gamma_{\nu\pi}^0(p_\pi - 1, h_\pi - 1, p_\nu + 1, h_\nu + 1) & (C + D) \\
& + [P(p_\pi, h_\pi, p_\nu - 1, h_\nu - 1)\Gamma_\pi^+(p_\pi, h_\pi, p_\nu - 1, h_\nu - 1) \\
& + P(p_\pi + 1, h_\pi + 1, p_\nu - 2, h_\nu - 2)\Gamma_\nu^+(p_\pi + 1, h_\pi + 1, p_\nu - 2, h_\nu - 2)] \\
& \times \Gamma_{\pi\nu}^0(p_\pi + 1, h_\pi + 1, p_\nu - 1, h_\nu - 1) & (E + F).
\end{aligned} \tag{4.69}$$

This relation contains 6 distinct feeding terms: (A) creation of a proton particle-hole pair from the  $(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu)$  state, (C) creation of a proton particle-hole pair from the  $(p_\pi - 2, h_\pi - 2, p_\nu + 1, h_\nu + 1)$  state followed by the conversion of a neutron particle-hole pair into a proton particle-hole pair, and (D) creation of a neutron particle-hole pair from the  $(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu)$  state followed by its conversion into a proton particle-hole pair. The three remaining terms (B), (E), and (F) are obtained by changing protons into neutrons and vice versa. The probabilities of creating new proton or neutron particle-hole pairs and for converting a proton (neutron) pair into a neutron (proton) pair are calculated as follows:

$$\begin{aligned}
\Gamma_\pi^+(p_\pi, h_\pi, p_\nu, h_\nu) &= \lambda_\pi^+(p_\pi, h_\pi, p_\nu, h_\nu)\tau(p_\pi, h_\pi, p_\nu, h_\nu), \\
\Gamma_\nu^+(p_\pi, h_\pi, p_\nu, h_\nu) &= \lambda_\nu^+(p_\pi, h_\pi, p_\nu, h_\nu)\tau(p_\pi, h_\pi, p_\nu, h_\nu), \\
\Gamma_\pi^{\prime+}(p_\pi, h_\pi, p_\nu, h_\nu) &= \lambda_\pi^+(p_\pi, h_\pi, p_\nu, h_\nu)\tau'(p_\pi, h_\pi, p_\nu, h_\nu), \\
\Gamma_\nu^{\prime+}(p_\pi, h_\pi, p_\nu, h_\nu) &= \lambda_\nu^+(p_\pi, h_\pi, p_\nu, h_\nu)\tau'(p_\pi, h_\pi, p_\nu, h_\nu), \\
\Gamma_{\pi\nu}^0(p_\pi, h_\pi, p_\nu, h_\nu) &= \lambda_{\pi\nu}^0(p_\pi, h_\pi, p_\nu, h_\nu)\tau(p_\pi, h_\pi, p_\nu, h_\nu), \\
\Gamma_{\nu\pi}^0(p_\pi, h_\pi, p_\nu, h_\nu) &= \lambda_{\nu\pi}^0(p_\pi, h_\pi, p_\nu, h_\nu)\tau(p_\pi, h_\pi, p_\nu, h_\nu), \\
\tau'(p_\pi, h_\pi, p_\nu, h_\nu) &= [\lambda_\pi^+(p_\pi, h_\pi, p_\nu, h_\nu) + \lambda_\nu^+(p_\pi, h_\pi, p_\nu, h_\nu) \\
&+ W(p_\pi, h_\pi, p_\nu, h_\nu)]^{-1}.
\end{aligned} \tag{4.70}$$

The use of  $\tau'$  in the probability  $\Gamma_\pi^{\prime+}$  ( $\Gamma_\nu^{\prime+}$ ), to create a new proton (neutron) particle-hole pair preceding an exchange interaction, originates from the approximation that only one exchange interaction is allowed in each pair-creation step. The appropriate lifetime in this case consists merely of pair creation and emission rates [60].

The initial condition for the recursive equations is

$$P(p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0) = 1, \tag{4.71}$$

after which  $P$  can be solved for any configuration.

To calculate the pre-equilibrium spectrum, the only quantities left to determine are the internal transition rates  $\lambda_\pi^+$ ,  $\lambda_\nu^+$ ,  $\lambda_{\pi\nu}^0$  and  $\lambda_{\nu\pi}^0$ .

**D. Internal transition rates** The transition rate  $\lambda_\pi^+$  for the creation of a proton particle-hole pair is given by four terms, accounting for  $p_\pi$ ,  $h_\pi$ ,  $p_\nu$  and  $h_\nu$  scattering that leads to a new  $(p_\pi, h_\pi)$  pair,

$$\begin{aligned}
\lambda_\pi^+(p_\pi, h_\pi, p_\nu, h_\nu) &= \frac{1}{\omega(p_\pi, h_\pi, p_\nu, h_\nu, E^{\text{tot}})} \\
[ & \int_{L_1^{p_\pi}}^{L_2^{p_\pi}} \lambda_{\pi\pi}^{1p}(u)\omega(p_\pi - 1, h_\pi, p_\nu, h_\nu, E^{\text{tot}} - u)\omega(1, 0, 0, 0, u)du
\end{aligned}$$

$$\begin{aligned}
& + \int_{L_1^{h\pi}}^{L_2^{h\pi}} \lambda_{\pi\pi}^{1h}(u) \omega(p_\pi, h_\pi - 1, p_\nu, h_\nu, E^{\text{tot}} - u) \omega(0, 1, 0, 0, u) du \\
& + \int_{L_1^{p\nu}}^{L_2^{p\nu}} \lambda_{\nu\pi}^{1p}(u) \omega(p_\pi, h_\pi, p_\nu - 1, h_\nu, E^{\text{tot}} - u) \omega(0, 0, 1, 0, u) du \\
& + \int_{L_1^{h\nu}}^{L_2^{h\nu}} \lambda_{\nu\pi}^{1h}(u) \omega(p_\pi, h_\pi, p_\nu, h_\nu - 1, E^{\text{tot}} - u) \omega(0, 0, 0, 1, u) du], \tag{4.72}
\end{aligned}$$

where the first and third term represent particle scattering and the second and fourth term hole scattering. The integration limits correct for the Pauli exclusion principle,

$$\begin{aligned}
L_1^{p\pi} &= A(p_\pi + 1, h_\pi + 1, p_\nu, h_\nu) - A(p_\pi - 1, h_\pi, p_\nu, h_\nu), \\
L_2^{p\pi} &= E^{\text{tot}} - A(p_\pi - 1, h_\pi, p_\nu, h_\nu), \\
L_1^{h\pi} &= A(p_\pi + 1, h_\pi + 1, p_\nu, h_\nu) - A(p_\pi, h_\pi - 1, p_\nu, h_\nu), \\
L_2^{h\pi} &= E^{\text{tot}} - A(p_\pi, h_\pi - 1, p_\nu, h_\nu), \\
L_1^{p\nu} &= A(p_\pi, h_\pi, p_\nu + 1, h_\nu + 1) - A(p_\pi, h_\pi, p_\nu - 1, h_\nu), \\
L_2^{p\nu} &= E^{\text{tot}} - A(p_\pi, h_\pi, p_\nu - 1, h_\nu), \\
L_1^{h\nu} &= A(p_\pi + 1, h_\pi + 1, p_\nu, h_\nu) - A(p_\pi, h_\pi, p_\nu, h_\nu - 1), \\
L_2^{h\nu} &= E^{\text{tot}} - A(p_\pi, h_\pi, p_\nu, h_\nu - 1), \tag{4.73}
\end{aligned}$$

which demands that (a) the minimal energy available to the scattering particle or hole creating a new particle-hole pair equals the Pauli energy of the final state minus the Pauli energy of the inactive particles and holes not involved in the scattering process, and (b) the maximal energy available equals the total excitation energy minus the latter Pauli energy.

The term  $\lambda_{\pi\pi}^{1p}(u)$  is the collision probability per unit time for a proton-proton interaction leading to an additional proton particle-hole pair. In general, the corresponding term for a hole is obtained by relating it to the particle collision probability through the accessible state density of the interacting particles and holes,

$$\lambda_{\pi\pi}^{1h}(u) = \lambda_{\pi\pi}^{1p}(u) \frac{\omega(1, 2, 0, 0, u)}{\omega(2, 1, 0, 0, u)}. \tag{4.74}$$

Similarly,  $\lambda_{\nu\pi}^{1p}(u)$  is the collision probability per unit time for a neutron-proton interaction leading to an additional proton particle-hole pair, and for the corresponding hole term we have

$$\lambda_{\nu\pi}^{1h}(u) = \lambda_{\nu\pi}^{1p}(u) \frac{\omega(1, 1, 0, 1, u)}{\omega(1, 1, 1, 0, u)}. \tag{4.75}$$

The transition rate for conversion of a proton particle-hole pair into a neutron pair is

$$\begin{aligned}
\lambda_{\pi\nu}^0(p_\pi, h_\pi, p_\nu, h_\nu) &= \frac{1}{\omega(p_\pi, h_\pi, p_\nu, h_\nu, E^{\text{tot}})} \int_{L_1^{p\pi}}^{L_2^{p\pi}} \lambda_{\nu\pi}^{1p1h}(u) \\
&\quad \omega(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu, E^{\text{tot}} - u) \omega(1, 1, 0, 0, u) du, \tag{4.76}
\end{aligned}$$

with integration limits

$$\begin{aligned}
L_1^{p\pi} &= A(p_\pi, h_\pi, p_\nu, h_\nu) - A(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu) \\
L_2^{p\pi} &= E^{\text{tot}} - A(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu). \tag{4.77}
\end{aligned}$$

The term  $\lambda_{\pi\nu}^{1p1h}$  is the associated collision probability. Interchanging  $\pi$  and  $\nu$  in Eqs. (4.72-4.77) gives the expressions for  $\lambda_{\nu}^+$ ,  $\lambda_{\nu\nu}^{1h}$ ,  $\lambda_{\pi\nu}^{1h}$  and  $\lambda_{\nu\pi}^0$ .

We distinguish between two options for the collision probabilities:

#### D1. Effective squared matrix element

Expressing the transition rate in terms of an effective squared matrix element has been used in many exciton model analyses. Also in TALYS, it is one of the options for our calculations and comparisons with data. The collision probabilities of Eqs. (4.72) and (4.76) are determined with the aid of Fermi's golden rule of time-dependent perturbation theory, which for a two-component model gives

$$\begin{aligned}
 \lambda_{\pi\pi}^{1p}(u) &= \frac{2\pi}{\hbar} M_{\pi\pi}^2 \omega(2, 1, 0, 0, u), \\
 \lambda_{\pi\pi}^{1h}(u) &= \frac{2\pi}{\hbar} M_{\pi\pi}^2 \omega(1, 2, 0, 0, u), \\
 \lambda_{\nu\pi}^{1p}(u) &= \frac{2\pi}{\hbar} M_{\nu\pi}^2 \omega(1, 1, 1, 0, u), \\
 \lambda_{\nu\pi}^{1h}(u) &= \frac{2\pi}{\hbar} M_{\nu\pi}^2 \omega(1, 1, 0, 1, u), \\
 \lambda_{\pi\nu}^{1p1h}(u) &= \frac{2\pi}{\hbar} M_{\pi\nu}^2 \omega(0, 0, 1, 1, u),
 \end{aligned} \tag{4.78}$$

where the relations (4.74)-(4.75) have been applied. Interchanging  $\pi$  and  $\nu$  gives the expressions for  $\lambda_{\nu\nu}^{1p}$ ,  $\lambda_{\nu\nu}^{1h}$ ,  $\lambda_{\pi\nu}^{1p}$ ,  $\lambda_{\pi\nu}^{1h}$ , and  $\lambda_{\nu\pi}^{1p1h}$ . Here, the  $M_{\pi\pi}^2$ , etc. are average squared matrix elements of the residual interaction, which are assumed to depend on the total energy  $E^{\text{tot}}$  of the whole composite nucleus only. Such a matrix element thus represents a truly *effective* residual interaction, whereby all individual residual interactions taking place inside the nucleus can be cast into an average form for the squared matrix element to which one assigns a global  $E^{\text{tot}}$ -dependence a posteriori.

The average residual interaction inside the nucleus is not necessarily the same for like and unlike nucleons. The two-component matrix elements are given, in terms of an average  $M^2$ , by

$$\begin{aligned}
 M_{\nu\nu}^2 &= M_{\pi\pi}^2 = M^2, \\
 M_{\pi\nu}^2 &= M_{\nu\pi}^2 = R_{\pi\nu} M^2.
 \end{aligned} \tag{4.79}$$

In TALYS, we take

$$R_{\pi\nu} = 1.5, \tag{4.80}$$

which is in line with the, more parameter-free, optical model based exciton model that we describe later. In TALYS,  $R_{\pi\nu}$  is adjustable (**Rpinu** keyword) with Eq. (4.80) as default. The following semi-empirical expression for the squared matrix element has been shown to work for incident energies between 7 and 200 MeV [3]:

$$M^2 = \frac{C_1}{A^3} \left[ 6.8C_2 + \frac{4.2 \times 10^5}{\left(\frac{E^{\text{tot}}}{n} + 10.7C_3\right)^3} \right]. \tag{4.81}$$

Eq. (4.81) is a generalization of older parameterisations such as given in Refs. [60, 52], which apply in smaller (lower) energy ranges. Here  $C_1$ ,  $C_2$  and  $C_3$  are adjustable constants (see the **M2constant**, **M2limit** and **M2shift** keywords) that are all equal to 1 by default.

Finally, for matrix element based transition rates and equidistant particle-hole level densities, the integrals in the transition rates can be approximated analytically [60], giving

$$\begin{aligned}
\lambda_{\pi+}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}) &= \frac{2\pi}{\hbar} \frac{g_{\pi}^2}{2n(n+1)} \frac{[E^{tot} - A(p_{\pi} + 1, h_{\pi} + 1, p_{\nu}, h_{\nu})]^{n+1}}{[E^{tot} - A(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu})]^{n-1}} \\
&\times (n_{\pi} g_{\pi} M_{\pi\pi}^2 + 2n_{\nu} g_{\nu} M_{\pi\nu}^2) f(p+1, h+1, E^{tot}, V) \\
\lambda_{\nu+}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}) &= \frac{2\pi}{\hbar} \frac{g_{\nu}^2}{2n(n+1)} \frac{[E^{tot} - A(p_{\pi}, h_{\pi}, p_{\nu} + 1, h_{\nu} + 1)]^{n+1}}{[E^{tot} - A(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu})]^{n-1}} \\
&\times (n_{\nu} g_{\nu} M_{\nu\nu}^2 + 2n_{\pi} g_{\pi} M_{\nu\pi}^2) f(p+1, h+1, E^{tot}, V) \\
\lambda_{\pi\nu}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}) &= \frac{2\pi}{\hbar} M_{\pi\nu}^2 \frac{p_{\pi} h_{\pi}}{n} g_{\nu}^2 f(p, h, E^{tot}, V) \left[ \frac{E^{tot} - B_{\pi\nu}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu})}{E^{tot} - A(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu})} \right]^{n-1} \\
&\times (2[E^{tot} - B_{\pi\nu}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu})] \\
&+ n|A(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}) - A(p_{\pi} - 1, h_{\pi} - 1, p_{\nu} + 1, h_{\nu} + 1)|) \\
\lambda_{\nu\pi}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}) &= \frac{2\pi}{\hbar} M_{\nu\pi}^2 \frac{p_{\nu} h_{\nu}}{n} g_{\pi}^2 f(p, h, E^{tot}, V) \left[ \frac{E^{tot} - B_{\nu\pi}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu})}{E^{tot} - A(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu})} \right]^{n-1} \\
&\times (2[E^{tot} - B_{\nu\pi}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu})] \\
&+ n|A(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}) - A(p_{\pi} + 1, h_{\pi} + 1, p_{\nu} - 1, h_{\nu} - 1)|), \quad (4.82)
\end{aligned}$$

with

$$\begin{aligned}
B_{\pi\nu}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}) &= \max[A(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}), A(p_{\pi} - 1, h_{\pi} - 1, p_{\nu} + 1, h_{\nu} + 1)] \\
B_{\nu\pi}(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}) &= \max[A(p_{\pi}, h_{\pi}, p_{\nu}, h_{\nu}), A(p_{\pi} + 1, h_{\pi} + 1, p_{\nu} - 1, h_{\nu} - 1)]. \quad (4.83)
\end{aligned}$$

which is also included as an option. The default is however to use the numerical solutions for the internal transition rates. This analytical solution requires a value for  $M^2$  that is 20% larger than that of Eq. (4.81), which apparently is the energy-averaged effect of introducing such approximations.

## D2. Collision rates based on the optical model

Instead of modeling the intranuclear transition rate by an average squared matrix element, one may also relate the transition rate to the average imaginary optical model potential depth [3]. The collision probabilities, when properly averaged over all particle-hole configurations as in Eq. (4.72), in principle would yield a parameter free expression for the transition rate.

The average well depth  $W_i$  can be obtained by averaging the total imaginary part of the potential  $\mathcal{W}$  over the whole volume of the nucleus

$$W_i(E) = \frac{\int \mathcal{W}_i(r, E) \rho(r) dr}{\int \rho(r) dr}, \quad (4.84)$$

where  $\rho$  represents the density of nuclear matter for which we take the form factor  $f(r, R, a)$  of the volume part of the optical model potential, given by the usual Woods-Saxon shape of Eq. (4.3). The total imaginary potential is given by

$$\mathcal{W}_i(r, E) = \mathcal{W}_{V,i}(E) f(r, R_{V,i}, a_{V,i}) - 4a_{D,i} \mathcal{W}_{D,i}(E) \frac{d}{dr} f(r, R_{D,i}, a_{D,i}). \quad (4.85)$$

Next, we define an *effective* imaginary optical potential [3] related to nucleon-nucleon collisions in nuclear matter:

$$W_i^{\text{eff}}(E) = C^{\text{omp}} W_i(E). \quad (4.86)$$

We use as best overall parameter

$$C^{\text{omp}} = 0.55. \quad (4.87)$$

This parameter can be adjusted with the **M2constant** keyword, which serves as a multiplier for the value given in Eq. (4.87). The collision probabilities are now related as follows to the *effective* imaginary optical potential:

$$\begin{aligned} \lambda_{\pi\pi}^{1p}(u) &= \frac{1}{4} \frac{2W_p^{\text{eff}}(u - S(p))}{\hbar} \\ \lambda_{\pi\pi}^{1h}(u) &= \frac{1}{4} \frac{2W_p^{\text{eff}}(u - S(p))}{\hbar} \frac{\omega(1, 2, 0, 0, u)}{\omega(2, 1, 0, 0, u)} \\ \lambda_{\nu\pi}^{1p}(u) &= \frac{3}{4} \frac{2W_n^{\text{eff}}(u - S(n))}{\hbar} \\ \lambda_{\nu\pi}^{1h}(u) &= \frac{3}{4} \frac{2W_n^{\text{eff}}(u - S(n))}{\hbar} \frac{\omega(1, 1, 0, 1, u)}{\omega(1, 1, 1, 0, u)} \\ \lambda_{\nu\pi}^{1p1h}(u) &= \frac{1}{2} \frac{2W_n^{\text{eff}}(u - S(n))}{\hbar}, \end{aligned} \quad (4.88)$$

and similarly for the components of  $\lambda_{\nu}^{+}$  and  $\lambda_{\nu\pi}^{0}$ . The transition rates for the exciton model are then obtained by inserting these terms in Eqs. (4.72) and (4.76). Apart from Eq. (4.87), a parameter-free model is obtained.

### One-component exciton model

The one-component exciton model has been made redundant by the more flexible and physically more justified two-component model. Nevertheless, it is included as an option since it connects to many older pre-equilibrium studies and thus may be helpful as comparison. In the one-component exciton model, the pre-equilibrium spectrum for the emission of a particle  $k$  at an energy  $E_k$  is given by

$$\frac{d\sigma_k^{\text{PE}}}{dE_k} = \sigma^{\text{CF}} \sum_{p=p_0}^{p_{\text{max}}} W_k(p, h, E_k) \tau(p, h), \quad (4.89)$$

where  $p_{\text{max}} = 6$  and  $\sigma^{\text{CF}}$  are defined as below Eq. (4.56). For the initial particle number  $p_0$  we have  $p_0 = A_p$  with  $A_p$  the mass number of the projectile. In general, the hole number  $h = p - p_0$  in Eq. (4.89), so that the initial hole number is always zero, i.e.  $h_0 = 0$  for primary pre-equilibrium emission.

The emission rate  $W_k$  is

$$W_k(p, h, E_k) = \frac{2s_k + 1}{\pi^2 \hbar^3} \mu_k E_k \sigma_{k,\text{inv}}(E_k) \frac{\omega(p - A_k, h, E_{\text{tot}} - E_k)}{\omega(p, h, E_{\text{tot}})} Q_k(p), \quad (4.90)$$

with all quantities explained below Eq. (4.58), and  $A_k$  is the mass number of the ejectile and  $Q_k(p)$  is a factor accounting for the distinguishability of neutrons and protons [66]

$$Q_k(p) = \frac{(p - A_k)!}{p!} \left[ \sum_{p_\pi = Z_k}^{p - N_k} \left(\frac{Z}{A}\right)^{n_\pi - Z_k} \left(\frac{A}{N}\right)^{n_\nu - N_k} \frac{1}{h_\pi! h_\nu!} \frac{1}{(p_\pi - Z_k)! (p_\nu - N_k)!} \right] / \left[ \sum_{p_\pi = Z_k}^{p - N_k} \left(\frac{Z}{A}\right)^{n_\pi} \left(\frac{N}{A}\right)^{n_\nu} \frac{1}{p_\pi! p_\nu! h_\pi! h_\nu!} \right]. \quad (4.91)$$

For gamma's we set  $Q_\gamma(p) = 1$ .

Finally,  $\omega(p, h, E_x)$  is the particle-hole state density for which we use the one-component expression by Běták and Dobeš [63], again corrected for the effect of the Pauli exclusion principle and for the finite depth of the potential well. The one-component particle-hole state density has a simpler form than that of Eq. (4.59),

$$\omega(p, h, E_x) = \frac{g^n}{p! h! (n-1)!} [E_x - A(p, h)]^{n-1} f(p, h, E_x, V), \quad (4.92)$$

where  $g = A/15$  is the single-particle state density and

$$A(p, h) = \frac{[\max(p, h)]^2}{g} - \frac{p^2 + h^2 + p + h}{4g}, \quad (4.93)$$

is the Pauli correction factor. The finite well function  $f$  is given by Eq. (4.65).

To obtain the lifetimes  $\tau(p, h)$  that appear in Eq. (4.89), we first define the total emission rate  $W(p, h)$  as the integral of Eq. (4.90) over all outgoing energies, summed over all outgoing particles:

$$W(p, h) = \sum_{k=\gamma, n, p, d, t, h, \alpha} \int dE_k W_k(p, h, E_k). \quad (4.94)$$

As mentioned already, we have implemented the never-come-back solution of the master equation. This is based on the assumption that at the beginning of the cascade one neglects the interactions that decrease the exciton number. Then, for the one-component model the expression for the lifetime is (see e.g. Ref. [59])

$$\tau(p, h) = \frac{1}{\lambda^+(p, h) + W(p, h)} D_{p, h}, \quad (4.95)$$

where  $D_{p, h}$  is a depletion factor that accounts for the removal of reaction flux, through emission, by the previous stages

$$D_{p, h} = \prod_{p'=p_0}^{p-1} \frac{\lambda^+(p', h')}{\lambda^+(p', h') + W(p', h')}, \quad (4.96)$$

with again  $h' = p' - p_0$ . The initial case of Eq. (4.95) is

$$\tau(p_0, h_0) = \frac{1}{\lambda^+(p_0, h_0) + W(p_0, h_0)}. \quad (4.97)$$

To calculate the pre-equilibrium spectrum, the only quantity left to determine is the internal transition rate  $\lambda^+(p, h)$  from state  $(p, h)$  to state  $(p + 1, h + 1)$ . The general definition of  $\lambda^+(p, h)$  is

$$\begin{aligned} \lambda^+(p, h) &= \frac{1}{\omega(p, h, E^{\text{tot}})} \left[ \int_{L_1^p}^{L_2^p} du \lambda^{1p}(u) \omega(p-1, h, E^{\text{tot}} - u) \omega(1, 0, u) \right. \\ &\quad \left. + \int_{L_1^h}^{L_2^h} du \lambda^{1h}(u) \omega(p, h-1, E^{\text{tot}} - u) \omega(0, 1, u) \right]. \end{aligned} \quad (4.98)$$

where the two terms account for particle and hole scattering, respectively, and the integration limits

$$\begin{aligned} L_1^p &= A(p+1, h+1) - A(p-1, h) \\ L_2^p &= E^{\text{tot}} - A(p-1, h) \\ L_1^h &= A(p+1, h+1) - A(p, h-1) \\ L_2^h &= E^{\text{tot}} - A(p, h-1), \end{aligned} \quad (4.99)$$

correct for the Pauli exclusion principle.

We again distinguish between two options:

#### 1. Effective squared matrix element

The collision probabilities are determined with the aid of Fermi's golden rule of time-dependent perturbation theory, which for the one-component model are

$$\begin{aligned} \lambda^{1p}(u) &= \frac{2\pi}{\hbar} M^2 \omega(2, 1, u) \\ \lambda^{1h}(u) &= \frac{2\pi}{\hbar} M^2 \omega(1, 2, u), \end{aligned} \quad (4.100)$$

with  $M^2$  the average squared matrix element of the residual interaction. In the one-component model, "forbidden" transitions are taken into account, so that a squared matrix element smaller than that of Eq. (4.81) of the two-component model is needed to compensate for these transitions. We find that for the one-component model we need to multiply  $M^2$  of Eq. (4.81) by 0.5 to obtain a global comparison with data that is closest to our two-component result, i.e.

$$M^2 = \frac{0.5C_1}{A^3} \left[ 6.8C_2 + \frac{4.2 \times 10^5}{\left(\frac{E^{\text{tot}}}{n} + 10.7C_3\right)^3} \right]. \quad (4.101)$$

For completeness, we note that the transition rate can be well approximated by an analytical form as discussed in Refs. [67, 63, 65]. The result is

$$\lambda^+(p, h) = \frac{2\pi}{\hbar} M^2 \frac{g^3}{2(n+1)} \frac{[E^{\text{tot}} - A(p+1, h+1)]^{n+1}}{[E^{\text{tot}} - A(p, h)]^{n-1}} f(p+1, h+1, E^{\text{tot}}, V). \quad (4.102)$$

However, the overall description of experimental data obtained with the one-component model is however worse than that of the two-component model, so we rarely use it.

## 2. Collision rates based on the optical model

Also in the one-component model the transition rates can be related to the effective nucleon-nucleon interaction  $\bar{\sigma}$  and thereby to the imaginary optical potential,

$$\begin{aligned}\lambda^{1p}(u) &= \frac{1}{2} \frac{2W^{\text{eff}}(u-S)}{\hbar} \\ \lambda^{1h}(u) &= \frac{1}{2} \frac{2W^{\text{eff}}(u-S)}{\hbar} \frac{\omega(1,2,u)}{\omega(2,1,u)},\end{aligned}\quad (4.103)$$

with  $S$  the separation energy of the particle. Since the one-component model makes no distinction between neutron and proton particle-hole pairs,  $W_V^{\text{eff}}$  is evaluated as follows,

$$W_i^{\text{eff}}(E) = 0.5C^{\text{omp}} W_i(E), \quad (4.104)$$

analogous to the multiplication with a factor 0.5 for  $M^2$ .

**Energy width representation** The formalism given above, i.e. Eqs. (4.89), (4.90) and (4.95), forms a representation in which the time appears, i.e. the dimensions of  $W(p, h)$  and  $\tau(p, h)$  are  $[s]^{-1}$  and  $[s]$  respectively. An alternative expression for the exciton model that is often used is in terms of energy widths. Since this may be more recognisable to some users we also give it here. The partial escape width  $\Gamma_k^\uparrow(p, h, E_k)$  is related to the emission rate by

$$\Gamma_k^\uparrow(p, h, E_k) = \hbar W_k(p, h, E_k). \quad (4.105)$$

Integrated over energy we have

$$\Gamma_k^\uparrow(p, h) = \hbar W_k(p, h), \quad (4.106)$$

and the total escape width is

$$\Gamma^\uparrow(p, h) = \sum_{k=\gamma, n, p, d, t, h, \alpha} \Gamma_k^\uparrow(p, h) = \hbar W(p, h). \quad (4.107)$$

The damping width  $\Gamma^\downarrow$  is related to the internal transition rate by

$$\Gamma^\downarrow(p, h) = \hbar \lambda^+(p, h). \quad (4.108)$$

Defining the total width by

$$\Gamma^{\text{tot}}(p, h) = \Gamma^\downarrow(p, h) + \Gamma^\uparrow(p, h), \quad (4.109)$$

we can rewrite the exciton model cross section (4.89) as

$$\frac{d\sigma_k^{\text{PE}}}{dE_k} = \sigma_{\text{CF}} \sum_{p=p_0}^{p_{\text{max}}} \frac{\Gamma_k^\uparrow(p, h, E_k)}{\Gamma^{\text{tot}}(p, h)} \left( \prod_{p'=p_0}^{p-1} \frac{\Gamma^\downarrow(p', h')}{\Gamma^{\text{tot}}(p', h')} \right). \quad (4.110)$$

In the output file of TALYS, the results for the various quantities in both the time and the energy width representation are given.

In sum, the default model used by TALYS is the two-component exciton model with collision probabilities based on the effective squared matrix element of Eq. (4.81).

### 4.4.2 Photon exciton model

For pre-equilibrium photon emission, we have implemented the model of Akkermans and Gruppelaar [68]. This model gives a simple but powerful simulation of the direct-semidirect capture process within the framework of the exciton model. Analogous to the particle emission rates, the continuum  $\gamma$ -ray emission rates may be derived from the principle of detailed balance or microscopic reversibility, assuming that only  $E1$ -transitions contribute. This yields

$$W_\gamma(p, h, E_\gamma) = \frac{E_\gamma^2}{\pi^2 \hbar^3 c^2} \frac{\sigma_{\gamma,abs}(E_\gamma)}{\omega(p, h, E^{tot})} \left( \frac{g^2 E_\gamma \omega(p-1, h-1, E_x - E_\gamma)}{g(n-2) + g^2 E_\gamma} + \frac{gn\omega(p, h, E_x - E_\gamma)}{gn + g^2 E_\gamma} \right) \quad (4.111)$$

where  $\sigma_{\gamma,abs}(E_\gamma)$  is the photon absorption cross section of Eq. (4.49). The initial particle-hole configuration in Eq. (4.89) is  $n_0 = 1$  ( $1p0h$ ) for photon emission. For “direct”  $\gamma$ -ray emission in nucleon-induced reactions only the second term between brackets ( $n = 1$ ) contributes. The “semi-direct”  $\gamma$ -ray emission ( $n = 3$ ) consists of both terms.

The emission rate (4.111) is included in Eqs. (4.89) and (4.94) so that the pre-equilibrium photon cross section automatically emerges.

For the two-component model, we use

$$\begin{aligned} W_\gamma(p_\pi, h_\pi, p_\nu, h_\nu, E_\gamma) &= \frac{E_\gamma^2}{\pi^2 \hbar^3 c^2} \frac{\sigma_{\gamma,abs}(E_\gamma)}{\omega(p_\pi, h_\pi, p_\nu, h_\nu, E^{tot})} \\ &\times \left( \frac{g^2 E_\gamma \frac{1}{2} [\omega(p_\pi - 1, h_\pi - 1, p_\nu, h_\nu, E_x - E_\gamma) + \omega(p_\pi, h_\pi, p_\nu - 1, h_\nu - 1, E_x - E_\gamma)]}{g(n-2) + g^2 E_\gamma} \right. \\ &\left. + \frac{gn\omega(p_\pi, h_\pi, p_\nu, h_\nu, E_x - E_\gamma)}{gn + g^2 E_\gamma} \right). \end{aligned} \quad (4.112)$$

### 4.4.3 Pre-equilibrium spin distribution

Since the exciton model described above does not provide a spin distribution for the residual states after pre-equilibrium emission, a model needs to be adopted that provides the spin population in the continuum in binary reactions. TALYS provides two options for this. The default is to adopt the compound nucleus spin distribution (described in Section 4.5) also for the excited states resulting from pre-equilibrium emission. Another option that has been quite often used in the past is to assign a spin distribution to the particle-hole state density. For that, we adopt the usual decomposition of the state density into a  $J$ -dependent part and an energy-dependent part,

$$\rho(p, h, J, E_x) = (2J + 1)R_n(J)\omega(p, h, E_x). \quad (4.113)$$

The function  $R_n(J)$  represents the spin distribution of the states in the continuum. It is given by

$$R_n(J) = \frac{2J + 1}{\pi^{1/2} n^{3/2} \sigma^3} \exp \left[ -\frac{(J + \frac{1}{2})^2}{n\sigma^2} \right], \quad (4.114)$$

and satisfies, for any exciton number  $n$ ,

$$\sum_J (2J + 1)R_n(J) = 1. \quad (4.115)$$

The used expression for the spin cutoff factor  $\sigma$  is [69],

$$\sigma^2 = 0.24nA^{\frac{2}{3}}, \quad (4.116)$$

where  $A$  is the mass number of the nucleus. Similarly, for the two-component particle-hole level density we have

$$\rho(p_\pi, h_\pi, p_\nu, h_\nu, J, E_x) = (2J + 1)R_n(J)\omega(p_\pi, h_\pi, p_\nu, h_\nu, E_x). \quad (4.117)$$

In practice, with this option (**preeqspin y**) the residual states formed by pre-equilibrium reactions would be multiplied by  $R_n$  a posteriori. There are various arguments to prefer the compound nucleus spin distribution, so we use that default.

#### 4.4.4 Continuum stripping, pick-up and knock-out reactions

For pre-equilibrium reactions involving deuterons, tritons, Helium-3 and alpha particles, a contribution from the exciton model is automatically calculated with the formalism of the previous subsections. It is however well-known that for nuclear reactions involving projectiles and ejectiles with different particle numbers, mechanisms like stripping, pick-up and knock-out play an important role and these direct-like reactions are not covered by the exciton model. Therefore, Kalbach [70] developed a phenomenological contribution for these mechanisms, which we have included in TALYS. In total, the pre-equilibrium cross section for these reactions is given by the sum of an exciton model (EM), nucleon transfer (NT), and knock-out (KO) contribution:

$$\frac{d\sigma_k^{\text{PE}}}{dE_k} = \frac{d\sigma_k^{\text{EM}}}{dE_k} + \frac{d\sigma_k^{\text{NT}}}{dE_k} + \frac{d\sigma_k^{\text{KO}}}{dE_k} \quad (4.118)$$

where the contribution from the exciton model was outlined in the previous subsection.

#### Transfer reactions

The general differential cross section formula for a nucleon transfer reaction of the type  $A(a, b)B$  is

$$\begin{aligned} \frac{d\sigma_{a,b}^{\text{NT}}}{dE_b} &= \frac{2s_b + 1}{2s_a + 1} \frac{A_b}{A_a} \frac{E_b \sigma_{b,inv}(E_b)}{A_a E_a} K \left( \frac{A_a}{E_a + V_a} \right)^{2n} \left( \frac{C}{A_B} \right)^n \\ &\times 0.0127 \left( \frac{2Z_A}{A_A} \right)^{6h_\pi} \omega_{\text{NT}}(p_\pi, h_\pi, p_\nu, h_\nu, U) \end{aligned} \quad (4.119)$$

where  $C = 6500$  for incident neutrons and  $C = 3800$  otherwise.  $K$  is an enhancement factor taking into account the fact that d, t and 3-He are loosely bound:  $K = 12$  for  $(\alpha, \text{nucleon})$  or  $(\text{nucleon}, \alpha)$  reactions and  $K = 1$  otherwise. This  $K$  parameter is currently under investigation. The well depth  $V_a$  is set at  $V_a = 12.5A_a$  MeV, representing the average potential drop seen by the projectile between infinity and the Fermi level. The possible degrees of freedom for the reaction are all included in the residual state density  $\omega_{\text{NT}}(p_\pi, h_\pi, p_\nu, h_\nu, U)$ . Since we do not use this model to describe exchange reactions in inelastic scattering, there is no need to sum the various terms of Eq. (4.119) over  $p_\pi$ , as in Ref. [70]. The exciton numbers are automatically determined by the transfer reaction, i.e.  $n = |A_a - A_b|$ ,  $n_\pi = h_\pi = |Z_a - Z_b|$ ,  $n_\nu = h_\nu = |N_a - N_b|$ ,  $p_\pi = p_\nu = 0$ . The accessible state density that is directly determined by the

reaction is  $\omega(p_\pi, h_\pi, p_\nu, h_\nu, U)$ , given by Eq. (4.59). The total residual state density however also takes into account more complex configurations that can be excited by the transfer reaction. It is given by

$$\begin{aligned} \omega_{NT}(p_\pi, h_\pi, p_\nu, h_\nu, U) &= \sum_{i=0}^3 \sum_{j=0}^{3-i} (X_{NT})^{i+j} \omega(p_\pi + i, h_\pi + i, p_\nu + j, h_\nu + j, U) \\ &+ \sum_{i=0}^{p_\pi} \sum_{j=0}^{h_\pi} \sum_{k=0}^{p_\nu} \sum_{l=0}^{h_\nu} \omega(p_\pi - i, h_\pi - j, p_\nu - k, h_\nu - l, U) \Theta(i + j + k + l - \frac{1}{2}) \end{aligned} \quad (4.120)$$

The first term allows that up to three particle-hole pairs can be excited in a transfer reaction. The factor  $X_{NT}$  represents the probability for exciting such a pair and is given by

$$X_{NT} = \frac{7\sqrt{E_a/A_a}}{V_{well} A_A^2} (p_\nu^2 + p_\pi^2 + h_\nu^2 + 1.5h_\pi^2) \quad (4.121)$$

where we have used an ad hoc incident energy ( $E_{in}$ ) dependent well depth to prevent divergence of the production cross section at energies above 100 MeV,

$$V_{well} = v_1 + (38. - v_1) \frac{E_{in}^4}{E_{in}^4 + 150^4} \quad (4.122)$$

with  $v_1 = 7$  MeV for incident neutrons,  $v_1 = 17$  MeV for incident protons, deuterons and tritons and  $v_1 = 25$  MeV for incident Helium-3 and alpha-particles. The second term of Eq. (4.120) allows for transfer of nucleons at the Fermi level. Here, the Heaviside function is merely used to avoid double counting of  $\omega(p_\pi, h_\pi, p_\nu, h_\nu, U)$ . For the particle-hole state densities, a finite well depth of 12.5 MeV is used.

### Knockout reactions

For (*nucleon*,  $\alpha$ ) reactions a knockout contribution is added. The general differential cross section formula for a knockout reaction of the type  $A(a, b)B$  is

$$\begin{aligned} \frac{d\sigma_{a,b}^{KO}}{dE_b} &= \frac{\sigma_{a,inv}(E_a)}{12} (2s_b + 1) A_b E_b \sigma_{b,inv}(E_b) \\ &\times \frac{P_b g_a g_b [U - A_{KO}(p_a, h_b)]}{\sum_{c=a,b} (2s_c + 1) A_c \langle \sigma_c \rangle (E_{max} + 2B_{coul,c})(E_{max} - B_{coul,c})^2 g_a g_b^2 / 6g_c} \end{aligned} \quad (4.123)$$

where  $P_b$  is the probability of exciting a  $b$ -type particle-hole pair,  $E_{max}$  is the maximum emission energy, and  $B_{coul,c}$  is the Coulomb barrier for a particle  $c$ . The average inverse cross section  $\langle \sigma_c \rangle$  is given by

$$\langle \sigma_c \rangle = \int_{B_{coul,c}}^{E_{max}} dE \sigma_c(E) \quad (4.124)$$

For the knockout model, the single-particle state density parameters for the cluster degrees of freedom  $g$  represent the number of cluster states per unit energy. The relevant values are given by

$$g_n = N/13, \quad g_p = Z/13, \quad g_\alpha = A/208 \text{ MeV}. \quad (4.125)$$

The Pauli correction factor  $A_{KO}$  is given by

$$A_{KO}(p_a, h_b) = \frac{1}{2g_a^2} - \frac{1}{2g_b^2} \quad (4.126)$$

The probabilities for exciting the various particle-hole pairs are

$$\begin{aligned} P_n &= \frac{N_A - \phi Z_A}{A_A - 2\phi Z_A + \phi Z_A/2} \\ P_p &= \frac{Z_A - \phi Z_A}{A_A - 2\phi Z_A + \phi Z_A/2} \\ P_\alpha &= \frac{\phi Z_A/2}{A_A - 2\phi Z_A + \phi Z_A/2} \end{aligned} \quad (4.127)$$

The factors  $\phi$  are a kind of pre-formation parameters  $\tilde{\text{itekal01}}$ . The following values are adopted

$$\begin{aligned} N_A \leq 116 & : \phi = 0.08 \\ 116 \leq N_A < 126 & : \phi = 0.02 + 0.06(126 - N_A)/10 \\ 126 \leq N_A < 129 & : \phi = 0.02 + 0.06(N_A - 126)/3 \\ 129 \leq N_A & : \phi = 0.08 \end{aligned} \quad (4.128)$$

Finally, we mention that this formalism is by no means final. Kalbach is currently working on an updated model, which should remove the most severe uncertainties.

#### 4.4.5 Angular distribution systematics

A sound pre-equilibrium theory should, besides the angle-integrated spectra, also describe the smooth forward peaked angular distributions in the continuum. A physics method to do so will be included in a future version of TALYS (multi-step direct reactions). Semi-classical models, such as the exciton model, have always had some problems to describe angular distributions (essentially because it is based on a compound-like concept instead of a direct one [71]). A powerful phenomenological method is given by Kalbach [72]. It is based on experimental information only and the insight that in general, a pre-equilibrium process consists of a forward peaked part (multi-step direct) and an isotropic part (multi-step compound), and that the angular distributions are fairly structureless and all look alike. The Kalbach formula for the double-differential cross section for a projectile  $a$  and an ejectile  $b$  is

$$\frac{d^2\sigma_{a,xb}}{dE_b d\Omega} = \frac{1}{4\pi} \left[ \frac{d\sigma^{\text{PE}}}{dE_b} + \frac{d\sigma^{\text{comp}}}{dE_b} \right] \frac{a}{\sinh(a)} [\cosh(a \cos \Theta) + f_{MSD}(E_b) \sinh(a \cos \Theta)] \quad (4.129)$$

where  $\frac{d\sigma^{\text{PE}}}{dE_b}$  and  $\frac{d\sigma^{\text{comp}}}{dE_b}$  are the angle-integrated pre-equilibrium and compound spectra, respectively, and  $f_{MSD}$  is the so-called multi-step direct or pre-equilibrium ratio:

$$f_{MSD}(E_b) = \frac{d\sigma^{\text{PE}}}{dE_b} / \left[ \frac{d\sigma^{\text{PE}}}{dE_b} + \frac{d\sigma^{\text{comp}}}{dE_b} \right] \quad (4.130)$$

which thus increases from practically 0 at very low emission energy to 1 at the highest emission energies. Hence, once the angle-integrated spectra are known, the parameter  $a$  determines the angular distribution. Kalbach parameterized it as

$$\begin{aligned}
a(e'_a, e'_b) &= 0.04 \frac{E_1 e'_b}{e'_a} + 1.8 \times 10^{-6} \left( \frac{E_1 e'_b}{e'_a} \right)^3 + 6.7 \times 10^{-7} M_a m_b \left( \frac{E_3 e'_b}{e'_a} \right)^4, \\
E_1 &= \min(e'_a, 130 \text{ MeV}) \\
E_3 &= \min(e'_a, 41 \text{ MeV}) \\
e'_b &= E_b + S_b \\
e'_a &= E_a + S_a. \\
M_a &= 1 \text{ for neutrons, protons, deuterons, tritons and Helium} - 3 \\
&= 0 \text{ for alpha's} \\
m_b &= 1 \text{ for protons, deuterons, tritons and Helium} - 3 \\
&= \frac{1}{2} \text{ for neutrons} \\
&= 2 \text{ for alpha's} \\
S_b &= 15.68(A_C - A_B) - 28.07 \left[ \frac{(N_C - Z_C)^2}{A_C} - \frac{(N_B - Z_B)^2}{A_B} \right] \\
&\quad - 18.56(A_C^{2/3} - A_B^{2/3}) + 33.22 \left[ \frac{(N_C - Z_C)^2}{A_C^{4/3}} - \frac{(N_B - Z_B)^2}{A_B^{4/3}} \right] \\
&\quad - 0.717 \left[ \frac{Z_C^2}{A_C^{1/3}} - \frac{Z_B^2}{A_B^{1/3}} \right] + 1.211 \left[ \frac{Z_C^2}{A_C} - \frac{Z_B^2}{A_B} \right] - I_b \\
I_d &= 2.225 \\
I_t &= 8.482 \\
I_h &= 7.718 \\
I_\alpha &= 28.296,
\end{aligned} \tag{4.131}$$

Here,  $E_a$  and  $E_b$  are the incident and the outgoing energy, respectively. The number  $M_a$  represents the incident particle, while  $m_b$  represents the outgoing particle, C is a label for the compound nucleus, B for the final nucleus and the Myers and Swiatecki mass formula [73] for spherical nuclides should be used here to determine the separation energy  $S$ . Finally  $I_b$  is the energy required to break the emitted particle up into its constituents.

Since we calculate the pre-equilibrium and compound cross sections explicitly (and actually only use  $f_{MSD}$  for ENDF-6 data libraries), Eq. (4.129) can be reduced to a formula for the double-differential pre-equilibrium cross section

$$\frac{d^2 \sigma_{a,xb}^{\text{PE}}}{dE_b d\Omega} = \frac{1}{4\pi} \frac{d\sigma^{\text{PE}}}{dE_b} \frac{a}{\sinh(a)} \exp(a \cos \Theta), \tag{4.132}$$

to which the isotropic compound angular distribution can be added. In sum, given the angle-integrated spectrum  $\frac{d\sigma^{\text{PE}}}{dE_b}$  by some physics model, the double-differential cross section is returned quite simply and reasonably accurate by Eq. (4.132).

## 4.5 Compound reactions

The term compound nucleus reaction is commonly used for two different mechanisms: (i) the process of the capture of the projectile in the target nucleus to form a compound nucleus, which subsequently emits a particle or gamma, (ii) the multiple emission process of highly excited residual nuclei formed after the binary reaction. The latter, which is known as multiple compound emission, will be explained in Section 4.6. We first treat the binary compound nucleus reaction that plays a role at low incident energy. It differs from the multiple compound emission at two important points: (a) the presence of width fluctuation corrections and (b) non-isotropic, though still symmetric, angular distributions.

### 4.5.1 Binary compound cross section and angular distribution

In the compound nucleus picture, the projectile and the target nucleus form a compound nucleus with a total energy  $E^{tot}$  and a range of values for the total spin  $J$  and parity  $\Pi$ . The following energy, angular momentum and parity conservation laws need to be obeyed,

$$\begin{aligned} E_a + S_a &= E_{a'} + E_x + S_{a'} = E^{tot} \\ s + I + l &= s' + I' + l' = J \\ \pi_0 \Pi_0 (-1)^l &= \pi_f \Pi_f (-1)^{l'} = \Pi. \end{aligned} \quad (4.133)$$

The compound nucleus formula for the binary cross section is given by

$$\begin{aligned} \sigma_{\alpha\alpha'}^{comp} &= D^{comp} \frac{\pi}{k^2} \sum_{J=mod(I+s,1)}^{l_{max}+I+s} \sum_{\Pi=-1}^1 \frac{2J+1}{(2I+1)(2s+1)} \sum_{j=|J-I|}^{J+I} \sum_{l=|j-s|}^{j+s} \sum_{j'=|J-I'|}^{J+I'} \sum_{l'=|j'-s'|}^{j'+s'} \\ &\times \delta_\pi(\alpha) \delta_\pi(\alpha') \frac{T_{\alpha l j}^J(E_a) \langle T_{\alpha' l' j'}^J(E_{a'}) \rangle}{\sum_{\alpha'', l'', j''} \delta_\pi(\alpha'') \langle T_{\alpha'' l'' j''}^J(E_{a'') \rangle} W_{\alpha l j \alpha' l' j'}^J, \end{aligned} \quad (4.134)$$

In the above equations, the symbols have the following meaning:

$E_a$  = projectile energy

$s$  = spin of the projectile

$\pi_0$  = parity of the projectile

$l$  = orbital angular momentum of the projectile

$j$  = total angular momentum of the projectile

$\delta_\pi(\alpha) = 1$ , if  $(-1)^l \pi_0 \Pi_0 = \Pi$  and 0 otherwise

$\alpha$  = channel designation of the initial system of projectile and target nucleus:

$\alpha = \{a, s, E_a, E_x^0, I, \Pi_0\}$ , where  $a$  is the projectile type and  $E_x^0$  the excitation energy of the target nucleus (usually zero)

$l_{max}$  = maximum l-value for projectile

$S_a$  = separation energy

$E_{a'}$  = ejectile energy

$s'$  = spin of the ejectile

$\pi_f$  = parity of the ejectile

$l'$  = orbital angular momentum of the ejectile

$j'$  = total angular momentum of the ejectile

$\delta_\pi(\alpha') = 1$ , if  $(-1)^{l'}\pi_f\Pi_f = \Pi$  and 0 otherwise

$\alpha'$  = channel designation of the final system of ejectile and residual nucleus:

$\alpha' = \{a', s', E_{a'}, E_x, l', \Pi_f\}$ , where  $a'$  is the ejectile type,  $E_x$  the excitation energy of the residual nucleus

$I$  = spin of the target nucleus

$\Pi_0$  = parity of the target

$I'$  = spin of the residual nucleus

$\Pi_f$  = parity of the residual nucleus

$\Pi$  = parity of the compound system

$J$  = total angular momentum of the compound system

$D^{comp}$  = depletion factor to account for direct and pre-equilibrium effects

$k$  = wave number of relative motion

$T$  = transmission coefficient

$W$  = width fluctuation correction (WFC) factor, see the next Section.

In order to let Eq. (4.134) represent the general case, we have denoted the outgoing transmission coefficient by  $\langle T_{\alpha'l'j'}^J \rangle$ . For this, two cases can be distinguished. If the excitation energy  $E_x$ , that is implicit in the definition of channel  $\alpha'$ , corresponds to a discrete state of the final nucleus, then we simply have

$$\langle T_{\alpha'l'j'}^J(E_{a'}) \rangle = T_{\alpha'l'j'}^J(E_{a'}) \quad (4.135)$$

and  $E_{a'}$  is exactly determined by Eq. (4.133). For  $\alpha'$  channels in which  $E_x$  is in the continuum, we have an effective transmission coefficient for an excitation energy bin with width  $\Delta E_x$ ,

$$\langle T_{\alpha'l'j'}^J(E_{a'}) \rangle = \int_{E_x - \frac{1}{2}\Delta E_x}^{E_x + \frac{1}{2}\Delta E_x} dE_{x'} \rho(E_{x'}, J, \Pi) T_{\alpha'l'j'}^J(E_{a'}) \quad (4.136)$$

where  $\rho$  is the level density, which will be discussed in Section 4.7, and  $T$  is evaluated at an emission energy  $E_{a'}$  that corresponds to the middle of the excitation energy bin, i.e.  $E_{a'} = E^{tot} - E_x - S_{a'}$ . Hence,

both transitions to discrete states and transitions to the whole accessible continuum are covered by the sum over  $\alpha'$  in Eq. (4.134). The normalisation factor  $D^{comp}$  is

$$D^{comp} = [\sigma_{react} - \sigma^{disc,direct} - \sigma^{PE}]/\sigma_{react} \quad (4.137)$$

This indicates that in TALYS we assume that direct and compound contributions can be added incoherently. This formula for  $D^{comp}$  is only applied for weakly coupled channels that deplete the flux, such as contributions from DWBA or pre-equilibrium. In the case of coupled-channels calculations for the discrete collective states, the transmission coefficients of Eq. (4.134) are automatically reduced by ECIS-97 to account for direct effects and TALYS only subtracts the direct cross section for the weakly coupled levels (DWBA), i.e. if

$$\sigma^{disc,direct} = \sigma^{disc,cc} + \sigma^{disc,DWBA} \quad (4.138)$$

then

$$D^{comp} = [\sigma_{react} - \sigma^{disc,DWBA} - \sigma^{PE}]/\sigma_{react} \quad (4.139)$$

TALYS also computes the compound nucleus formula for the angular distribution. It is given by

$$\frac{d\sigma_{\alpha\alpha'}^{comp}(\theta)}{d\Omega} = \sum_L C_L^{comp} P_L(\cos \Theta), \quad (4.140)$$

where  $P_L$  are Legendre polynomials. The Legendre coefficients  $C_L^{comp}$  are given by

$$\begin{aligned} C_L^{comp} &= D^{comp} \frac{\pi}{k^2} \sum_{J,\Pi} \frac{2J+1}{(2I+1)(2s+1)} \sum_{j=|J-I|}^{J+I} \sum_{l=|j-s|}^{j+s} \sum_{j'=|J-I'|}^{J+I'} \sum_{l'=|j'-s'}^{j'+s'} \\ &\times \delta_\pi(\alpha)\delta_\pi(\alpha') \frac{T_{\alpha l j}^J(E_a) \langle T_{\alpha' l' j'}^J(E_{a'}) \rangle}{\sum_{\alpha'', l'', j''} \delta_\pi(\alpha'') \langle T_{\alpha'' l'' j''}^J(E_{a'') \rangle} W_{\alpha l j \alpha' l' j'}^J A_{I l j I' l' j'; L}^J, \end{aligned} \quad (4.141)$$

where the Blatt-Biedenharn factor  $A$  is given by

$$\begin{aligned} A_{I l j I' l' j'; L}^J &= \frac{(-1)^{I'-s'-I+s}}{4\pi} (2J+1)(2j+1)(2l+1)(2j'+1)(2l'+1) \\ &(ll00|L0) \mathcal{W}(JjJj; IL) \mathcal{W}(jjll; Ls) (l'l'00|L0) \mathcal{W}(Jj'Jj'; I'L) \mathcal{W}(j'j'l'l'; Ls'), \end{aligned} \quad (4.142)$$

where  $(\quad | \quad)$  are Clebsch-Gordan coefficients and  $\mathcal{W}$  are Racah coefficients.

Formulae (4.134) and (4.140-4.142) show that the width fluctuation correction factors and the angular distribution factors depend on all the angular momentum quantum numbers involved, and thus have to be re-evaluated each time inside all the summations. We generally need these formulae for relatively low incident energy, where the WFC has a significant impact and where the compound nucleus cross section to each individual discrete state is large enough to make its angular distribution of interest. For projectile energies above several MeV (we generally take the neutron separation energy for safety), the width fluctuations have disappeared, meaning that  $W_{\alpha l j \alpha' l' j'}^J = 1$  for all channels. Then for the angle-integrated compound cross section, instead of performing the full calculation, Eq. (4.134) can be decoupled into two parts that represent the incoming and outgoing reaction flux, respectively. It simplifies to

$$\sigma_{\alpha\alpha'}^{comp} = \sum_{J=\text{mod}(I+s,1)}^{l_{max}+I+s} \sum_{\Pi=-1}^1 \sigma_{J\Pi}^{CF}(E^{tot}) \frac{\Gamma_{\alpha'}(E^{tot}, J, \Pi \rightarrow E_x, I', \Pi_f)}{\Gamma^{tot}(E^{tot}, J, \Pi)} \quad (4.143)$$

where  $\sigma_{J\Pi}^{CF}$  is the compound formation cross section per spin and parity:

$$\sigma_{J\Pi}^{CF}(E^{tot}) = D^{comp} \frac{\pi}{k^2} \frac{2J+1}{(2I+1)(2S+1)} \sum_{j=|J-I|}^{J+I} \sum_{l=|j-s|}^{j+s} T_{\alpha l j}^J(E_a) \delta_{\pi}(\alpha) \quad (4.144)$$

which itself obeys

$$\sum_{J=\text{mod}(I+s,1)}^{l_{max}+I+s} \sum_{\Pi=-1}^1 \sigma_{J\Pi}^{CF}(E^{tot}) = D^{comp} \sigma_{react} \quad (4.145)$$

The partial decay widths are

$$\Gamma_{\alpha'}(E^{tot}, J, \Pi \longrightarrow E_x, I', \Pi_f) = \frac{1}{2\pi\rho(E^{tot}, J, \Pi)} \sum_{j'=|J-I'|}^{J+I'} \sum_{l'=|j'-s'}^{j'+s'} \delta_{\pi}(\alpha') \langle T_{\alpha' l' j'}^J(E'_a) \rangle \quad (4.146)$$

and the total decay width is

$$\Gamma^{tot}(E^{tot}, J, \Pi) = \sum_{\alpha''} \Gamma_{\alpha''}(E^{tot}, J, \Pi \longrightarrow E_x, I'', \Pi_f) \quad (4.147)$$

where we sum over all possible states in the residual nuclides through the sum over  $\alpha''$ . Note that the term with the compound nucleus level density,  $2\pi\rho$ , is present in both Eq. (4.146) and Eq. (4.147) and therefore does not need to be calculated in practice for Eq. (4.143). A formula similar to Eq. (4.143) is used for multiple emission, see Section 4.6.

In sum, we use Eqs. (4.134) and (4.141) if either width fluctuations (**widthfluc y**, p. 132) or compound angular distributions (**outangle y**, p. 159) are to be calculated and Eq. (4.143) if they are both not of interest.

A final note to make here is that the formulae of this whole Section can also be applied for excited (isomeric) target states.

#### 4.5.2 Width fluctuation correction factor

The WFC factor  $W$  accounts for the correlations that exist between the incident and outgoing waves. From a qualitative point of view, these correlations enhance the elastic channel and accordingly decrease the other open channels. Above a few MeV of projectile energy, when many competing channels are open, the WFC factor can be neglected and the simple Hauser-Feshbach model is adequate to describe the compound nucleus decay. To explain the WFC factors, we now switch to a more compact notation in which we leave out  $J$  and define  $a = \{\alpha, l, j\}$  and  $b = \{\alpha', l', j'\}$ . With such a notation the compound nucleus cross section can be written in the compact form

$$\sigma_{ab} = \frac{\pi}{k_a^2} \frac{T_a T_b}{\sum_c T_c} W_{ab} \quad (4.148)$$

for each combination of  $a$  and  $b$ . In general, the WFC factor may be calculated using three different expressions, which have all been implemented in TALYS: The Hofmann-Richert-Tepel-Weidenmüller (HRTW) model [74, 75, 76], the Moldauer model [77, 78], and the model using the Gaussian Orthogonal Ensemble (GOE) of Hamiltonian matrices [79]. A comparison between the three models is given in Ref. [6].

For each expression, flux conservation implies that

$$T_a = \sum_b \frac{T_a T_b}{\sum_c T_c} W_{ab} \quad (4.149)$$

This equation can be used to check the numerical accuracy of the WFC calculation (see the **flagcheck** keyword in Chapter 6).

### The HRTW method

The simplest approach is the HRTW method. It is based on the assumption that the main effect of the correlation between incident and outgoing waves is in the elastic channel. In that case, it is convenient to express the compound nucleus cross section (4.148) as

$$\sigma_{ab} = \frac{\pi}{k^2} \frac{V_a V_b}{\sum_c V_c} [1 + \delta_{ab}(W_a - 1)], \quad (4.150)$$

where the  $V_i$ 's are effective transmission coefficients that take into account the correlations.

This expression means that only the elastic channel enhancement is described since for  $a = b$ , Eq. (4.150) becomes

$$\sigma_{aa} = \frac{\pi}{k_a^2} \frac{V_a^2}{\sum_c V_c} W_a \quad (4.151)$$

while for  $a \neq b$ ,

$$\sigma_{ab} = \frac{\pi}{k_a^2} \frac{V_a V_b}{\sum_c V_c} \quad (4.152)$$

An expression for the  $V_i$  values can be determined from the flux conservation condition

$$\sum_b \sigma_{ab} = \frac{\pi}{k_a^2} T_a, \quad (4.153)$$

which yields using Eq. (4.150)

$$T_a = V_a + (W_a - 1) \frac{V_a^2}{\sum_c V_c}, \quad (4.154)$$

or

$$V_a = \frac{T_a}{1 + \frac{(W_a - 1)V_a}{\sum_c V_c}}. \quad (4.155)$$

The only required information is thus the expression for  $W_a$ , which can be derived from an analysis using random matrix calculations. In TALYS, the expression of Ref. [76] is used. It reads

$$W_a = 1 + \frac{2}{1 + T_a^F} + 87 \left( \frac{T_a - \bar{T}}{\sum_c T_c} \right)^2 \left( \frac{T_a}{\sum_c T_c} \right)^5, \quad (4.156)$$

$$\text{with } \bar{T} = \frac{\sum_c T_c^2}{\sum_c T_c} \text{ and the exponent } F = \frac{4 \frac{\bar{T}}{\sum_c T_c} \left( 1 + \frac{T_a}{\sum_c T_c} \right)}{1 + \frac{3\bar{T}}{\sum_c T_c}}.$$

The result for  $V_a$  is obtained after iterating Eq. (4.155) several times, starting from the initial value

$$V_a(i=0) = \frac{T_a}{1 + (W_a - 1) \frac{T_a}{\sum_c T_c}} \quad (4.157)$$

and calculating  $V_a(i+1)$  using

$$V_a(i+1) = \frac{T_a}{1 + (W_a - 1) \frac{V_a(i)}{\sum_c V_c(i)}} \quad (4.158)$$

until  $V_a(i+1) \approx V_a(i)$ . In a calculation, a few tens of iterations are generally required to reach a stable result.

For each  $J$  and  $\Pi$ , expressions (4.155)-(4.158) only need to be evaluated once. This is done in *hrtwprepare.f*, before all the loops over  $l, j, l'$  and  $j'$ , etc. quantum numbers are performed. For the calculation of  $W_{alja'l'j'}$  in Eq. (4.134), which takes place inside all loops, the correct  $V_a$  and  $V_b$  are then addressed. The WFC factor can then be derived from Eqs. (4.148) and (4.150),

$$W_{ab} = \frac{V_a V_b}{\sum_c V_c} [1 + \delta_{ab}(W_a - 1)] \frac{\sum_c T_c}{T_a T_b} \quad (4.159)$$

which is calculated in *hrtw.f*.

### Moldauer expression

This is the default option for the WFC in TALYS. Moldauer's expression for  $W_{ab}$  is based on the assumption that a  $\chi^2$  law with  $\nu$  degrees of freedom applies for the partial widths  $\Gamma$ , which can be calculated from a Porter-Thomas distribution. These are associated with transmission coefficients as

$$T = \frac{2\pi \langle \Gamma \rangle}{D} \quad (4.160)$$

provided  $\langle \Gamma \rangle \ll D$ , where  $D$  is the mean level spacing. The WFC factor  $W_{ab}$  reads

$$W_{ab} = \left( 1 + \frac{2\delta_{ab}}{\nu_a} \right) \int_0^{+\infty} \prod_c \left( 1 + \frac{2T_c x}{\nu_c \sum_i T_i} \right)^{-(\delta_{ac} + \delta_{bc} + \nu_c/2)} dx \quad (4.161)$$

Moldauer has parameterised  $\nu$  using Monte Carlo calculations, giving

$$\nu_a = 1.78 + (T_a^{1.212} - 0.78) \exp \left( -0.228 \sum_c T_c \right) \quad (4.162)$$

In TALYS, the integral in Eq. (4.161) is evaluated numerically. For this, the Gauss-Laguerre method has been chosen and we find that 40 integration points are enough to reach convergence, the criterion being the flux conservation of Eq. (4.149). As for the HRTW model, the calculation can be split into parts dependent and independent of the channel quantum numbers. First, in *molprepare.f*, for each  $J$  and  $\Pi$ , we calculate Eq. (4.162) for all channels and the product  $\prod_c \left(1 + \frac{2T_c x}{v_c \sum_i T_i}\right)^{-v_c/2}$  that appears in Eq. (4.161). Inside all the loops, we single out the correct  $a$  and  $b$  channel and calculate Eq. (4.161) in *moldauer.f*.

Eq. (4.161) involves a product over all possible open channels. When the number of channels is large, the product calculation drastically increases the time of computation, forcing us to consider another method. Many open channels are considered for capture reactions and reactions to the continuum.

**A. Capture reactions** If the projectile is captured by the target nucleus, the compound nucleus is formed with an excitation energy at least equal to the projectile separation energy in the compound system. Since the  $\gamma$  transmission coefficient calculation involves all the possible states to which a photon can be emitted from the initial compound nucleus state, the number of radiative open channels is almost infinite, but each has a very small transmission coefficient. Following Ref. [80], the product over the radiative channels in Eq. (4.161) can be transformed as

$$\prod_{c \in \gamma} \left(1 + \frac{2T_c x}{v_c \sum_i T_i}\right)^{-v_c/2} \approx \lim_{v_\gamma \rightarrow +\infty} \left(1 + \frac{2T_\gamma x}{\bar{v}_\gamma \sum_i T_i}\right)^{-\bar{v}_\gamma/2} = \exp\left(-\frac{T_\gamma^{eff} x}{\sum_i T_i}\right) \quad (4.163)$$

where  $T_\gamma^{eff}$  is given by the procedure sketched in Section 4.3. The derivation is based on the hypothesis that all the individual  $T_\gamma$  are almost identical to 0. Therefore, to calculate  $W_{ab}$  when  $b$  denotes the gamma channel, we set  $T_b = 0$  in Eqs. (4.161) and use Eqs. (4.163) to calculate the product for  $\gamma$  channels.

**B. Continuum reactions** For high excitation energies, it is impossible to describe all the open channels individually. It is then necessary to introduce energy bins to discretize the continuum of levels and define continuum (or effective) transmission coefficients as

$$T_{eff}(U) = \int_{E_{min}}^{E_{max}} \rho(\varepsilon) T(\varepsilon) d\varepsilon, \quad (4.164)$$

where  $U$  is generally taken as the middle of the interval  $[E_{min}, E_{max}]$  and  $\rho$  is the density of levels under consideration. This effective transmission coefficient corresponds to an effective number of channels  $N_{eff}(U)$ , given by

$$N_{eff}(U) = \int_{E_{min}}^{E_{max}} \rho(\varepsilon) d\varepsilon. \quad (4.165)$$

Calculating the product term in Eq. (4.161) is tedious, unless one assumes that the energy variation of  $T(\varepsilon)$  is smooth enough to warrant that each of the  $N_{eff}(U)$  channels has the same average transmission coefficient

$$T_{mean}(U) = \frac{T_{eff}(U)}{N_{eff}(U)}. \quad (4.166)$$

Then, the product over the channels  $c$  belonging to such a continuum bin in the Moldauer integral Eq. (4.161) can be replaced by a single term, i.e.

$$\prod_c \left( 1 + \frac{2T_c}{v_c \sum_i T_i} x \right)^{-v_c/2} \approx \left( 1 + \frac{2T_{mean}(U)}{v_{mean} \sum_i T_i} x \right)^{-N_{eff}(U)v_{mean}/2}, \quad (4.167)$$

where

$$v_{mean} = 1.78 + (T_{mean}^{1.212} - 0.78) \exp\left(-0.228 \sum_c T_c\right) \quad (4.168)$$

**C. Fission reactions** The fission reaction is treated as one global channel, regardless of the nature of the fission fragments that result from fission. We will see later on in Section 4.8, how the global fission transmission coefficient is calculated. It is however important to state here that the fission transmission coefficient is generally greater than 1 since it results from a summation over several fission paths and can therefore be defined as

$$T_{fis}(U) = \int_{E_{min}}^{E_{max}} \rho_{fis}(\varepsilon) T_f(\varepsilon) d\varepsilon. \quad (4.169)$$

Of course, one has  $0 \leq T_f(\varepsilon) \leq 1$ , but one can not assume that  $T_f$  is constant over the whole integration energy range as in the case of continuum reactions. To bypass this problem, instead of using a global fission transmission coefficient, we have grouped the various components of Eq. (4.169) according to their values. Instead of dealing with a global fission transmission coefficient, we use  $N$  different global transmission coefficients (where  $N$  is an adjustable parameter) such that

$$T_{fis}(U) = \sum_{i=0}^N T_{fis}(i, U) \quad (4.170)$$

where

$$T_{fis}(i, U) = \int_{E_{min}}^{E_{max}} \rho_{fis}(\varepsilon) T_f(\varepsilon) \delta_{i,N} d\varepsilon \quad (4.171)$$

and  $\delta_{i,N} = 1$  is  $i/N \leq T_f(\varepsilon) \leq (i+1)/N$  and 0 otherwise.

In this case one can define, as for continuum reactions, an effective number of channels  $N_{fis}(i, U)$ , and use  $N$  average fission transmission coefficients defined by

$$T_{fismean}(i) = \frac{T_{fis}(i, U)}{N_{fis}(i, U)}. \quad (4.172)$$

If  $N$  is large enough, these  $N$  average coefficients can be used for the width fluctuation calculation without making a too crude approximation.

### The GOE triple integral

The two previously described methods to obtain  $W_{ab}$  are readily obtained since both are relatively simple to implement. However, in each case, a semi-empirical parameterisation is used. The GOE formulation avoids such a parameterisation, in which sense it is the more general expression. In the GOE approach,  $W_{ab}$  reads

$$W_{ab} = \frac{\sum_c T_c}{8} \int_0^{+\infty} d\lambda_1 \int_0^{+\infty} d\lambda_2 \int_0^1 d\lambda f(\lambda_1, \lambda_2, \lambda) \prod_c (\lambda_1, \lambda_2, \lambda) g_{ab}(\lambda_1, \lambda_2, \lambda) \quad (4.173)$$

with

$$f(\lambda_1, \lambda_2, \lambda) = \frac{\lambda(1-\lambda)|\lambda_1 - \lambda_2|}{\sqrt{\lambda_1 \lambda_2 (1 + \lambda_1)(1 + \lambda_2)} (\lambda + \lambda_1)^2 (\lambda + \lambda_2)^2}, \quad (4.174)$$

$$\prod_c (\lambda_1, \lambda_2, \lambda) = \prod_c \frac{1 - \lambda T_c}{\sqrt{(1 + \lambda_1 T_c)(1 + \lambda_2 T_c)}}, \quad (4.175)$$

and

$$g_{ab}(\lambda_1, \lambda_2, \lambda) = \delta_{ab}(1 - T_a) \left( \frac{\lambda_1}{1 + \lambda_1 T_a} + \frac{\lambda_2}{1 + \lambda_2 T_a} + \frac{2\lambda}{1 - \lambda T_a} \right)^2 + (1 + \delta_{ab}) \times \left[ \frac{\lambda_1(1 + \lambda_1)}{(1 + \lambda_1 T_a)(1 + \lambda_1 T_b)} + \frac{\lambda_2(1 + \lambda_2)}{(1 + \lambda_2 T_a)(1 + \lambda_2 T_b)} + \frac{2\lambda(1 - \lambda)}{(1 - \lambda T_a)(1 - \lambda T_b)} \right] \quad (4.176)$$

The numerical method employed to compute this complicated triple integral is explained in Ref. [6].

Also here, a particular situation exists for the capture channel, where we set

$$\prod_{c \in \gamma} \frac{1 - \lambda T_c}{\sqrt{(1 + \lambda_1 T_c)(1 + \lambda_2 T_c)}} \approx \exp[-(2\lambda + \lambda_1 + \lambda_2) T_\gamma^{eff}/2] \quad (4.177)$$

and for the continuum, for which we set

$$\prod_c (\lambda_1, \lambda_2, \lambda) = \prod_{c \in \text{continuum}} \frac{(1 - \lambda \bar{T}_c)^{N_c}}{\sqrt{(1 + \lambda_1 \bar{T}_c)^{N_c} (1 + \lambda_2 \bar{T}_c)^{N_c}}}. \quad (4.178)$$

Again, for each  $J$  and  $\Pi$ , the multiplications that do not depend on  $a$  or  $b$  are first prepared in *goeprepare.f*, while the actual WFC calculation takes place in *goef*.

## 4.6 Multiple emission

At incident energies above approximately the neutron separation energy, the residual nuclides formed after the first binary reaction are populated with enough excitation energy to enable further decay by particle emission or fission. This is called multiple emission. We distinguish between two mechanisms: multiple compound (Hauser-Feshbach) decay and multiple pre-equilibrium decay.

### 4.6.1 Multiple Hauser-Feshbach decay

This is the conventional way, and for incident energies up to several tens of MeV a sufficient way, to treat multiple emission. It is assumed that pre-equilibrium processes can only take place in the binary reaction and that secondary and further particles are emitted by compound emission.

After the binary reaction, the residual nucleus may be left in an excited discrete state  $i'$  or an excited state within a bin  $i'$  which is characterized by excitation energy  $E_x'(i')$ , spin  $I'$  and parity  $\Pi'$ . The population of this state or set of states is given by a probability distribution for Hauser-Feshbach decay  $P^{\text{HF}}$  that is completely determined by the binary reaction mechanism. For a binary neutron-induced reaction to a discrete state  $i'$ , i.e. when  $E_x'(i')$ ,  $I'$  and  $\Pi'$  have unique values, the residual population is given by

$$P^{\text{HF}}(Z', N', E_x'(i'), I', \Pi') = \sigma_{n,k'}^{i'}(E^{\text{tot}}, I, \Pi \rightarrow E_x'(i'), I', \Pi'), \quad (4.179)$$

where the non-elastic reaction cross section for a discrete state  $\sigma_{n,k'}^{i'}$  was defined in Section 3.2.3 and where the ejectile  $k'$  connects the initial compound nucleus  $(Z_C, N_C)$  and the residual nucleus  $(Z', N')$ . For binary reactions to the continuum, the residual population of states characterised by  $(I', \Pi')$  per  $E_x'(i')$  bin is given by the sum of a pre-equilibrium and a compound contribution

$$P^{\text{HF}}(Z', N', E_x'(i'), I', \Pi') = \int dE_{k'} \frac{d\sigma^{\text{comp,cont}}}{dE_{k'}}(E^{\text{tot}}, I, \Pi \rightarrow E_x'(i'), I', \Pi') \\ + \mathcal{P}^{\text{pre}}(Z', N', p_\pi^{\text{max}} + 1, h_\pi^{\text{max}} + 1, p_v^{\text{max}} + 1, h_v^{\text{max}} + 1, E_x'(i')), \quad (4.180)$$

where the integration range over  $dE_{k'}$  corresponds exactly with the bin width of  $E_x'(i')$  and  $\mathcal{P}^{\text{pre}}$  denotes the population entering the compound stage after primary preequilibrium emission. The expression for  $\mathcal{P}^{\text{pre}}$  will be given in Eq. (4.184) of the next section. Once the first generation of residual nuclides/states has been filled, the picture can be generalized to tertiary and higher order multiple emission.

In general, the population  $P^{\text{HF}}$  before decay of a level  $i'$  or a set of states  $(I', \Pi', E_x'(i'))$  in bin  $i'$  of a nucleus  $(Z', N')$  in the reaction chain is proportional to the feeding, through the ejectiles  $k'$ , from all possible mother bins  $i$  with an energy  $E_x(i)$  in the  $(Z, N)$  nuclides, i.e.

$$P^{\text{HF}}(Z', N', E_x'(i'), I', \Pi') = \sum_{I, \Pi} \sum_{k'} \sum_i [P^{\text{HF}}(Z, N, E_x(i), I, \Pi) \\ + \mathcal{P}^{\text{pre}}(Z, N, p_\pi^{\text{max}} + 1, h_\pi^{\text{max}} + 1, p_v^{\text{max}} + 1, h_v^{\text{max}} + 1, E_x(i))] \\ \times \frac{\Gamma_{k'}(E_x(i), I, \Pi \rightarrow E_x'(i'), I', \Pi')}{\Gamma^{\text{tot}}(E_x(i), I, \Pi)}. \quad (4.181)$$

The appearance of the indices  $p_\pi^{\text{max}}$  indicates that only the reaction population that has not been emitted via the (multiple) pre-equilibrium mechanism propagates to the multiple compound stage. Similar to Eq. (4.146) the decay widths are given by

$$\Gamma_{k'}(E_x(i), I, \Pi \rightarrow E_x'(i'), I', \Pi') = \frac{1}{2\pi\rho(E_x(i), I, \Pi)} \sum_{j'=|J-I'|}^{J+I'} \sum_{l'=|j'-s'|}^{j'+s'} \delta_\pi(\alpha') \langle T_{\alpha'l'j'}^J(E_{\alpha'}) \rangle. \quad (4.182)$$

Again, the term  $2\pi\rho$  (compound nucleus level density) of the decay width (4.182) falls out of the multiple emission equation (4.181) and therefore does not need to be calculated in practice. The total decay width

is

$$\Gamma^{tot}(E_x(i), I, \Pi) = \sum_{k''} \sum_{I''=mod(J+s,1)}^{J+l_{max}} \sum_{\Pi''=-1}^1 \sum_{i''} \Gamma_{k''}(E_x(i), I, \Pi \longrightarrow E_{x''}(i''), I'', \Pi''). \quad (4.183)$$

In sum, the only differences between binary and multiple compound emission are that width fluctuations and angular distributions do not enter the model and that the initial compound nucleus energy  $E^{tot}$  is replaced by an excitation energy bin  $E_x$  of the mother nucleus. The calculational procedure, in terms of sequences of decaying bins, was already explained in Chapter 3.

#### 4.6.2 Multiple pre-equilibrium emission

At high excitation energies, resulting from high incident energies, the composite nucleus is far from equilibrated and it is obvious that the excited nucleus should be described by more degrees of freedom than just  $E_x$ ,  $J$  and  $\Pi$ . In general, we need to keep track of the particle-hole configurations that are excited throughout the reaction chain and thereby calculate multiple pre-equilibrium emission up to any order. This is accomplished by treating multiple pre-equilibrium emission within the exciton model. This is the default option for multiple pre-equilibrium calculations in TALYS (selected with the keyword **mpreeqmode 1**). TALYS contains, furthermore, an alternative more approximative model for multiple pre-equilibrium emission (**mpreeqmode 2**), called the *s-wave transmission coefficient method*. Both approaches are discussed below.

##### Multiple emission within the exciton model

We introduce the pre-equilibrium population  $\mathcal{P}^{pre}(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i))$  which holds the amount of the reaction population present in a unique  $(Z, N)$  nucleus,  $(p_\pi, h_\pi, p_\nu, h_\nu)$  exciton state and excitation energy bin  $E_x(i)$ . A special case is the pre-equilibrium population for a particular exciton state after binary emission, which can be written as

$$\begin{aligned} & \mathcal{P}^{pre}(Z', N', p_\pi - Z_{k'}, h_\pi, p_\nu - N_{k'}, h_\nu, E_{x'}(i')) = \\ & = \sigma^{CF}(Z_C, N_C, E^{tot}) W_{k'}(Z_C, N_C, E^{tot}, p_\pi, h_\pi, p_\nu, h_\nu, E_{k'}) \\ & \times \tau(Z_C, N_C, E^{tot}, p_\pi, h_\pi, p_\nu, h_\nu) P(Z_C, N_C, E^{tot}, p_\pi, h_\pi, p_\nu, h_\nu), \end{aligned} \quad (4.184)$$

where  $Z_C$  ( $N_C$ ) again is the compound nucleus charge (neutron) number and  $Z_{k'}$  ( $N_{k'}$ ) corresponds to the ejectile charge (neutron) number. The residual excitation energy  $E_{x'}(i')$  is linked to the total energy  $E^{tot}$ , the ejectile energy  $E_{k'}$ , and its separation energy  $S(k')$  by  $E_{x'}(i') = E^{tot} - E_{k'} - S(k')$ . This  $\mathcal{P}^{pre}$  represents the feeding term for secondary pre-equilibrium emission. Note that for several particle-hole configurations this population is equal to zero.

In general, the pre-equilibrium population can be expressed in terms of the mother nucleus, excitation energy bins, and particle-hole configurations from which it is fed. The residual population is given by a generalization of Eq. (4.56), in which  $\sigma^{CF}(Z_C, N_C, E^{tot})$  is replaced by the population of the particle-hole states left after the previous emission stage  $\mathcal{P}^{pre}(Z, N, p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0, E_x(i))$ . Since several combinations of emission and internal transitions may lead to the same configuration, a summation is applied

over the ejectiles treated in multiple pre-equilibrium (neutrons and protons), over the  $(p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0)$  configurations with which the next step is started and over the mother excitation energy bins:

$$\begin{aligned}
\mathcal{P}^{\text{pre}}(Z', N', p'_\pi, h'_\pi, p'_\nu, h'_\nu, E_{x'}(i')) &= \sum_{k'=n, p} \sum_{p_\pi^0=1}^{p_\pi^{\text{max}}} \sum_{h_\pi^0=1}^{h_\pi^{\text{max}}} \sum_{p_\nu^0=1}^{p_\nu^{\text{max}}} \sum_{h_\nu^0=1}^{h_\nu^{\text{max}}} \\
&\sum_i \mathcal{P}^{\text{pre}}(Z, N, p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0, E_x(i)) \\
&W_k(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i), E_{k'}) \tau(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i)) \\
&\times P(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i)), \tag{4.185}
\end{aligned}$$

where the mother and daughter quantities are related by

$$\begin{aligned}
Z &= Z' + Z_{k'}, \\
N &= N' + N_{k'}, \\
p_\pi &= p'_\pi + Z_{k'}, \\
h_\pi &= h'_\pi, \\
p_\nu &= p'_\nu + N_{k'}, \\
h_\nu &= h'_\nu, \\
E_x &= E_{x'}(i') + E_{k'} + S_{k'}. \tag{4.186}
\end{aligned}$$

In the computation, we thus need to keep track of every possible  $(Z', N', p'_\pi, h'_\pi, p'_\nu, h'_\nu, E_{x'}(i'))$  configuration, which is uniquely linked to a mother exciton state  $(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i))$  through the ejectile characterized by  $(Z_{k'}, N_{k'}, E_{k'})$ . The term  $P(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i))$  represents the part of the pre-equilibrium cross section that starts in  $(Z, N, p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0, E_x(i))$  and survives emission up to a new particle-hole state  $(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i))$ . Again (see Eq. (4.71)),

$$P(Z, N, p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0, E_x(i)) = 1, \tag{4.187}$$

and the calculation for each newly encountered  $(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i))$  configuration proceeds according to Eq. (4.69).

The part of  $\mathcal{P}^{\text{pre}}$  that does not feed a new multiple pre-equilibrium population automatically goes to the multiple Hauser-Feshbach chain of Eq. (4.181).

The final expression for the multiple pre-equilibrium spectrum is very similar to Eq. (4.56)

$$\begin{aligned}
\frac{d\sigma_k^{\text{MPE}}}{dE_{k'}} &= \sum_{p_\pi^0=1}^{p_\pi^{\text{max}}} \sum_{h_\pi^0=1}^{h_\pi^{\text{max}}} \sum_{p_\nu^0=1}^{p_\nu^{\text{max}}} \sum_{h_\nu^0=1}^{h_\nu^{\text{max}}} \\
&\sum_i \mathcal{P}^{\text{pre}}(Z, N, p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0, E_x(i)) \\
&\sum_{p_\pi=p_\pi^0}^{p_\pi^{\text{max}}} \sum_{h_\pi=h_\pi^0}^{h_\pi^{\text{max}}} \sum_{p_\nu=p_\nu^0}^{p_\nu^{\text{max}}} \sum_{h_\nu=h_\nu^0}^{h_\nu^{\text{max}}} W_k(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i), E_{k'}) \\
&\times \tau(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i)) P(Z, N, p_\pi, h_\pi, p_\nu, h_\nu, E_x(i)) \tag{4.188}
\end{aligned}$$

### Multiple emission with the s-wave transmission coefficient method

Apart from the exciton model, TALYS offers another, slightly faster, method to determine multiple pre-equilibrium emission [81, 82]. Within this approach the multiple pre-equilibrium spectrum is given by the following expression:

$$\begin{aligned} \frac{d\sigma_k^{\text{MPE}}}{dE_{k'}} &= \sum_{p_\pi^0=1}^{p_\pi^{\text{max}}} \sum_{h_\pi^0=1}^{h_\pi^{\text{max}}} \sum_{p_\nu^0=1}^{p_\nu^{\text{max}}} \sum_{h_\nu^0=1}^{h_\nu^{\text{max}}} \\ &\sum_i \mathcal{P}^{\text{pre}}(Z, N, p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0, E_x(i)) \\ &\frac{1}{p_\pi^0 + p_\nu^0} \frac{\omega(Z_{k'}, h_\pi^0, N_{k'}, h_\nu^0, E_{k'} + S_{k'}) \omega(p_\pi^0 - Z_{k'}, h_\pi^0, p_\nu^0 - N_{k'}, h_\nu^0, E_x(i) - E_{k'} - S_{k'})}{\omega(p_\pi^0, h_\pi^0, p_\nu^0, h_\nu^0, E_x(i))} \\ &\times T_s(E_{k'}) \end{aligned} \quad (4.189)$$

In this approach each residual particle-hole configuration created in the primary pre-equilibrium decay may have one or more excited particles in the continuum. Each of these excited particles can either be emitted or captured. The emission probability is assumed to be well represented by the s-wave transmission coefficient  $T_s(E_{k'})$ .

## 4.7 Level densities

In statistical models for predicting cross sections, nuclear level densities are used at excitation energies where discrete level information is not available or incomplete. We use several models for the level density in TALYS, which range from phenomenological analytical expressions to tabulated level densities derived from microscopic models.

To set the notation, we first give some general definitions. The *total level density*  $\rho^{\text{tot}}(E_x)$  corresponds to the number of nuclear levels per MeV around an excitation energy  $E_x$ . Similarly, the *level density*  $\rho(E_x, J, \Pi)$  corresponds to the number of levels for a certain spin  $J$  and parity  $\Pi$ . The total level density is obtained by summing the level density over spin and parity:

$$\rho^{\text{tot}}(E_x) = \sum_J \sum_\Pi \rho(E_x, J, \Pi), \quad (4.190)$$

The *total state density*  $\omega(E_x)$  includes the  $2J + 1$  degenerate states for each level, i.e.

$$\omega(E_x) = \sum_J \sum_\Pi (2J + 1) \rho(E_x, J, \Pi) \quad (4.191)$$

When level densities are given by analytical expressions, they are usually written as follows

$$\rho(E_x, J, \Pi) = P(\Pi, J, E_x) R(J, E_x) \rho^{\text{tot}}(E_x) \quad (4.192)$$

where  $P(\Pi, J, E_x)$  describes the parity distribution and  $R(J, E_x)$  the spin distribution. In any level density model we use in TALYS, the parity equipartition is assumed, i.e.

$$P(\Pi, J, E_x) = 1/2 \quad (4.193)$$

In our programming, we have accounted for possible future revisions to non-equidistant parities.

### 4.7.1 Effective level density

We first describe the simplest expressions that are included in TALYS for level densities. We here use the term "effective" to remind the reader that the nuclear collective effects are not explicitly considered. In other words, in what follows, the excited levels of the nucleus are considered as resulting only from independent excitations of its constituents.

#### The Fermi gas Model

The Fermi gas model is the basic model used to derive analytical level densities. It is based on the equidistant spacing model which assumes that the single particle states with which the excited levels of the nucleus are constructed are equally spaced. For this model, it can be shown that the total state density reads

$$\omega(E_x) \equiv \omega_F(E_x) = \frac{\sqrt{\pi} \exp(2\sqrt{aU})}{12 a^{1/4} U^{5/4}} \quad (4.194)$$

where  $U = E_x - \Delta$ , with  $\Delta$  the pairing energy, and  $a$  is the so-called level density parameter given by

$$a = \frac{\pi^2}{6} (g_\pi + g_\nu) \quad (4.195)$$

with  $g_\pi$  (resp.  $g_\nu$ ) denoting the spacing of the proton (resp. neutron) single particle states. The pairing energy  $\Delta$  is an empirical parameter added to simulate the known odd-even effects in the nuclei. The underlying idea is to introduce  $\Delta$  to account for the fact that pairs of nucleons must be separated before exciting individually each component. By default, it has a systematic value given by

$$\Delta = \chi \frac{12}{\sqrt{A}} \quad (4.196)$$

where  $\chi = 0, 1$  or  $2$  for odd-odd, odd or even-even nuclei, respectively, but in TALYS  $\Delta$  may also be used as an adjustable parameter.

Under the assumption that the projection of the total angular momentum follows a Gaussian distribution, it can be derived [83] that the Fermi gas level density is

$$\rho_F(E_x, J, \Pi) = \frac{1}{2} \frac{2J+1}{2\sqrt{2\pi}\sigma^2} \exp\left[-\frac{(J+\frac{1}{2})^2}{2\sigma^2}\right] \frac{\sqrt{\pi} \exp(2\sqrt{aU})}{12 a^{1/4} U^{5/4}} \quad (4.197)$$

where the first factor  $\frac{1}{2}$  represents the aforementioned equiparity distribution. The spin cut-off factor  $\sigma^2$ , with an implicit treatment of the collective enhancement, is given by

$$\sigma^2 = cA^{2/3} \sqrt{aU} \quad (4.198)$$

with  $c = 0.0888$ . The parameter  $c$  can be altered by means of the **spincut** keyword, see page 147.

Summing  $\rho_F(J, E_x, \Pi)$  over all spins and parities yields for the total level density

$$\rho_F^{tot}(E_x) = \frac{\sqrt{\pi} \exp(2\sqrt{aU})}{12 \sqrt{2\pi}\sigma a^{1/4} U^{5/4}} = \frac{\omega_F(E_x)}{\sqrt{2\pi}\sigma} \quad (4.199)$$

In the TALYS-output, all quantities of interest are printed, if requested.

### Energy dependent level density parameter $a$

In the Fermi gas model, the level density parameter  $a$  can be derived from  $D_0$ , the average s-wave level spacing at the neutron separation energy  $S_n$ , which is usually obtained from the available experimental set of s-wave resonances. The following equation can be used:

$$\frac{1}{D_0} = \sum_{J=|I-\frac{1}{2}|}^{J=I+\frac{1}{2}} \rho_F(S_n, J, \Pi) \quad (4.200)$$

where  $I$  is the spin of the target nucleus. From this equation, the level density parameter  $a$  can be extracted by an iterative search procedure.

The formulae described above may suggest a constant value for the level density parameter  $a$ . However, Ignatyuk et al. [84] proposed an energy dependent expression for this crucial parameter, to take into account the damping of shell effects at high excitation energy. The expression is semi-empirical since its functional form has not been derived theoretically but is fitted to microscopic calculations of level densities. It reads

$$a(E_x) = \tilde{a} \left[ 1 + \delta W \frac{1 - \exp(-\gamma U)}{U} \right] \quad (4.201)$$

Here,  $\tilde{a}$  is the asymptotic level density value (i.e.  $E_x \rightarrow \infty$ ),  $\gamma$  is called the shell damping parameter and  $\delta W$  is the shell correction energy. It is important to define the order in which the various parameters of Eq. (4.201) are calculated in TALYS, because they can be given as an adjustable parameter in the input file, they can be known from experiment or they can be determined from systematics.

First, we define  $\delta W$ , in MeV, as the difference between the real mass of the nucleus,  $M_{exp}$  and its spherical liquid drop model mass  $M_{LDM}$ :

$$\delta W = (M_{exp} - M_{LDM}) * amu \quad (4.202)$$

where  $amu = 931.49386$ . For the real mass we take the value from the experimental/theoretical mass database (see Chapter 5) and for  $M_{LDM}$  we take the formula by Myers and Swiatecki [73]:

$$\begin{aligned} M_{LDM} &= A + E_{LDM}/amu \\ E_{LDM} &= M_n N + M_H Z + E_{vol} + E_{sur} + E_{coul} + \delta \\ M_n &= 8.07144 \text{ MeV} \\ M_H &= 7.28899 \text{ MeV} \\ E_{vol} &= -c_1 A \\ E_{sur} &= c_2 A^{2/3} \\ E_{coul} &= c_3 \frac{Z^2}{A^{1/3}} - c_4 \frac{Z^2}{A} \\ c_i &= a_i \left[ 1 - \kappa \left( \frac{N - Z}{A} \right)^2 \right], \quad i = 1, 2 \\ a_1 &= 15.677 \text{ MeV} \\ a_2 &= 18.56 \text{ MeV} \\ \kappa &= 1.79 \end{aligned}$$

$$\begin{aligned}
c_3 &= 0.717 \text{ MeV} \\
c_4 &= 1.21129 \text{ MeV} \\
\delta &= -\frac{11}{\sqrt{A}} \text{ even - even} \\
&= 0 \text{ even - odd} \\
&= \frac{11}{\sqrt{A}} \text{ odd - odd}
\end{aligned} \tag{4.203}$$

The asymptotic value  $\tilde{a}$  is given by the expression

$$\tilde{a} = \alpha A + \beta A^{2/3} \tag{4.204}$$

in which we generally use the parameters

$$\alpha = 0.0666, \beta = 0.2587 \tag{4.205}$$

which we have obtained from a simultaneous fit to all  $D_0$  parameters of the RIPL library [36] using Eq. (4.200). The  $\alpha$  and  $\beta$  parameters can be changed with the **alphald** and **betald** keywords, see page 143.

If the level density parameter at the neutron separation energy  $a(S_n)$  is *not* known from an experimental  $D_0$  value, we use the following systematical formula for the shell damping parameter

$$\gamma = \frac{0.459}{A^{1/3}} \tag{4.206}$$

which was obtained in the same fit that led to Eq. (4.204). Eq. (4.206) is a special case of the general formula

$$\gamma = \frac{\gamma_1}{A^{1/3}} + \gamma_2 \tag{4.207}$$

that we have implemented, where the constants  $\gamma_1$  and  $\gamma_2$  can be adjusted with the **gammashell1** and **gammashell2** keywords, see 144.

In this case, all parameters in Eq. (4.201) are defined and  $a(E_x)$  can be completely computed at any excitation energy. However, for several nuclei  $a(S_n)$  can be derived from an experimental  $D_0$  value through Eq. (4.200), and one may want to use this information. In TALYS, this occurs when an input value for  $a(S_n)$  is given or when **asys n** is set (meaning that instead of using the systematical formulae (4.204)-(4.206) the resonance parameter database is used to determine level densities). If we want to use this “experimental”  $a(S_n)$  we are immediately facing a constraint: Eq. (4.201) gives the following condition that must be obeyed

$$a(S_n) = \tilde{a} \left[ 1 + \delta W \frac{1 - \exp(-\gamma(S_n - \Delta))}{S_n - \Delta} \right] \tag{4.208}$$

This means also that  $a(S_n)$ ,  $\tilde{a}$ ,  $\delta W$  and  $\gamma$  cannot *all* be given simultaneously in the input, since it would be inconsistent. In the case of an experimental  $a(S_n)$ , at least another parameter must be re-adjusted. The damping parameter  $\gamma$  is the first choice since we consider  $\delta W$  (directly derived from nuclear structure) and  $\tilde{a}$  (which should theoretically not deviate from the asymptotical smooth  $A$ -dependence of Eq. (4.204)) as more fundamental. Thus, if  $a(S_n)$  is given while  $\gamma$  is not given in the input, then we

again adopt the aforementioned systematical relations for  $\delta W$  and  $\tilde{a}$ , which then necessarily eliminates  $\gamma$  as a free parameter. It is obtained by inverting Eq. (4.208),

$$\gamma = -\frac{1}{S_n - \Delta} \ln \left[ 1 - \frac{S_n - \Delta}{\delta W} \left( \frac{\tilde{a}}{a(S_n)} - 1 \right) \right] \quad (4.209)$$

However, since both  $\delta W$  and  $a(S_n)$  are independently derived from experimental values, it may occur that Eq. (4.209) poses problems. In particular,  $\delta W$  may have a sign opposite to  $[a(S_n) - \tilde{a}]$ . In other words, if the argument of the natural logarithm is not between 0 and 1, our escape route is to return to Eq. (4.206) for  $\gamma$  and to readjust  $\delta W$  by inverting Eq. (4.208) in another way

$$\delta W = \frac{(S_n - \Delta) \left( \frac{a(S_n)}{\tilde{a}} - 1 \right)}{1 - \exp(-\gamma(S_n - \Delta))} \quad (4.210)$$

Finally, if both  $a(S_n)$  and  $\gamma$  are given in the input then a few possibilities are left. If  $\tilde{a}$  is also given, again Eq. (4.210) will be applied, otherwise, i.e. if  $\delta W$  is given instead or  $\tilde{a}$  and  $\delta W$  are both not given, the asymptotic level density parameter is obtained from

$$\tilde{a} = a(S_n) / \left[ 1 + \delta W \frac{1 - \exp(-\gamma(S_n - \Delta))}{S_n - \Delta} \right] \quad (4.211)$$

The recipe outlined above represents a full-proof method to deal with all the parameters of Eq. (4.201), i.e. it always gives a reasonable answer since we are able to invert the Ignatyuk formula in all possible ways. Care is however required since this flexibility gives rise to some peculiar calculation possibilities, such as Eq. (4.210) where the shell correction is re-calculated on the basis of level density parameters! We emphasize that in general, consistent calculations are obtained with Eqs. (4.202),(4.204),(4.206), and no experimental  $a(S_n)$ . In this case, the whole story below Eq. (4.206) is not relevant. The full range of possibilities of parameter specification for the Ignatyuk formula is summarized in Table 4.3. The reason to include all these parameter possibilities is simple: fitting experiments. Moreover, these variations are not as unphysical as they may seem: Regardless of whether they are derived from experimental data or from microscopic nuclear structure models, the parameters  $a(S_n)$ ,  $\tilde{a}$ ,  $\delta W$  and  $\gamma$  always have an uncertainty. Hence, as long as the deviation from their default values (assuming they are reasonable!) is kept within bounds, they can be helpful fitting parameters.

As a minor extra note, for small excitation energies the limiting value of Eq. (4.201) is given by its first order Taylor expansion

$$\lim_{U \rightarrow 0} a(E_x) = \tilde{a} [1 + \gamma \delta W] \quad (4.212)$$

which we use if  $U$  is around 0.

For level densities in which collective effects are not explicitly considered, we have included an option (through the **colldamp** parameter) to wash out the collective effects at high energies. For this, we multiply the asymptotic level density parameter  $\tilde{a}$  by a Fermi function as follows

$$\tilde{a}' = \frac{A/13}{1 + \exp(-(U - U_f)/C_f)} + \tilde{a} \left( 1 - \frac{1}{1 + \exp(-(U - U_f)/C_f)} \right) \quad (4.213)$$

where  $U_f$  and  $C_f$  are adjustable parameters. With this option, we use  $\tilde{a}'$  in the equations of this Section. In this way, the asymptotic limit is  $A/13$  instead of (roughly)  $A/8$ , as suggested by many authors (see e.g. Ref. [85]). A different approach is to use explicit collective enhancements, as governed by **ldmodel 2**, see later in this Section.

Table 4.3: Specification of parameter handling for Ignatyuk formula

Input	Calculation
- (Default)	$\gamma$ : Eq. (4.206), $\tilde{a}$ : Eq. (4.204), $\delta W$ : Eq. (4.202), $a(S_n)$ : Eq. (4.208)
$a(S_n), \gamma, \tilde{a}, \delta W$	TALYS-Error: Conflict
$a(S_n)$ (table), $\gamma, \tilde{a}, \delta W$	$a(S_n)$ : Eq. (4.208) (Input overruled)
$\gamma, \tilde{a}, \delta W$	$a(S_n)$ : Eq. (4.208)
$\gamma, \tilde{a}$	$\delta W$ : Eq. (4.202), $a(S_n)$ : Eq. (4.208)
$\gamma, \delta W$	$\tilde{a}$ : Eq. (4.204), $a(S_n)$ : Eq. (4.208)
$\tilde{a}, \delta W$	$\gamma$ : Eq. (4.206), $a(S_n)$ : Eq. (4.208)
$\gamma$	$\tilde{a}$ : Eq. (4.204), $\delta W$ : Eq. (4.202), $a(S_n)$ : Eq. (4.208)
$\tilde{a}$	$\gamma$ : Eq. (4.206), $\delta W$ : Eq. (4.202), $a(S_n)$ : Eq. (4.208)
$\delta W$	$\gamma$ : Eq. (4.206), $\tilde{a}$ : Eq. (4.204), $a(S_n)$ : Eq. (4.208)
$a(S_n)$	$\gamma$ : Eq. (4.209) or (4.206), $\tilde{a}$ : Eq. (4.204), $\delta W$ : Eq. (4.202) or (4.210)
$a(S_n), \tilde{a}, \delta W$	$\gamma$ : Eq. (4.209)
$a(S_n), \delta W$	$\tilde{a}$ : Eq. (4.204) $\gamma$ : Eq. (4.209)
$a(S_n), \tilde{a}$	$\delta W$ : Eq. (4.202), $\gamma$ : Eq. (4.209) or $\gamma$ : Eq. (4.206), $\delta W$ : Eq. (4.210)
$a(S_n), \gamma$	$\delta W$ : Eq. (4.202), $\tilde{a}$ : Eq. (4.211)
$a(S_n), \gamma, \delta W$	$\tilde{a}$ : Eq. (4.211)
$a(S_n), \gamma, \tilde{a}$	$\delta W$ : Eq. (4.210)

### Gilbert and Cameron Model

In the Gilbert and Cameron level density formulation [86], the excitation energy range is divided in a low energy part from zero to a matching energy  $E_M$  and a high energy part from  $E_M$  to infinity. Hence,

$$\begin{aligned}\rho^{tot}(E_x) &= \rho_T(E_x), \quad \text{if } E_x \leq E_M, \\ &= \rho_F(E_x), \quad \text{if } E_x \geq E_M\end{aligned}\quad (4.214)$$

For low excitation energy, the model is based on the experimental evidence that the cumulated histogram  $N(E_x)$  of the first discrete levels can be well reproduced by an exponential law of the type

$$N(E_x) = \exp\left(\frac{E_x - E_0}{T}\right) \quad (4.215)$$

which is called the constant temperature law. The nuclear temperature  $T$  and  $E_0$  are parameters that serve to adjust the formula to the experimental discrete levels. Accordingly, the constant temperature part of the total level density,  $\rho_T$ , reads

$$\rho_T(E_x) = \frac{1}{T} \exp\left(\frac{E_x - E_0}{T}\right) \quad (4.216)$$

for low excitation energies. Note that Eq. (4.216) is a special case of the general formula

$$\frac{1}{\tau} = \frac{d \ln \rho^{tot}(E_x)}{dE_x}, \quad (4.217)$$

namely when the logarithm of the total level density is given by a straight line.

For higher energies, the Fermi gas model is more suitable and the total level density is then given by Eq. (4.194). The expressions for  $\rho_T$  and  $\rho_F$  have to be matched at a matching energy  $E_M$  where they both give the same answer and where their derivatives are identical. First, continuity requires that

$$\rho_T(E_M) = \rho_F(E_M) \quad (4.218)$$

Inserting Eq. (4.216) in this equation directly leads to the condition

$$E_0 = E_M - T \ln [T \rho_F(E_M)] \quad (4.219)$$

Second, continuity of the derivatives requires that

$$\frac{d\rho_T}{dE_x}(E_M) = \frac{d\rho_F}{dE_x}(E_M) \quad (4.220)$$

Inserting Eq. (4.216) for the temperature part gives

$$\frac{\rho_T(E_M)}{T} = \frac{d\rho_F}{dE_x}(E_M) \quad (4.221)$$

or

$$\frac{1}{T} = \frac{d \ln \rho_F}{dE_x}(E_M) \quad (4.222)$$

We determine the temperature numerically on a sufficiently dense excitation energy grid. For simple Fermi gas type expressions Eq. (4.222) can be solved analytically, but we have chosen a completely numerical approach to allow any level density model to be used in the matching problem.

We now have two conditions, given by Eqs. (4.219) and (4.222), with three unknowns:  $T$ ,  $E_0$  and  $E_M$ . Hence, to obtain  $E_M$  we need another constraint. This can be obtained by considering that in the discrete level region, the constant temperature law should reproduce the experimental discrete levels. This condition can be fulfilled by requiring that  $\rho_T$  fits the discrete level scheme from a lower level  $N_L$  with energy  $E_L$  to an upper level  $N_U$  with energy  $E_U$ , i.e.

$$N_U = N_L + \int_{E_L}^{E_U} dE_x \rho_T(E_x) \quad (4.223)$$

or, after inserting Eq. (4.216),

$$N_U = N_L + \left[ \exp\left(\frac{E_U}{T}\right) - \exp\left(\frac{E_L}{T}\right) \right] \exp\left(\frac{-E_0}{T}\right) \quad (4.224)$$

The combination of Eqs. (4.219), (4.222) and (4.224) determines  $T$ ,  $E_0$  and  $E_M$ . Inserting (4.219) in (4.224) yields:

$$T \rho_F(E_M) \exp\left(\frac{-E_M}{T}\right) \left[ \exp\left(\frac{E_U}{T}\right) - \exp\left(\frac{E_L}{T}\right) \right] + N_L - N_U = 0 \quad (4.225)$$

which can be considered as an equation in  $E_M$ , from which  $E_M$  can be solved by an iterative procedure with the simultaneous utilisation of (4.222). The levels  $N_L$  and  $N_U$  should be chosen such that  $\rho_T(E_x)$  optimally describes the observed discrete states. We take  $N_L = 2$  for the lower state and read  $N_U$  from

Goriely's table (RIPL), whose  $N_U$  values were determined from microscopic level densities. If a value is not given in this table, we take  $N_U$  equal to the number of included discrete levels (usually 25).

Once the matching energy  $E_M$  has been defined, it is also necessary to define a spin distribution below  $E_M$ . For this purpose, a discrete spin cut-off factor  $\sigma_d^2$  is derived from the spins of the  $N_U$  discrete **levels** as follows.

The spin cut-off factor  $\sigma^2(U)$  can be formally defined for a given excitation energy  $U$  as

$$\sigma^2(U) = \sum_M M^2 \frac{\omega(U, M)}{\omega(U)} \quad (4.226)$$

where  $\omega(U)$  is the total **state** density and  $\omega(U, M)$  is the **state** density with a specified spin projection  $M$ . To calculate the discrete spin cut-off factor  $\sigma_d^2$  we approximate the formal expression of  $\omega$ ,

$$\omega(U) = \frac{dN_s(U)}{dU}, \quad (4.227)$$

where  $N_s(U)$  is the cumulated number of excited **states** of the nucleus up to the excitation energy  $U$ , writing

$$\omega(U) = \frac{N_s(E_U)}{E_U} \quad (4.228)$$

which is an acceptable approximation if  $E_U$  is small enough. In this case, one can replace Eq. (4.226) by

$$\sigma_d^2 = \frac{1}{N_s(E_U)} \sum_{M_d} N_s(E_U, M_d) M_d^2 \quad (4.229)$$

where the sum runs over all the projections  $M_d$  of the  $N_U$  discrete **levels** with spins  $J_i$  and  $N_s(E_U, M_d)$  is the number of **levels** in the energy interval  $[0, E_U]$  yielding a **state** with a projection  $M_d$ . Since each excited **level** with spin  $J$  yields  $2J + 1$  excited **states** with projections  $M_1 = -J, M_2 = -J + 1, \dots, M_{2J+1} = J$ , the total number of **states**  $N_s(E_U)$  reads

$$N_s(E_U) = \sum_{i=1}^{N_U} 2J_i + 1, \quad (4.230)$$

and the sum over  $M_d$  in Eq. (4.229) reads

$$\sum_{M_d} N_s(E_U, M_d) M_d^2 = \sum_{i=1}^{N_U} \sum_{M=-J_i}^{M=+J_i} M^2. \quad (4.231)$$

With the well know identity

$$\sum_{i=1}^N i^2 = \frac{1}{6} N(N+1)(2N+1), \quad (4.232)$$

we can finally determine  $\sigma_d^2$ , which reads

$$\sigma_d^2 = \frac{1}{3 \sum_{i=1}^{N_U} 2J_i + 1} \sum_{i=1}^{N_U} J_i(J_i + 1)(2J_i + 1) \quad (4.233)$$

The energy dependence of  $\sigma^2$  is then obtained by a linear interpolation between the value  $\sigma^2(\frac{1}{2}E_U) = \sigma_d^2$  and  $\sigma^2(E_M)$  given by Eq. (4.198).

For cases where either Eqs. (4.198) or (4.233) are not applicable, e.g. because there are no discrete levels and  $U = E_x - P$  is negative, we take the systematics of von Egidy et al. [87]

$$\sigma^2 = (0.98A^{0.23})^2 \quad (4.234)$$

which gives a reasonable estimate for energies in the order of 1-2 MeV.

#### 4.7.2 Collective effects in the level density

All the previously described models do not explicitly account for collective effects. However, it is well known that generally the first excited levels of nuclei result from coherent excitations of the fermions it contains. The Fermi gas model is not appropriate to describe such levels. Nevertheless, the models presented so far can still be applied successfully in most cases since they incorporate collectivity in the level density in an effective way through a proper choice of the energy-dependent level density parameter values.

In some calculations, especially if the disappearance of collective effects with excitation energy plays a role (e.g. in the case of fission), one would like to model the collective effects in more detail. It can be shown that the collective effects may be accounted for explicitly by introducing collective enhancement factors on top of an intrinsic level density so that  $\rho(U, J, \Pi)$  reads

$$\rho(U, J, \Pi) = K_{rot}(U)K_{vib}(U)\rho_{int}(U, J, \Pi). \quad (4.235)$$

$K_{rot}$  and  $K_{vib}$  are called the rotational and vibrational enhancement factors, respectively. The intrinsic level density, solely linked with single-particle excitations, is denoted by  $\rho_{int}(U, J, \Pi)$ . If  $K_{rot}$  and  $K_{vib}$  (described below) are explicitly accounted for,  $\rho_{int}(U, J, \Pi)$  can be determined again by using the Fermi gas level density formula. This time, however, it is evaluated with appropriate new values of the energy-dependent level density parameter  $a$  (Eqs. (4.201) and (4.204)), characterized by

$$\alpha' = 0.0564, \beta' = 0.0830, \gamma' = \frac{0.62}{A^{\frac{1}{3}}}. \quad (4.236)$$

These parameters result from a simultaneous fit to all  $D_0$  parameters of the RIPL library [36] through a combination of Eq. (4.200) and (4.235). For the spin cut-off parameter we use a somewhat different expression than Eq. (4.198), since it yields better  $D_0$ -fits:

$$\sigma^2 = c'A^{2/3} \sqrt{\frac{U}{a}} \quad (4.237)$$

with  $c' = 0.01389$ . This expressions and Eq. (4.198) are equivalent when the level density parameter is assumed to take the form of  $a = \frac{A}{6}$ .

The liquid drop model estimation of the vibrational collective enhancement factor is given by [85]

$$K_{vib}(U) = \exp\left(0.0555A^{\frac{2}{3}}T^{\frac{4}{3}}\right). \quad (4.238)$$

This factor is deformation independent and varies with the nuclear temperature,

$$T = \sqrt{U/a}, \quad (4.239)$$

and mass only.

The most important contribution to the collective enhancement of the level density originates from rotational excitations. Its effect is not only much stronger ( $K_{rot} \sim 10 - 100$  whereas  $K_{vib} \sim 3$ ), but the form for the rotational enhancement depends on the nucleus shape as well. This makes it crucial for the description of fission cross sections.

According to a study by Iljinov *et al.* [85] the best phenomenological description of the asymptotic level density parameter is obtained when assuming the presence of a rotational enhancement factor even for nuclei with a small ground-state deformation. Furthermore, dynamical excitations may cause even spherical nuclides to exhibit properties of deformed nuclides. Hence, TALYS includes  $K_{rot}$  for all nuclei irrespective of their ground-state deformation.

We use two expressions for the rotational enhancement factor, depending on the deformation [36, 88]. Ground-state deformations, subactinide barriers, inner barriers of actinides with neutron number  $N \leq 144$ , and all outer barriers are assumed to be axially symmetric by default,

$$K_{rot}(U) = K_{rot}^{sym}(U, \beta_2) = \begin{cases} (\sigma_{\perp}^2 - 1)f(U) + 1 & \text{for } \sigma_{\perp}^2 > 1, \\ 1 & \text{for } \sigma_{\perp}^2 \leq 1. \end{cases} \quad (4.240)$$

The inner saddle points of actinides with  $N > 144$  are taken to be axially asymmetric,

$$K_{rot}(U) = K_{rot}^{asym}(U, \beta_2) = \begin{cases} (2\sqrt{2\pi}\sigma_{\perp}^2\sigma_{\parallel} - 1)f(U) + 1 & \text{for } 2\sqrt{2\pi}\sigma_{\perp}^2\sigma_{\parallel} > 1, \\ 1 & \text{for } 2\sqrt{2\pi}\sigma_{\perp}^2\sigma_{\parallel} \leq 1. \end{cases} \quad (4.241)$$

Additionally, we apply an extra factor of 2 to Eq. (4.241) for the outer barrier, due to the mass asymmetry.

In these equations, the spin-cutoff parameter  $\sigma_{\perp}^2$  is given by

$$\sigma_{\perp}^2 = \frac{\mathfrak{S}_{\perp}T}{\hbar^2}, \quad (4.242)$$

with the rigid-body moment of inertia perpendicular to the symmetry axis given by

$$\mathfrak{S}_{\perp} = \frac{2}{5}m_0AR^2\left(1 + \frac{\beta_2}{3}\right). \quad (4.243)$$

$R = 1.2A^{\frac{1}{3}}$  is the nuclear radius,  $m_0$  is the mass unit (*amu*) and  $\beta_2$  is the ground-state quadrupole deformation, generally taken from the Möller database, see Chapter 5. The spin distribution parameter  $\sigma_{\parallel}^2$  is defined as

$$\sigma_{\parallel}^2 = \frac{6}{\pi^2} \langle m^2 \rangle a \left(1 - \frac{2\beta_2}{3}\right) T, \quad (4.244)$$

with  $\langle m^2 \rangle = 0.24A^{\frac{2}{3}}$  the average value of the squared projection of the angular momentum of the single-particle states on the symmetry axis. In the case of fission,  $\beta_2$  is assumed to be 0.6 for the inner barrier and 0.8 for the outer barrier. For the ground-state,  $\beta_2$  vanishes with T:

$$\beta_2(T) = \frac{\beta_2(0)}{1 + \exp\left(\frac{(T-2.0)}{0.5}\right)}. \quad (4.245)$$

and this  $T$ -dependence needs to be taken into account accordingly in Eqs. 4.243 and 4.244. The contribution of dynamical deformation at higher  $l$ -values is not built into TALYS.

For high excitation energies, it is known that the collective behavior vanishes. The function  $f(U)$ , responsible for this damping effect in the definition of  $K_{rot}^{sym}$  and  $K_{rot}^{asym}$ , is assumed to be a Fermi function [88]

$$f(u) = \frac{1}{1 + \exp\left(\frac{U - U_{col}^{g.s./B_f}}{d_{col}^{g.s./B_f}}\right)} \quad (4.246)$$

When inserted into Eqs. (4.240) and (4.241) this function yields the desired property of  $K_{rot}$  going to 1 for high temperatures. The parameters  $U_{col}^{g.s./B_f}$  and  $d_{col}^{g.s./B_f}$  may be used as a fit parameter in fission cross section calculations. In general, different values are assigned for the ground state and on top of the fission barriers. The default values are  $U_{col}^{g.s.} = 30.$ ,  $d_{col}^{g.s.} = 10.$ ,  $U_{col}^{B_f} = 45.$ ,  $d_{col}^{B_f} = 10.$ .

### 4.7.3 Microscopic level densities

Besides the phenomenological models that are used in TALYS, there is also an option to employ more microscopic approaches. For the RIPL database, S. Goriely has calculated level densities from drip line to drip line on the basis of Hartree-Fock calculations [89] for excitation energies up to 150 MeV and for spin values up to  $I = 30$ . If **ldmodel 3**, see page 142, these tables with microscopic level densities can be read. To add some fitting flexibility, there is a possibility to multiply the tabulated level densities with a scaling function, i.e.

$$\rho(E_x, J, \pi) = c_1 \exp(c_2 \sqrt{E_x}) \rho_{micro}(E_x, J, \pi) \quad (4.247)$$

where by default  $c_1 = 1.$  and  $c_2 = 0.$  (i.e. unaltered values from the tables).

## 4.8 Fission

### 4.8.1 Fission transmission coefficients

For fission, the default model implemented in TALYS is based on the transition state hypothesis of Bohr and the Hill-Wheeler expression. This yields transmission coefficients that enter the Hauser-Feshbach model to compete with the particle and photon transmission coefficients.

### Transmission coefficient for one fission barrier

The Hill-Wheeler expression gives the probability of tunneling through a barrier with height  $B_f$  and width  $\hbar\omega_f$  for a compound nucleus with excitation energy  $E_x$ . It reads

$$T_f(E_x) = \frac{1}{1 + \exp\left[-2\pi \frac{(E_x - B_f)}{\hbar\omega_f}\right]} \quad (4.248)$$

For a transition state with excitation energy  $\varepsilon_i$  above the top of the same barrier, one has

$$T_f(E_x, \varepsilon_i) = \frac{1}{1 + \exp\left[-2\pi \frac{(E_x - B_f - \varepsilon_i)}{\hbar\omega_f}\right]} \quad (4.249)$$

which means that the barrier is simply shifted up by  $\varepsilon_i$ .

For a compound nucleus with excitation energy  $E_x$ , spin  $J$ , and parity  $\Pi$ , the total fission transmission coefficient is the sum of the individual transmissions coefficients for each barrier through which the nucleus may tunnel, and thus reads in terms of the previously introduced  $T_f(E_x, \varepsilon_i)$

$$T_f^{J,\Pi}(E_x) = \sum_i T_f(E_x, \varepsilon_i) f(i, J, \Pi) + \int_{E_{th}}^{E_x} \rho(\varepsilon, J, \Pi) T_f(E_x, \varepsilon) d\varepsilon \quad (4.250)$$

The summation runs over all discrete transition states on top of the barrier and  $E_{th}$  marks the beginning of the continuum. In this equation,  $f(i, J, \Pi) = 1$  if the spin and parity of the transition state equal that of the compound nucleus and 0 otherwise. Moreover,  $\rho(\varepsilon, J, \Pi)$  is the level density of fission channels with spin  $J$  and parity  $\Pi$  for an excitation energy  $\varepsilon$ . The main difference with the usually employed expressions is that the upper limit in the integration is finite. This expression also enables to define the number of fission channels by replacing  $T_f(E_x, \varepsilon_i)$  by 1 in Eq. (4.250). This is needed for width fluctuation calculations where the fission transmission coefficient is treated as a continuum transmission coefficient.

### 4.8.2 Transmission coefficient for multi-humped barriers

For double humped barriers, the generally employed expression is based on an effective transmission coefficient  $T_{eff}$  defined by

$$T_{eff} = \frac{T_A T_B}{T_A + T_B} \quad (4.251)$$

where  $T_A$  and  $T_B$  are the transmission coefficients for barrier  $A$  and  $B$  respectively, calculated with Eq. (4.250).

If a triple humped barrier needs to be considered, the expression for  $T_{eff}$  reads

$$T_{eff} = \frac{T_{AB} T_C}{T_{AB} + T_C} \quad (4.252)$$

where  $T_{AB}$  is given by Eq. (4.251). Consequently, the expression used in TALYS reads

$$T_{eff} = \frac{T_A T_B T_C}{T_A T_B + T_A T_C + T_B T_C} \quad (4.253)$$

For any number of barrier, the effective number of fission channels is calculated as in the case for one barrier [6].

### 4.8.3 Class II/III states

Class II (resp. III) states may be introduced when double (resp. triple) humped barriers are considered. In the particular situation where the excitation energy  $E_{CN}$  of the compound nucleus is lower than the barrier heights, fission transmission coefficients display resonant structures which are due to the presence of nuclear excited levels (Class II) in the second, or in the third (Class III) well of the potential energy surface. When such resonant structures occur, the expression for the effective fission transmission coefficient has to be modified (generally enhanced).

The way this resonant effect is determined depends on the number of barriers that are considered.

#### Double humped fission barrier

In the case where two barriers occur, the effective fission transmission coefficient  $T_{eff}$  can be written as

$$T_{eff} = \frac{T_A T_B}{T_A + T_B} \times F_{AB}(E_{CN}) \quad (4.254)$$

where  $F_{AB}(E_{CN})$  is a factor whose value depends on the energy difference between the excitation energy of the nucleus and that of the a class II state located in the well between barrier  $A$  and  $B$ . It has been shown [90] that the maximum value of  $F_{AB}(E)$  reaches  $\frac{4}{T_A + T_B}$  and gradually decreases over an energy interval defined as the width  $\Gamma_{II}$  of the class II state with excitation energy  $E_{II}$ . This is accounted for using the empirical quadratic expression

$$F_{AB}(E) = \frac{4}{T_A + T_B} + \left( \frac{E - E_{II}}{0.5\Gamma_{II}} \right)^2 \times \left( 1 - \frac{4}{T_A + T_B} \right) \quad (4.255)$$

if  $E_{II} - 0.5\Gamma_{II} \leq E \leq E_{II} + 0.5\Gamma_{II}$  and  $F_{AB} = 1$  otherwise.

Theoretically, this expression is valid for the tunneling through a single double humped barrier whereas in realistic situations, both  $T_A$  and  $T_B$  are obtained from a summation over several transition states. One may thus have large  $T_A$  and  $T_B$  values so that Eq. 4.255 may give  $F_{AB}(E) \leq 1$ . Such a situation can only occur for high enough excitation energies for which the individual Hill-Wheeler contributions in Eq. (4.250) are large enough. However, in TALYS, we only consider class II states with excitation energies lower than the height of the first barrier. Consequently, the resonant effect can only occur if the compound nucleus energy  $E_{CN}$  is (i) lower than the top of the first barrier and (ii) close to a resonant class II state ( $E_{II} - 0.5\Gamma_{II} \leq E_{CN} \leq E_{II} + 0.5\Gamma_{II}$ ). With such requirements, the individual Hill-Wheeler terms are clearly small, and  $T_A + T_B \ll 1$ .

#### Triple humped fission barrier

If three barriers  $A$ ,  $B$  and  $C$  are considered, the situation is more complicated. In this case, three situations can occur depending on the positions of the class II and class III states. Indeed the enhancement can be due either to a class II state or to a class III state, but on top of that, a double resonant effect can also occur if both a class II and a class III state have an excitation energy close to the compound nucleus energy. For any situation, the enhancement is first calculated for the first and the second barrier giving the transmission coefficient

$$T_{eff}^{AB} = T_{AB} \times F_{AB} \quad (4.256)$$

with  $F_{AB}$  given by Eq. (4.255) as in the previous case.

Next, the eventual coupling with a class III state with energy  $E_{III}$  of width  $\Gamma_{III}$  is accounted for by generalizing Eq. (4.254) writing

$$T_{eff}^{ABC} = \frac{T_{eff}^{AB} T_C}{T_{eff}^{AB} + T_C} \times F_{ABC}(E_{CN}) \quad (4.257)$$

where  $F_{ABC}(E_{CN})$  is given by generalizing Eq. (4.255) writing

$$F_{ABC}(E) = \frac{4}{T_{eff}^{AB} + T_C} + \left( \frac{E - E_{III}}{0.5\Gamma_{III}} \right)^2 \times \left( 1 - \frac{4}{T_{eff}^{AB} + T_C} \right) \quad (4.258)$$

if  $E_{III} - 0.5\Gamma_{III} \leq E \leq E_{III} + 0.5\Gamma_{III}$  and  $F_{ABC} = 1$  otherwise.

#### 4.8.4 Fission barrier parameters

In TALYS several options are included for the choice of the fission barrier parameters:

1. Experimental parameters [36]: collection of a large set of actinide fission barrier heights and curvatures for both the inner and outer barrier based on a fit to experimental data, compiled by V. Maslov. Moreover, this compilation contains head band transition states.
2. Mamdouh parameters [93]: set of double-humped fission barrier heights for numerous isotopes derived from Extended Thomas-Fermi plus Strutinsky Integral calculations.
3. Rotating-Finite-Range Model (RFRM) by Sierk [91]: single-humped fission barrier heights are determined within a rotating liquid drop model, extended with finite-range effects in the nuclear surface energy and finite surface-diffuseness effects in the Coulomb energy.
4. Rotating-Liquid-Drop Model (RLDM) by Cohen *et al* [92].

In the current version of TALYS, the dependence on angular momentum of the fission barriers is discarded. If LDM barriers are employed in the calculation, they are corrected for the difference between the ground-state and fission barrier shell correction energy:

$$B_f^{LDM}(T) = B_f^{LDM}(0) - (\delta W_{groundstate} - \delta W_{barrier}) * g(T) \quad (4.259)$$

This correction gradually disappears with temperature due to the washing out of the shell effects [94]:

$$g(T) = \begin{cases} 1 & \text{for } T < 1.65\text{MeV}, \\ g(T) = 5.809 \exp(-1.066 T) & \text{for } T \geq 1.65\text{MeV}. \end{cases} \quad (4.260)$$

Shell corrections on top of the fission barrier are generally unknown. They obviously play an important role for the level density as well. Default values are adopted: for subactinides  $\delta W_{barrier} = 0$  MeV, for actinides  $\delta W_{barrier,inner} = 2.5$  MeV and  $\delta W_{barrier,outer} = 0.6$  MeV [36].

### 4.8.5 Fission fragment properties

The description of fission fragment and product yields follows the procedure outlined in Ref. [96]. The Hauser-Feshbach formalism gives a fission cross section per excitation energy bin for each fissioning system. The fission fragment masses and charges are, subsequently, determined per given excitation energy bin  $E_x$ , in a fissioning system FS, characterised by  $(Z_{FS}, A_{FS}, E_x)$ , for which the fission cross section exceeds some minimum value. The total fragment mass distribution is given by a sum over all contributing bins weighted with the corresponding fission cross sections:

$$\sigma(A_{FF}) = \sum_{Z_{FS}, A_{FS}, E_x} \sigma_f(Z_{FS}, A_{FS}, E_x) Y(A_{FF}; Z_{FS}, A_{FS}, E_x), \quad (4.261)$$

where  $Y(A_{FF}; Z_{FS}, A_{FS}, E_x)$  is the relative yield of a fission fragment with mass  $A_{FF}$  originating from a fissioning system. Combining this expression with the result of a fission fragment charge distribution calculation yields the final production cross section of a fission fragment with mass  $A_{FF}$  and charge  $Z_{FF}$ :

$$\begin{aligned} \sigma_{prod}(Z_{FF}, A_{FF}) = & \sum_{Z_{FS}, A_{FS}, E_x} \sigma_f(Z_{FS}, A_{FS}, E_x) Y(A_{FF}; Z_{FS}, A_{FS}, E_x) \\ & \times Y(Z_{FF}; A_{FF}, Z_{FS}, A_{FS}, E_x) \end{aligned} \quad (4.262)$$

$Y(Z_{FF}; A_{FF}, Z_{FS}, A_{FS}, E_x)$  is the relative yield of a fission fragment with charge  $Z_{FF}$  given its mass  $A_{FF}$  and the fissioning system characterised by  $(Z_{FS}, A_{FS}, E_x)$ .

In general, an excitation energy distribution is connected to these fission *fragment* production cross sections. In theory, this could be used to deduce the fission *product* yields through a full evaporation calculation of the fission fragments. This is not yet possible in TALYS. Instead a rather crude approximation, outlined later in this section, is adopted to estimate the number of post-scission neutrons emitted from each fragment. This procedure leads to relative yields for the fission product masses  $Y(A_{FP}; Z_{FS}, A_{FS}, E_x)$  and charges  $Y(Z_{FP}; A_{FP}, Z_{FS}, A_{FS}, E_x)$  and, hence, to expressions similar to Eq. (4.261) and Eq. (4.262) for the final fission products.

#### Fission fragment mass distribution

The fission fragment mass distribution is determined with a revised version of the multi-modal random neck-rupture model (MM-RNRM). The original model has been developed by Brosa to calculate properties of fission fragments at zero temperature [95]. However, fission calculations within TALYS require fragment mass distributions up to higher temperatures.

In the recent version of the model [96] the temperature is added to the calculation of the potential energy landscape of the nucleus. A search for the fission channels in deformation space yields the superlong (SL), standard I (ST I), and standard II (ST II) fission barriers and pre-scission shapes as a function of temperature. In this manner, the incorporated melting of shell effects naturally gives rise to the vanishing of the asymmetric fission modes ST I and ST II with increasing excitation energies. The obtained temperature-dependent fission barrier and pre-scission shape parameters serve as input for the fragment mass distribution computations in TALYS.

Each mass distribution is a sum over contributions of the three dominant fission modes FM:

$$Y(A_{FF}; Z_{FS}, A_{FS}, E_x) = \sum_{FM=SL, STI, STII} W_{FM}(Z_{FS}, A_{FS}, E_x) Y_{FM}(A_{FF}; Z_{FS}, A_{FS}, E_x), \quad (4.263)$$

where  $W_{FM}(Z_{FS}, A_{FS}, E_x)$  denotes the weight of a fission mode, and  $Y_{FM}(A_{FF}; Z_{FS}, A_{FS}, E_x)$  is the corresponding mass distribution.  $Y(A_{FF}; Z_{FS}, A_{FS}, E_x)$  can then be substituted in Eq. (4.261) to determine the full fission fragment mass distribution for the reaction under consideration. An analogous expression can be written down for  $Y(A_{FP}; Z_{FS}, A_{FS}, E_x)$ .

Each mass distribution calculation is started by determining the relative contributions of the different fission modes. These are evaluated with the Hill-Wheeler penetrability through inverted parabolic barriers using temperature-dependent barrier parameters and, consequently (the reader is referred to [96] for a detailed explanation), ground-state level densities:

$$T_{f,FM}(Z_{FS}, A_{FS}, E_x) = \int_0^\infty d\epsilon \rho_{gs}(Z_{FS}, A_{FS}, \epsilon) \frac{1}{1 + \exp \left[ \frac{2\pi(B_{f,FM}(Z_{FS}, A_{FS}, T(\epsilon)) + \epsilon - E_x)}{\hbar\omega_{f,FM}(Z_{FS}, A_{FS}, T(\epsilon))} \right]}. \quad (4.264)$$

All actinides encounter a double-humped barrier on their way to fission. The effective transmission coefficient can be expressed in terms of the transmission coefficient through the first and second barrier denoted by  $T_f^A$  and  $T_f^B$  respectively by Eq. (4.251). Since, however, the theoretical inner barrier is much lower than the outer barrier, the relative contribution  $W_{FM}(Z_{FS}, A_{FS}, E_x)$  of the three fission modes may simply be determined by an equation of the following form:

$$W_{SL}(Z_{FS}, A_{FS}, E_x) = \frac{T_{f,SL}^B}{T_{f,SL}^B + T_{f,STI}^B + T_{f,STII}^B}. \quad (4.265)$$

Equivalent formulas hold for  $W_{STI}(Z_{FS}, A_{FS}, E_x)$  and  $W_{STII}(Z_{FS}, A_{FS}, E_x)$ .

For subactinides it is not possible to calculate the competition between symmetric and asymmetric fission modes, since the computed fission channels exhibit rather broad and strangely shaped outer barriers, which makes a parabola fit to these barriers impossible. Hence, the Hill-Wheeler approach cannot be applied. Fortunately, the SL barriers are much lower than the ST barriers. Therefore, in all these calculations the asymmetric fission modes are simply discarded and the dominant symmetric SL mode is solely taken into account for subactinides.

The RNRM is employed to calculate the mass distribution per fission mode. An extensive description of the RNRM may be found in [95]. Here it is merely attempted to communicate its main ideas. In this model, the fission process is regarded as a series of instabilities. After the passage over the barriers, a neck starts to form. If this neck becomes flat its rupture may happen anywhere, which means that the point of future constriction can shift over the neck. This motion of the dent is called the shift instability. In the instant that the Rayleigh instability starts to deepen the dent, the position of the asymmetry is frozen and rupture is taking place. The RNRM translates the effect of both mechanisms into measurable quantities.

In order for the shift instability to do its work, a perfectly flat neck is required. Hence, the so-called flat-neck parameterisation is introduced: (see Fig. 4.3):

$$\rho(\zeta) = \begin{cases} (r_1^2 - \zeta^2)^{1/2} & -r_1 \leq \zeta \leq \zeta_1 \\ r + a^2 c \left( \cosh \left( \frac{\zeta - \zeta_1 + l - r_1}{a} \right) - 1 \right) & \zeta_1 \leq \zeta \leq \zeta_2 \\ (r_2^2 - (2l - r_1 - r_2 - \zeta)^2)^{1/2} & \zeta_2 \leq \zeta \leq 2l - r_1. \end{cases} \quad (4.266)$$

The radius of the nucleus is given by  $\rho$  as a function of a parameter  $\zeta$  in terms of several parameters: the semilength  $l$ , the neck radius  $r$ , the position  $z$  of the dent, the curvature  $c$ , the extension of the neck  $a$ , the

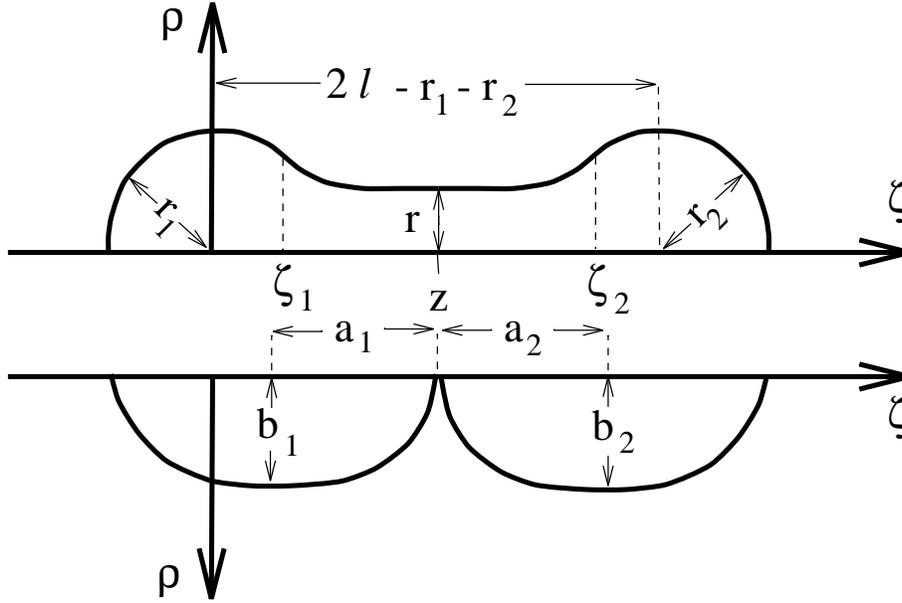


Figure 4.3: The upper part illustrates the flat-neck representation. The lower part contains the embedded spheroids parameterisation.

radii of the spherical heads  $r_1$  and  $r_2$ , and the transitional points  $\zeta_1$  and  $\zeta_2$ . By requiring continuity and differentiability of the shape, volume conservation and a minimal value of  $c$  for a really flat neck, only  $(l, r, z)$  remain as independent parameters. Subsequently, the neck radius is eliminated by the Rayleigh criterion, which relates the total length  $2l$  of the precission shape to the neck radius  $r$  by  $2l = 11r$ . The value of  $z$  can be transformed into the heavy fragment mass  $A_h$  by:

$$A_h = \frac{3A}{4r_{cn}^3} \int_{-l}^z \rho^2(\zeta) d\zeta, \quad (4.267)$$

where  $r_{cn}$  is the compound nucleus radius. The actual values of  $A_h$  and  $l$  originate from the channel searches and are called the precission shape parameters. They have been stored in the structure database and are input to the RNRM calculations.

One last ingredient is missing for the computation of the mass distribution, namely the surface tension:

$$\gamma_0 = 0.9517 \left( 1 - 1.7828 \left( \frac{N - Z}{A} \right)^2 \right) \text{MeV fm}^{-2}. \quad (4.268)$$

This is taken from the LDM by Myers and Swiatecki [73].

Fluctuations amplified by the shift instability alter the shape slightly and enable the rupture of the nucleus to take place at another point than the most probable point  $z$ . In order to determine the fission-fragment mass distribution, the probability of cutting the neck at an arbitrary position  $z_r$  has to be calculated. This probability is given by the change in potential energy from  $z_r$  to  $z$ :  $E(z_r) - E(z)$ . This is replaced by the energy to cut the nucleus at the two positions:  $E_{cut}(z_r) - E_{cut}(z)$ , with  $E_{cut}(z_r) =$

$2\pi\gamma_0\rho^2(z_r)$ . The rupture probability is now proportional to the Boltzmann factor:

$$y(A_{FF}) \propto \exp\left(\frac{-2\pi\gamma_0(\rho^2(z_r) - \rho^2(z))}{T}\right). \quad (4.269)$$

The fragment mass number  $A_{FF}$  can be computed according to the analogue of Eq. (4.267):

$$A_{FF}(z_r) = \frac{3A}{4r_{cn}^3} \int_{-l}^{z_r} \rho^2(\zeta) d\zeta. \quad (4.270)$$

The theoretical yield is finally determined with the following relation in which  $Y(A_{FF})$  stands for the normalised fission fragment mass yield:

$$Y_{FM}(A_{FF}; Z_{FS}, A_{FS}, E_x) = y(A_{FF}) + y(A - A_{FF}). \quad (4.271)$$

In Eq. (4.269) the temperature of the scissioning nucleus must be provided. All calculations of the PES and the crossing of the fission barriers have been isothermal. However, for the RNRM the loss and gain of excitation energy in crossing the barrier is taken into account into a new excitation energy and temperature at scission:

$$E_x^{scission} = E_x^{groundstate} + F_{def,scission}. \quad (4.272)$$

The new excitation energy has two components: the original excitation energy in the ground state  $E_x^{groundstate}$  and the deformation energy at scission  $F_{def,scission}$ .  $F_{def,scission}$  is positive for actinides and becomes negative in the subactinide region. The new excitation energy is related to a new temperature  $T_{scission}$ . However, a new prescission temperature corresponds to a different prescission shape with a somewhat different value for  $F_{def,scission}$ . Therefore, the temperature  $T_{scission}$  has to be determined in a self-consistent manner together with the final prescission shape. If a prescission shape has a high temperature or a very long neck, the mass distribution will be broad. Low temperatures and short necks result in a narrow mass distribution.

### Post-scission neutron multiplicities

The mass distribution calculated above belongs to the primary fission fragments. Most fragments, however, are highly excited directly after their creation. They take their share of total excitation energy available at scission (4.272). Moreover, they are strongly deformed, which manifests itself in an extra amount of excitation energy set free when this deformation relaxes towards the ground-state deformation of the fragments by the strong surface tension. The superfluous excitation energy is released during the process of post-scission neutron and gamma emission. The neutron emission is responsible for a shift of the pre-neutron emission mass distribution to somewhat smaller masses.

The total excitation energy in a newly created fragment with mass  $A_{FF}$  results from:

$$E_x^{fragment}(A_{FF}) = E_{def,fragment}(A_{FF}) + \frac{A_{FF}}{A} E_x^{scission}. \quad (4.273)$$

$E_{def,fragment}(A_{FF})$  denotes the deformation energy of the fragment, and the second term contains the portion of the thermal energy at scission of the whole fissioning system picked up by the fragment. The assumption is that the fragment receives a share proportional to its mass.

For the calculation of  $E_{def,fragment}(A_{FF})$  another shape parameterisation is employed: the embedded spheroids (see Fig. 4.3). The newborn fragments are modeled as two contacting spheroids with major axes  $a_1$  and  $a_2$ , which are linked to  $2l$  and  $z_r$  by:

$$a_1 = \frac{1}{2}(r_1 + z_r), \quad a_2 = l - \frac{1}{2}(r_1 + z_r). \quad (4.274)$$

The minor axes  $b_1$  and  $b_2$  follow from volume conservation:

$$b_1^2 = \frac{3}{4a_1} \int_{-r_1}^{z_r} \rho^2 d\zeta, \quad b_2^2 = \frac{3}{4a_2} \int_{z_r}^{2l-r_1} \rho^2 d\zeta. \quad (4.275)$$

The energy difference of the spheroidally deformed and the spherical fragment  $E_{def,fragment}(A_{FF})$  is given by:

$$\begin{aligned} E_{def,fragment}(A_{FF}, \epsilon) &= E_{surf}^{sph}(A_{FF}) \left( \frac{\arcsin(\epsilon) + \epsilon(1 - \epsilon^2)^{1/2}}{2\epsilon(1 - \epsilon^2)^{1/6}} - 1 \right) + \\ &E_{Coul}^{sph}(A_{FF}) \left( \frac{(1 - \epsilon^2)^{1/3}}{2\epsilon} \ln \left( \frac{1 + \epsilon}{1 - \epsilon} \right) - 1 \right). \end{aligned} \quad (4.276)$$

The eccentricity is defined as:

$$\epsilon_i = \left( 1 - \left( \frac{b_i}{a_i} \right)^2 \right)^{1/2}, \quad (4.277)$$

and  $E_{surf}^{sph}(A_{FF})$  and  $E_{Coul}^{sph}(A_{FF})$  represent the LDM surface and the Coulomb energy of a spherical nucleus obtained from Ref. [97].

The neutron multiplicity  $\nu_{FM}(A_{FF})$  for a fragment with mass  $A_{FF}$  is now derived by finding the root of the following relation:

$$E_x^{fragment}(A_{FF}) = \sum_{n=1}^{\nu_{FM}(A_{FF})} (S_n + \eta_n) + E_\gamma. \quad (4.278)$$

The separation energy  $S_n$  is calculated from the mass formula [97]. The average kinetic energy of the neutrons is taken to be  $\frac{3}{2}$  times the fragment temperature, and the energy carried off by  $\gamma$ -rays  $E_\gamma$  is approximately half the separation energy of the first non-evaporated neutron.

The final fission product mass yield per fission mode is given by:

$$Y_{FM}(A_{FP}; Z_{FS}, A_{FS}, E_x) = Y_{FM}(A_{FF} - \nu_{FM}(A_{FF})) + Y_{FM}(A - A_{FF} - \nu_{FM}(A - A_{FF})). \quad (4.279)$$

### Fission fragment charge distribution

Unfortunately, the MM-RNRM only yields information on the mass yields of the fission fragments. Predictions of charge distributions are performed in TALYS within a scission-point-model-like approach (Wilkins *et al.* [98]). Corresponding to each fission fragment mass  $A_{FF}$  a charge distribution is computed

using the fact that the probability of producing a fragment with a charge  $Z_{FF}$  is given by the total potential energy of the two fragment system inside a Boltzmann factor:

$$Y_{FM}(Z_{FF}; A_{FF}, Z_{FS}, A_{FS}, E_x) = \frac{\exp\left(\frac{-E(Z_{FF}, A_{FF}, Z, A)}{T}\right)}{\sum_{Z_{FF_i}} \exp\left(\frac{-E(Z_{FF_i}, A_{FF}, Z, A)}{T}\right)} \quad (4.280)$$

In the original scission-point model this potential energy is integrated over all deformation space. Within the MM-RNRM, however, fission channel calculations already define the deformation at the scission point. Furthermore, a strong coupling between the collective and single particle degrees of freedom is assumed near the scission point. This means that the nucleus is characterised by a single temperature  $T$ .

The potential energy for the creation of one fragment with  $(Z_{FF}, A_{FF})$  and a second fragment with  $(Z - Z_{FF}, A - A_{FF})$  consists of a sum over the binding energy of the deformed fragments by the droplet model without shell corrections and their mutual Coulomb repulsion energy as well as the nuclear proximity repulsion energy:

$$E(Z_{FF}, A_{FF}, Z, A) = B(Z_{FF}, A_{FF}) + B(Z - Z_{FF}, A - A_{FF}) + E_{Coul} + V_{prox}. \quad (4.281)$$

The single constituents of this formula are defined by the following relations:

$$B(Z_{FF}, A_{FF}) = -a_1 \left[ 1 - \kappa \left( \frac{A_{FF} - 2Z_{FF}}{A_{FF}} \right)^2 \right] A_{FF} \quad (4.282)$$

$$+ a_2 \left[ 1 - \kappa \left( \frac{A_{FF} - 2Z_{FF}}{A_{FF}} \right)^2 \right] A_{FF}^{\frac{2}{3}} f(shape)$$

$$+ \frac{3}{5} \frac{e^2}{r_0} \frac{Z_{FF}^2}{A_{FF}^{\frac{1}{3}}} g(shape) - \frac{\pi^2 e^2}{2 r_0} \left( \frac{d}{r_0} \right)^2 \frac{Z_{FF}^2}{A_{FF}} \quad (4.283)$$

$$E_{Coul} = e^2 Z_{FF} (Z - Z_{FF}) S_{form} / (a_1 + a_2) \quad (4.284)$$

$$V_{prox} = -1.7817 \frac{4\pi \gamma_0 b_1^2 b_2^2}{a_1 b_2^2 + a_2 b_1^2} \quad (4.285)$$

The parameters in the binding energy formula are taken from Ref. [97]. The function  $f(shape)$  is the form factor for the Coulomb term whereas  $g(shape)$  denotes the form factor for the surface energy.  $S_{form}$  is the form factor for the Coulomb interaction energy between two spheroids.

The fission product charge distribution is obtained from the calculated fission fragment charge distribution by shifting the corresponding fragment masses  $A_{FF}$  to the fission product masses  $A_{FP}$  with the aid of the post-scission neutron multiplicity  $\nu_{FM}(A_{FF})$ :

$$Y_{FM}(Z_{FP}; A_{FP}, Z_{FS}, A_{FS}, E_x) = Y_{FM}(Z_{FF}; A_{FF} - \nu_{FM}(A_{FF}), Z_{FS}, A_{FS}, E_x). \quad (4.286)$$

Since proton evaporation of the fission fragments is neglected, the charge distribution connected with  $A_{FF}$  becomes simply linked to the fission product mass  $A_{FP}$ .

## 4.9 Thermal reactions

The Introduction states that TALYS is meant for the analysis of data in the 1 keV - 200 MeV energy region. The lower energy of 1 keV should not be taken too literally. More accurate is: above the resolved

resonance range. The start of the unresolved resonance range differs from nucleus to nucleus and is related to the average resonance spacing  $D_0$  or, equivalently, the level density at the binding energy. Generally, the starting energy region is higher for light nuclides than for heavy nuclides. Only beyond this energy, the optical and statistical models are expected to yield reasonable results, at least for the non-fluctuating cross sections. The lower energies are the domain of R-matrix theory, which describes the resonances. Nevertheless, it would be useful to have a first-order estimate of the non-threshold reactions, not only for the obvious neutron capture channel, but also for the exothermal  $(n, p)$ ,  $(n, \alpha)$  and fission channels. The fact that a nuclear model calculation in TALYS is only performed down to about 1 keV should not prevent us to give at least an estimate of the  $1/v$ -like behaviour of the excitation function down to  $10^{-5}$  eV (the lower energy limit in ENDF-6 files). In collaboration with J. Kopecky, we constructed a method that provides this.

### 4.9.1 Capture channel

First, we decide on the lower energy of validity of a TALYS nuclear model calculation  $E_L$ . Somewhat arbitrarily, we set as default  $E_L = D_0$ , where  $D_0$  is taken from the nuclear model database or, if not present, derived from the level density.  $E_L$  can also be entered as an input keyword (**Elow**). Next, we determine the neutron capture cross section at the thermal energy  $E_{th} = 2.53 \cdot 10^{-8}$  MeV, either from the experimental database, see Chapter 5, or, if not present, from the systematical relation [99]

$$\sigma_{n,\gamma}(E_{th}) = 1.5 \times 10^{-3} a (S_n - \Delta)^{3.5} \text{ mb} \quad (4.287)$$

with  $a$  the level density parameter at the separation energy  $S_n$  and  $\Delta$  the pairing energy. We assign a  $1/v$ , i.e.  $1/\sqrt{E}$ , dependence to the cross section from  $10^{-5}$  eV to an upper limit  $E_{1/v}$  which we set, again arbitrarily, at  $E_{1/v} = 0.2E_L$ . The  $1/v$  line obviously crosses  $\sigma_{n,\gamma}(E_{th})$  at  $E_{th}$ . The points at  $E_{1/v}$  and  $E_L$  are connected by a straight line. The resulting capture cross section then looks like Fig. 4.4. In reality, the region between  $E_{1/v}$  and  $E_L$  is filled with resolved resonances, the only feature we did not try to simulate.

### 4.9.2 Other non-threshold reactions

For other reactions with positive Q-values, such as  $(n, p)$  and  $(n, \alpha)$ , only a few experimental values at thermal energy are available and a systematical formula as for  $(n, \gamma)$  is hard to construct. If we do have a value for these reactions at thermal energy, the same method as for capture is followed. If not, we assume that the ratio between the gamma decay width and e.g. the proton decay width is constant for incident energies up to  $E_L$ . Hence, we determine  $R_p = \sigma_{n,p}/\sigma_{n,\gamma}$  at  $E_L$ , and since we know the thermal  $(n, \gamma)$  value we can produce the (n,p) excitation function down to  $10^{-5}$  eV by multiplying the capture cross section by  $R_p$ . A similar procedure is applied to all other non-threshold reactions.

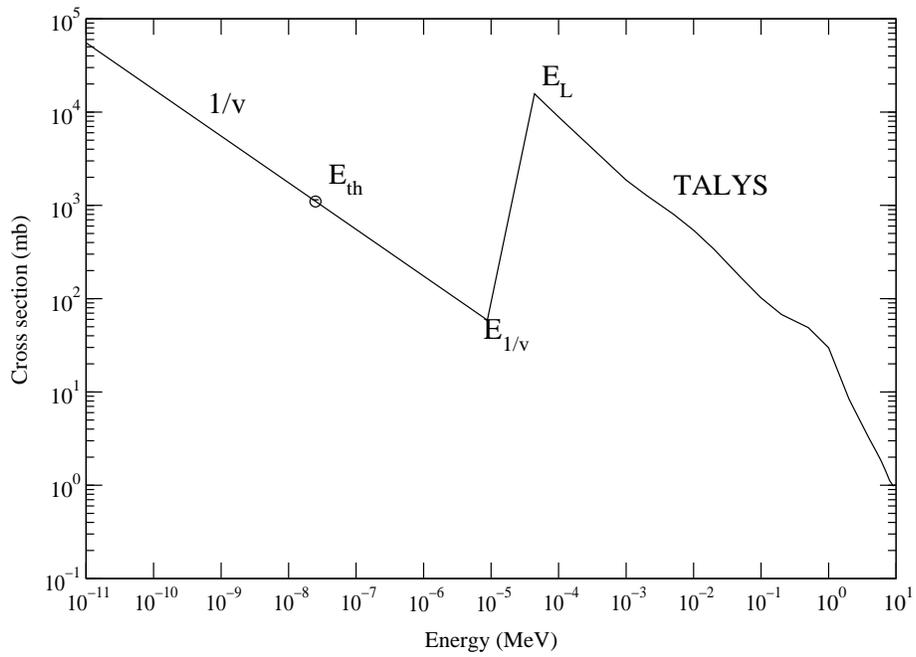


Figure 4.4: Capture cross section at low energies. The origin of the various energy regions are indicated.



## Chapter 5

# Nuclear structure and model parameters

### 5.1 General setup of the database

We have aimed to unify the nuclear structure and model parameter database of TALYS as much as possible. In the *talys/structure/* directory you can find the *masses/*, *abundance/*, *levels/*, *fission/*, *resonances/*, *deformation/*, *optical/*, *thermal/*, *gamma/* and *density/* subdirectories. Most subdirectories contain about 100 files, where each individual file points to a nuclear element and has the name *zZZZ* where *ZZZ* is the charge number of the element. One file contains the info for all the isotopes of one element. For example, the file *talys/structure/masses/z026* contains the theoretical and experimental masses of all Fe ( $Z=26$ ) isotopes. As you will see below, the chemical symbol is always present in the file itself, allowing an easy search. Every directory has this same substructure and also the formats in which the data are stored have been kept uniform as much as possible.

The nuclear structure database has been created from a collection of “raw” data files, which for a large part come from the Reference Input Parameter Library RIPL [36], that we used as a basis for TALYS.

### 5.2 Nuclear masses

The nuclear masses are stored in the *talys/structure/masses/* directory. In TALYS, we use three different sources. In order of priority:

1. Experimental masses: The Audi Wapstra table (1995) [100]
2. Theoretical masses: The Möller mass table [101]
3. The Duflo-Zuker mass formula [102], included as a subroutine in TALYS.

The Audi-Wapstra and Möller mass tables have been processed into our database. There, we have stored both the real mass  $M$  in atomic mass units ( $amu = 931.49386$  MeV) and the mass excess  $\Delta M = (M - A) * amu$  in MeV for both the experimental mass (if available) and the theoretical mass. The mass excesses are stored for a more precise calculation of separation energies.

For reaction Q-values one needs the masses of two nuclides. If for only one of them the experimental mass is known, we take the two *theoretical* mass excesses to calculate the Q-value, for consistency. This

only occurs for nuclides far from the line of stability. If a nuclide is even outside the tables given in the database, we use the formula of Duflo-Zuker, which is included as a subroutine in TALYS.

As an example, below are the masses of some of the Fe-isotopes as given in file *masses/z026*. We have stored  $Z$ ,  $A$ , experimental mass (*amu*), theoretical mass (*amu*), experimental mass excess (MeV), theoretical mass excess (MeV), nuclear symbol with the format (2i4,3f12.6,f8.2,22x,i4,a2).

26	42		42.053033		49.40	42Fe
26	43		43.040784		37.99	43Fe
26	44		44.025357		23.62	44Fe
26	45	45.014560	45.013859	13.563000	12.91	45Fe
26	46	46.000810	45.999979	0.755000	-0.02	46Fe
26	47	46.992890	46.991283	-6.623000	-8.12	47Fe
26	48	47.980560	47.979678	-18.108000	-18.93	48Fe
26	49	48.973610	48.973076	-24.582000	-25.08	49Fe
26	50	49.962993	49.962855	-34.471499	-34.60	50Fe
26	51	50.956824	50.956178	-40.217307	-40.82	51Fe
26	52	51.948116	51.948094	-48.329137	-48.35	52Fe
26	53	52.945312	52.944251	-50.941273	-51.93	53Fe
26	54	53.939614	53.938722	-56.248410	-57.08	54Fe
26	55	54.938298	54.937606	-57.475007	-58.12	55Fe
26	56	55.934942	55.934814	-60.601003	-60.72	56Fe
26	57	56.935398	56.935577	-60.175708	-60.01	57Fe
26	58	57.933280	57.933462	-62.148844	-61.98	58Fe
26	59	58.934880	58.935383	-60.658421	-60.19	59Fe
26	60	59.934076	59.933988	-61.406923	-61.49	60Fe

### 5.3 Isotopic abundances

We have included the possibility to evaluate nuclear reactions for natural elements. If **mass 0**, see page 116, a calculation is performed for each isotope, after which the results are averaged with the isotopic abundance as weight. The isotopic abundances are stored in the *talys/structure/abundance/* directory and they are taken from RIPL (which are equal to those of the Nuclear Wallet Cards from Brookhaven National Laboratory). As an example, below are the isotopic abundances for Fe from the file *abundance/z026*. For each isotope, we have stored  $Z$ ,  $A$ , its abundance, its uncertainty (not used in TALYS), nuclear symbol with the format (2i4,f11.6,f10.6,45x,i4,a2).

26	54	5.845000	0.035000	54Fe
26	56	91.754000	0.036000	56Fe
26	57	2.119000	0.010000	57Fe
26	58	0.282000	0.004000	58Fe

### 5.4 Discrete level file

The discrete level schemes are in the *talys/structure/levels/* directory. It is based on the discrete level file of Belgya, as stored in the RIPL database. We have transformed it to a format that corresponds with that of the other parameter files in our database. Also, we filled in some omissions, repaired several errors and

added some information necessary for Hauser-Feshbach calculations. As an example, below are the first discrete levels of  $^{93}\text{Nb}$  as given in file *z041*. We have stored  $Z$ ,  $A$ , total number of lines for this isotope, number of levels for this isotope, nuclear symbol with the format (2i4,2i5,56x,i4,a2). There is a loop over the levels in which we first read the level number, level energy in MeV, spin, parity, number of gamma-ray branchings, lifetime, spin assignment character, parity assignment character, original ENSDF string with the format (i4,f11.6,f6.1,3x,i2,i3,19x,e9.3,1x,2a1,a18). If the spin of a level does not come from the original file but instead is assigned in RIPL or by us, we place a 'J' in column 59. Analogously, an assigned parity is denoted by a 'P' in column 60. Note also that we have retained the original ENSDF string in columns 61-78. This string indicates the possible choices for spins and parities. If TALYS produces odd results for a nuclear reaction, a possible cause could be the wrong assignment of spin or parity. Columns 59 and 60 and the ENSDF string will reveal whether there are other possibilities that can be (and maybe should have been) adopted. For each level, there may be an inner loop over the number of gamma-ray branchings, and for each branching we read the number of the level to which the gamma-ray decay takes place and the corresponding branching ratio and electron-conversion factor. If a branching ratio has been assigned by us, a 'B' is placed in column 58. The format for this line is (29x,i3,f10.6,e10.3,5x,a1).

41	93	285	100																93Nb	
0	0.000000	4.5	1	0																9/2+
1	0.030820	0.5	-1	1																1/2-
					0	1.000000	1.750E+05											5.090E+08		
2	0.687000	1.5	-1	1																3/2-
					1	1.000000	1.833E-03											2.800E-13		
3	0.743910	3.5	1	1																7/2+
					0	1.000000	1.381E-03											5.700E-13		
4	0.808580	2.5	1	2																5/2+
					3	0.038049	7.810E-01											6.160E-12		
					0	0.961951	1.170E-03													
5	0.810410	2.5	-1	1																5/2-
					1	1.000000	1.282E-03											1.000E-12		
6	0.949830	6.5	1	1																13/2+
					0	1.000000	7.931E-04											4.360E-12		
7	0.970000	1.5	-1	2																1/2-, 3/2-
					2	0.500000	0.000E+00											J	B	
					4	0.500000	0.000E+00											B		
8	0.978940	5.5	1	1																11/2+
					0	1.000000	7.564E-04											2.510E-13		
9	1.082670	4.5	1	2																9/2+
					3	0.712735	9.051E-03											2.900E-12		
					0	0.287265	5.500E-04													
10	1.126850	2.5	-1	1																(5/2)
					4	1.000000	4.407E-03													
11	1.284400	0.5	1	1																(1/2+)
					1	1.000000	1.791E-04													
12	1.290000	0.5	-1	2																1/2-, 3/2-
					1	0.500000	0.000E+00											J	B	
					5	0.500000	0.000E+00											B		

13	1.297240	4.5	1	3		2.100E-13		9/2+
					8	0.232989	1.070E-02	
					3	0.259831	2.721E-03	
					0	0.507181	3.770E-04	
14	1.315140	2.5	-1	2				5/2(-)
					4	0.190340	1.311E-03	
					3	0.809660	1.053E-03	
15	1.330000	1.5	1	2				J (3/2+, 5/2+)
					1	0.500000	0.000E+00	B
					3	0.500000	0.000E+00	B

## 5.5 Deformation parameters

Deformation parameters and lengths are put in directory *talys/structure/deformation/*. They are strongly linked to the discrete level file when deformation parameters per level are given. The first subdirectory with deformation parameters is *exp/*, which have been derived from experimental information (spectroscopy, DWBA, etc.). For each isotope, we have stored  $Z$ ,  $A$ , number of levels, type of collectivity, the type of parameter, nuclear symbol with the format (3i4,3x,a1,3x,a1,54x,i4,a2). The type of parameter can be D (deformation length  $\delta_L$ ) or B (deformation parameter  $\beta_L$ ). The type of collectivity can be S (spherical), V (vibrational), R (rotational) and A (asymmetric rotational). Next, we read for each level the level number, the type of collectivity per level, the number of the vibrational band, multipolarity, magnetic quantum number, phonon number of the level, deformation parameter(s) with the format (i4,3x,a1,4i4,4f9.4). The type of collectivity per level can be either D (DWBA), V (vibrational) or R (rotational). In the case of levels that belong to a rotational band, only the level number and an 'R' are given. For the first level of the rotational band, the deformation parameter  $\beta_2$  (and, if present,  $\beta_4$  and  $\beta_6$ ) is given. Also, for the first level of a vibrational band the deformation parameter is given. The vibration-rotational model is thus invoked if within the rotational model also states belonging to a vibrational band can be specified. The level of complexity of rotational or vibrational-rotational calculations can be specified with the **maxrot** (see page 131) and **maxband** (see page 131) keywords. For weakly coupled levels that can be treated with DWBA, the level number, a 'D' and the deformation parameter is given.

As an example, below are the deformation parameters for some even Ca isotopes, taken from *z020*. This file ensures that for a reaction on  $^{40}\text{Ca}$ , a coupled-channels calculation with a vibrational model will automatically be invoked. Levels 2 ( $3^-$  at 3.737 MeV, with  $\delta_3 = 1.34$ ), 3 ( $2^+$  at 3.904 MeV, with  $\delta_2 = 0.36$ ), 4 ( $5^-$  at 4.491 MeV, with  $\delta_5 = 0.93$ ), will all be coupled individually as one-phonon states. There is an option to enforce a spherical OMP calculation through **spherical y** in the input, see page 131. In that case all levels will be treated with DWBA. The table below reveals that for the other Ca-isotopes the direct calculation will always be done with DWBA, but with deformation parameters  $\beta_L$  instead of deformation lengths  $\delta_L$ .

20	40	4	V	D				40Ca
		0	V	0				
		2	V	1	3	1	1.34000	
		3	V	2	2	1	0.36000	
		4	V	3	5	1	0.93000	
20	42	3	S	B				42Ca

0	V	0					
1	D				0.24700		
9	D				0.30264		
20	44	3	S	B			44Ca
0	V	0					
1	D				0.25300		
8	D				0.24012		
20	46	3	S	B			46Ca
0	V	0					
1	D				0.15300		
6	D				0.20408		
20	48	3	S	B			48Ca
0	V	0					
1	D				0.10600		
4	D				0.23003		

As a second example, below is the info for  $^{238}\text{U}$  from the *z092* file. The basis for the coupling scheme is a rotational model with deformation lengths  $\delta_2 = 1.546$  and  $\delta_4 = 0.445$ , in which levels 1, 2, 3, 4, 7 and 20 can be coupled. In practice, we would include at least levels 1 and 2 (and if the results are important enough also levels 3 and 4) as rotational levels. There are 5 vibrational bands which can be included. By default we include no vibrational bands in a rotational model, but if e.g. **maxband 1** in the input, the levels 5, 6, 8 and 12 would be included with deformation length  $\delta_3 = 0.9$ .

92	238	23	R	D				238U
0	R	0			1.54606	0.44508		
1	R	0						
2	R	0						
3	R	0						
4	R	0						
5	V	1	3	0	0.90000			
6	V	1						
7	R	0						
8	V	1						
9	V	2	4	0	0.20000			
10	V	3	3	1	0.10000			
11	V	3						
12	V	1						
13	V	2						
14	V	4	2	0	0.10000			
15	V	3						
16	V	4						
17	V	2						
19	V	5	2	2	0.10000			
20	R	0						
21	V	5						
23	V	4						
27	V	5						

The other subdirectory with deformation parameters is *moller/*. It contains Möller's table with  $\beta_2$  and

$\beta_4$  deformation parameters (also included in the RIPL database). For each isotope, we have stored  $Z$ ,  $A$ ,  $\beta_2$  and  $\beta_4$ , nuclear symbol with the format (2i4,1x,2f12.6,42x,i4,a2). Here is an example for various Fe-isotopes

26	42	0.271000	-0.097000	42Fe
26	43	0.221000	-0.072000	43Fe
26	51	0.198000	0.023000	51Fe
26	53	0.098000	-0.005000	53Fe
26	57	0.189000	-0.003000	57Fe
26	58	0.199000	-0.019000	58Fe
26	59	0.219000	-0.048000	59Fe
26	60	0.211000	-0.057000	60Fe
26	61	0.200000	-0.069000	61Fe
26	62	0.200000	-0.052000	62Fe
26	63	-0.130000	-0.025000	63Fe
26	64	-0.087000	-0.020000	64Fe
26	65	-0.026000		65Fe

These parameters are used when information in the *exp/* is not available.

## 5.6 Level density parameters

The level density parameters are stored in the *talys/structure/density/* directory. First, there are 2 sub-directories, *ground/* and *fission/*, for ground state and fission barrier level densities, respectively. In *ground/fermi/*, level density parameters  $a$  (at the binding energy) for about 300 nuclides are stored. They are derived from a fit to the  $D_0$  resonance spacings of the RIPL database. As an example, below are the parameters for the Pb-isotopes from *ground/fermi/z082*. For each isotope, we have stored  $Z$ ,  $A$ , level density parameter  $a$  in  $\text{MeV}^{-1}$ , nuclear symbol. The format is (2i4,f8.4,58x,i4,a2).

82	205	13.0930	205Pb
82	207	8.7999	207Pb
82	208	7.8623	208Pb

The second subdirectory *ground/goriely/*, contains the tabulated microscopic level densities of Goriely [89], also present in RIPL. For each isotope, there are first 4 comment lines, indicating the nucleus under consideration. Next, the excitation energy, temperature, number of cumulative levels, total level density, total state density and state density per spin are read in the format (f7.2,7.3,e10.2,31e9.2). Below is an example for the first energies of  $^{42}\text{Fe}$  from *ground/goriely/z026*

```
*****
* Z= 26 A= 42: Total and Spin-dependent Level Density [MeV-1] for FE 42 *
*****
U[MeV] T[MeV] NCUMUL RHO OBS RHOTOT J=0 J=1 J=2
0.25 0.224 1.09E+00 7.33E-01 2.07E+00 2.44E-01 3.39E-01 1.26E-01
0.50 0.302 1.33E+00 1.17E+00 4.14E+00 2.74E-01 4.83E-01 2.88E-01
0.75 0.365 1.71E+00 1.86E+00 7.60E+00 3.45E-01 6.76E-01 4.95E-01
1.00 0.419 2.29E+00 2.82E+00 1.31E+01 4.33E-01 9.05E-01 7.55E-01
```

The third subdirectory *ground/nmax/*, contains the  $N_U$  values per isotope, see Eq. (4.223), i.e. the level number at which the discrete level scheme starts to deviate from the constant-temperature level density law. This file also stems from a RIPL file of Goriely. For each isotope, we have stored  $Z$ ,  $A$ ,  $N_U$ , nuclear symbol with the format (3i4,62x,i4,a2). In *ground/nmax/z026* an example for the Fe-isotopes can be found:

26	52	4	52Fe
26	53	12	53Fe
26	54	20	54Fe
26	55	33	55Fe
26	56	55	56Fe
26	57	40	57Fe
26	58	12	58Fe
26	59	11	59Fe
26	60	6	60Fe

Level densities for fission barriers are tabulated in *fission/goriely/*. There is an *inner/* and *outer/* subdirectory, for the inner and outer barrier, respectively. Here is an example for the first few energy/spin points of  $^{230}\text{U}$  from *fission/goriely/inner/z090*. The format is the same as for the ground state, see above.

```
*****
* Z= 92 A=230: Total and Spin-dependent Level Density [MeV-1] at the inner
* saddle point c= 1.24 h= 0.00 a= 0.00 B= 3.80 MeV *
*****
U[MeV] T[MeV] NCUML  RHOBS  RHOTOT    J=0    J=1    J=2
  0.25  0.162  1.11E+00 8.86E-01 5.92E+00 6.44E-02 1.64E-01 1.98E-01
  0.50  0.190  1.51E+00 2.32E+00 1.81E+01 1.19E-01 3.20E-01 4.31E-01
  0.75  0.209  2.56E+00 6.10E+00 5.25E+01 2.54E-01 7.01E-01 9.85E-01
```

## 5.7 Resonance parameters

Neutron resonance parameters are provided in the *talys/structure/resonances/* directory and stem from the Obninsk file of the RIPL database. As an example, below are the parameters for the Fe-isotopes from *resonances/z026*. For each isotope, we have stored  $Z$ ,  $A$ , the experimental s-wave resonance spacing  $D_0$  in keV, its uncertainty, the experimental s-wave strength function  $S_0$  ( $\times 10^{-4}$ ), its uncertainty, the experimental total radiative width in eV and its uncertainty, nuclear symbol. The format is (2i4,2e9.2,2f5.2,2f9.5,20x,i4,a2).

26	55	1.30E+01	2.00E+00	6.90	1.80	1.80000	0.50000	55Fe
26	57	1.70E+01	2.00E+00	2.30	0.60	0.92000	0.41000	57Fe
26	58	6.00E+00	1.00E+00	4.70	1.10	1.90000	0.60000	58Fe
26	59	3.50E+01	1.50E+01	4.40	1.30	3.00000	0.90000	59Fe

## 5.8 Gamma-ray parameters

The Giant Dipole Resonance (GDR) parameters, stored in the *talys/structure/gamma/* directory, originate from the Beijing GDR compilation, as present in the RIPL database. As an example, below are the GDR

parameters for the U-isotopes from  $z092$ . For each isotope, we have stored  $Z$ ,  $A$ , energy  $E_0$  in MeV, strength  $\sigma_0$  in mb, width of the GDR  $\Gamma_0$  in MeV and, if present, another energy, strength and width for the second peak, nuclear symbol. The format is (2i4,6f8.2,18x,i4,a2).

92	233	11.08	221.00	1.94	13.86	433.00	5.47	233U
92	234	11.13	371.00	2.26	13.94	401.00	4.46	234U
92	235	10.90	328.00	2.30	13.96	459.00	4.75	235U
92	236	10.92	271.00	2.55	13.78	415.00	4.88	236U
92	238	10.77	311.00	2.37	13.80	459.00	5.13	238U

## 5.9 Thermal cross sections

In *talys/structure/thermal/*, the thermal cross sections for  $(n, \gamma)$ ,  $(n, p)$ ,  $(n, \alpha)$  and  $(n, f)$  cross sections are stored. The values come from Kopecky, who has compiled this database for use in the EAF library. In TALYS, we use this to determine cross sections for non-threshold reactions at low energies. For each isotope, we read  $Z$ ,  $A$ , target state (ground state or isomer), final state (ground state or isomer), the thermal  $(n, \gamma)$  cross section, its error, the thermal  $(n, p)$  cross section, its error, the thermal  $(n, \alpha)$  cross section, its error, the thermal  $(n, f)$  cross section, its error, nuclear symbol. The format is (4i4,8e9.2,7x,i4,a2). As an example, below are the values for the Fe-isotopes from  $z026$ .

26	54	0	0	2.70e+03	5.00e+02	1.00e-02	...	54Fe
26	55	0	0	1.30e+04	2.00e+03	1.70e+05	...	55Fe
26	56	0	0	2.60e+03	2.00e+02		...	56Fe
26	57	0	0	2.50e+03	5.00e+02		...	57Fe
26	58	0	0	1.30e+03	1.00e+02		...	58Fe
26	59	0	0	1.30e+04	3.00e+03	1.00e+04	...	59Fe

## 5.10 Optical model parameters

The optical model parameters are stored in the *talys/structure/optical/* directory. All the parameters are based on one and the same functional form, see Section 4.1. There are two subdirectories: *neutron/* and *proton/*. For each isotope, a non-dispersive optical potential can be given. Per isotope, we have stored  $Z$ ,  $A$ , number of different optical potentials (2), character to determine coupled-channels potential, nuclear symbol with the format (3i4,3x,a1,58x,i4,a2). On the next line we read the OMP index (1: non-dispersive), which currently runs to 1 only since our dispersive potentials are not yet published. Fermi energy and reduced Coulomb radius with the format (i4,f7.2,f8.3). On the next 3 lines we read the optical model parameters as defined in Section 4.1 with the following format

```
(2f8.3, f6.1, f10.4, f9.6, f6.1, f7.1) rv, av, v1, v2, v3, w1, w2
(2f8.3, f6.1, f10.4, f7.2) rvd, avd, d1, d2, d3
(2f8.3, f6.1, f10.4, f7.2, f6.1) rvso, avso, vso1, vso2, wso1, wso2
```

As an example, here are the parameters for the Fe-isotopes from *neutron/z026*.

```

26 54 1
1 -11.34 0.000
1.186 0.663 58.2 0.0071 0.000019 13.2 78.0
1.278 0.536 15.4 0.0223 10.90
1.000 0.580 6.1 0.0040 -3.1 160.0
26 56 1
1 -9.42 0.000
1.186 0.663 56.8 0.0071 0.000019 13.0 80.0
1.282 0.532 15.3 0.0211 10.90
1.000 0.580 6.1 0.0040 -3.1 160.0

```

54Fe

56Fe

## 5.11 Fission parameters

The fission parameters are stored in the *talys/structure/fission/* directory. There are various subdirectories: *barrier/*, *states/*, *brosa/*, and *mamdouh/*,

First, the experimental fission parameter set can be found in directory *barrier/*. The directory *states/* includes headband transition states for even-even, even-odd, odd-odd, and odd-even nuclides. The parameters are the result of an extensive fit to many experimental fission cross sections, compiled by V. Maslov for the RIPL library. As an example we show the available parameters for the uranium isotopes which are present in the file *barrier/z092*. We have stored *Z*, *A*, a parameter specifying the symmetry of the inner barrier, height of the inner barrier, curvature of the inner barrier, a parameter specifying the symmetry of the outer barrier, height of the outer barrier, curvature of the outer barrier, the pairing correlation function at the barrier (which is not used in the calculation) and the nuclear symbol with the format (2i4,a5,2f8.3,a5,2f8.3,f9.4,15x,i4,a2).

```

92 231 S 4.40 0.70 MA 5.50 0.50 0.869 231U
92 232 S 4.90 0.90 MA 5.40 0.60 0.848 232U
92 233 S 4.35 0.80 MA 5.55 0.50 0.946 233U
92 234 S 4.80 0.90 MA 5.50 0.60 0.889 234U
92 235 S 5.25 0.70 MA 6.00 0.50 0.803 235U
92 236 S 5.00 0.90 MA 5.67 0.60 0.833 236U
92 237 GA 6.40 0.70 MA 6.15 0.50 0.809 237U
92 238 GA 6.30 1.00 MA 5.50 0.60 0.818 238U
92 239 GA 6.45 0.70 MA 6.00 0.50 0.816 239U

```

In *states*, we have stored files with default head band and class II-states for even-even, even-odd, odd-odd, and odd-even nuclides. An example of a file containing the head band transition states is given below for *states/hbstates.ee*. This file is used for even-even nuclides. We loop over the two barriers. On the first line one finds the barrier number, the number of head band states and the energy at which the continuum starts with the format(2i4,f8.3). Next we loop over the transition states, in which we read the level number, level energy in MeV, spin and parity with the format (i4,f11.6,f6.1,i5).

```

1 8 0.800
1 0.000000 0.0 1
2 0.500000 2.0 1
3 0.400000 0.0 -1

```

```

4  0.400000  1.0  -1
5  0.500000  2.0   1
6  0.400000  2.0  -1
7  0.800000  0.0   1
8  0.800000  0.0   1
2  4   0.500
1  0.000000  0.0   1
2  0.500000  2.0   1
3  0.200000  0.0  -1
4  0.500000  1.0  -1

```

We also include the possibility to incorporate the effect of class II states in the calculation. For this purpose we take four parameter sets with class II states for even-even, even-odd, odd-odd, and odd-even nuclides. As an example we show the file *states/class2states.ee*. This file contains the well number, and the number of class II states. Subsequent lines contain the level number, the level energy in MeV, spin and parity with the format (i4,f8.3,f9.1,i5).

```

1  10
1  2.700      0.0   1
2  3.400      0.0  -1
3  4.100      1.0  -1
4  4.800      2.0  -1
5  5.000      1.0   1
6  5.200      0.0   1
7  5.400      0.0  -1
8  5.500      1.0  -1
9  5.600      2.0  -1
10 5.700      1.0   1

```

The directory *brosa/* contains three subdirectories: *barrier/*, *groundstate/*, and *precession/*. In *brosa/barrier/* temperature-dependent fission barrier parameters per fission mode can be found. They are the results of calculations performed within the Brosa model. The extension in the filename reveals the fission mode: *sl* for superlong, *st* for standard I, and *st2* for standard II. As an example, below are the superlong parameters for several U isotopes taken from *brosa/barrier/z092.sl*. Each line gives Z, A, temperature T in MeV,  $B_F$  in MeV,  $\hbar\omega$  in MeV, and the barrier position in terms of the distance between the fragment centers d in fm. The format is (2i4,4f15.5).

```

92 240      0.00000      11.40470      3.92020      10.37450
92 240      0.30000      11.23440      4.18630      10.34980
92 240      0.60000      11.64780      4.25390      10.44170
92 240      0.90000      9.58680      2.58900      10.35970
92 240      1.20000      7.88030      2.36520      10.53400
92 240      1.60000      5.69890      1.58010      10.43420
92 240      2.00000      4.17750      1.07010      10.28590
92 240      2.50000      2.76320      0.47300      9.69080
92 240      3.00000      1.84230      0.25520      8.57080
92 238      0.00000      10.88450      4.67530      10.27930
92 238      0.30000      10.97680      4.87110      10.27090
92 238      0.60000      10.59680      4.44100      10.29590

```

92 238	0.90000	9.31080	3.69600	10.37940
92 238	1.20000	7.55620	2.32260	10.40990
92 238	1.60000	5.46180	1.51320	10.33670
92 238	2.00000	3.98050	0.82730	10.15860
92 238	2.50000	2.74050	0.43440	9.43930
92 238	3.00000	1.87030	0.34600	8.62610

The ground state energies as a function of temperature are stored in *brosa/barrier/groundstate/*. Each line has the same format: Z, A, T in MeV, and  $E_{groundstate}$  in MeV (2i4,2f15.5). An example is included for U isotopes, see *brosa/barrier/groundstate/z092*.

92 240	0.00000	-1811.82104
92 240	0.30000	-1813.38599
92 240	0.60000	-1818.06006
92 240	0.90000	-1825.59497
92 240	1.20000	-1836.26599
92 240	1.60000	-1855.76294
92 240	2.00000	-1881.23901
92 240	2.50000	-1921.08105
92 240	3.00000	-1969.60205
92 238	0.00000	-1800.57996
92 238	0.30000	-1802.16504
92 238	0.60000	-1806.85205
92 238	0.90000	-1814.34302
92 238	1.20000	-1825.23596
92 238	1.60000	-1844.68799
92 238	2.00000	-1870.17004
92 238	2.50000	-1910.02905
92 238	3.00000	-1958.52405

The third directory, *brosa/barrier/pre-scission/*, contains parameters that fix the pre-scission shape of the nucleus in each fission mode. They mark the end of the fission path found in the same fission channel calculations that resulted in the Brosa barrier parameters. Again each line has the same format: Z, A, T in MeV,  $A_h$  the heavy fragment mass in amu,  $l$  the nucleus half length in fm, and  $E_{pre-scission}$  in MeV (2i4,4f15.5). An example is included for pre-scission shape parameters in the superlong mode of U isotopes, see *brosa/barrier/pre-scission/z092.sl*,

92 240	0.00000	120.45900	21.29700	-1840.84900
92 240	0.30000	120.83730	21.48670	-1826.35022
92 240	0.60000	120.83670	20.74300	-1831.38477
92 240	0.90000	120.30430	20.21950	-1840.12256
92 240	1.20000	120.65520	20.13060	-1854.43555
92 240	1.60000	120.83060	19.56120	-1874.16174
92 240	2.00000	120.74340	19.33610	-1902.75671
92 240	2.50000	120.62800	18.38600	-1945.59497
92 240	3.00000	120.78300	18.45000	-1998.50598
92 238	0.00000	120.00730	21.40630	-1815.46497
92 238	0.30000	119.64770	21.36200	-1816.33203

92 238	0.60000	119.50730	20.50950	-1821.51123
92 238	0.90000	119.27930	20.50120	-1830.13428
92 238	1.20000	119.47550	19.91770	-1842.70630
92 238	1.60000	123.00390	19.23990	-1864.13489
92 238	2.00000	120.49580	19.24370	-1892.63281
92 238	2.50000	119.62200	18.37100	-1935.14502
92 238	3.00000	119.37600	18.38000	-1988.42395

The Mamdouh fission parameter set can be found in directory *mamdouh/*. This parameter set has been derived from Extended Thomas-Fermi plus Strutinsky Integral calculations and comprise double-humped fission barrier heights and curvatures for numerous isotopes. As an example we show the available parameters for the various U isotopes which are present in the file *mamdouh/z092*. We have stored Z, A, height of the inner barrier, height of the outer barrier in MeV and the nuclear symbol with the format (i3,i4,2(24x,f8.2),5x,i3,a2).

92 230	1.24	0.00	0.00	3.80	1.77	-0.02	0.35	3.90	230U
92 231	1.24	0.01	0.00	4.10	1.83	0.05	0.50	4.30	231U
92 232	1.25	0.02	0.00	4.20	1.83	0.05	0.53	4.20	232U
92 233	1.28	0.05	0.00	4.70	1.84	0.06	0.53	4.40	233U
92 234	1.28	0.03	0.00	4.80	1.83	0.06	0.53	4.40	234U
92 235	1.28	0.04	0.00	5.40	1.63	0.01	0.53	4.10	235U
92 236	1.29	0.04	0.00	5.20	1.64	0.01	0.53	4.00	236U
92 237	1.28	0.04	0.00	5.70	1.63	0.01	0.53	4.30	237U
92 238	1.29	0.03	0.00	5.70	1.91	0.07	0.47	4.90	238U
92 239	1.29	0.03	0.00	6.10	1.81	-0.07	0.35	5.50	239U
92 240	1.29	0.03	0.00	6.00	1.90	-0.04	0.53	6.30	240U
92 241	1.30	0.04	0.00	6.30	1.91	-0.03	0.55	5.70	241U
92 242	1.30	0.04	0.00	5.90	1.90	-0.04	0.53	6.00	242U

## Chapter 6

# Input description

For the communication between TALYS and its users, we have constructed an input/output method which shields beginners from all the possible options for nuclear model parameters that can be specified in TALYS, while enabling at the same time maximal flexibility for experienced users.

An input file of TALYS consists of keywords and their associated values. Before we list all the input possibilities, let us illustrate the use of the input directly by the following example. It represents a minimum input file for TALYS:

```
projectile n
element    al
mass      27
energy    14.
```

This input file represents the simplest question that can be asked to TALYS: if a  $^{27}\text{Al}$  nucleus is hit by 14 MeV neutrons, what happens? Behind this simple input file, however, there are more than a hundred default values for the various nuclear models, parameters, output flags, etc., that you may or may not be interested in. When you use a minimal input file like the one above, you leave it to the authors of TALYS to choose all the parameters and models for you, as well as the level of detail of the output file. If you want to use specific nuclear models other than the default, adjust parameters or want to have more specific information in the output file, more keywords are required. Obviously, more keywords means more flexibility and, in the case of adequate use, better results, though often at the expense of increasing the level of phenomenology. In this Chapter, we will first give the basic rules that must be obeyed when constructing an input file for TALYS. Next, we give an outline of all the keywords, which have been categorised in several groups. Finally, we summarize all keywords in one table.

### 6.1 Basic input rules

Theoretically, it would be possible to make the use of TALYS completely idiot-proof, i.e. to prevent the user from any input mistakes that possibly can be made and to continue a calculation with “assumed” values. Although we have invested a relatively large effort in the user-friendliness of TALYS, we have not taken such safety measures to the extreme limit and ask at least some minimal responsibility from the user. Once you have accepted that, only very little effort is required to work with the code. Successful

execution of TALYS can be expected if you remember the following simple rules and possibilities of the input file:

1. One input line contains one keyword. Usually it is accompanied by only one value, as in the simple example given above, but some keywords for model parameters need to be accompanied by indices (usually *Z* and *A*) on the same line.
2. A keyword *must* start in column 1.
3. A keyword and its value(s) *must* be separated by at least 1 blank character.
4. The keywords can be given in arbitrary order. If, by mistake, you use the same keyword more than once, the value of the last one will be adopted. This does not hold for keywords with different *Z* and *A* indices, see below.
5. All characters can be given in either lowercase or uppercase.
6. A keyword *must* be accompanied by a value. (There is one exception, the **rotational** keyword). To use default values, the keywords should simply be left out of the input file.
7. An input line starting with a # in column 1 is neglected. This is helpful for including comments in the input file or to temporarily deactivate keywords.
8. A minimal input file always consists of 4 lines and contains the keywords **projectile**, **element**, **mass** and **energy**. These 4 keywords *must* be given in any input file.
9. An input line may not exceed 80 characters.

As an example of rules 3, 4, 5 and 7, it can be seen that the following input file is completely equivalent to the one given in the beginning of this Chapter:

```
# Equivalent input file
energy           14.
projectile n
mass 27
Element AL
#outbasic y
```

In the following erroneous input file, only the second line is correct, while rules 2, 3 and 6 are violated in the other lines.

```
projectile n
element u
mass27
energy
```

In cases like this, TALYS will give an error message for the first encountered problem and the execution will be stopped. We like to believe that we have covered all such cases and that it is impossible to let TALYS crash (at least with our compilers, see also Chapter 8) without giving an appropriate error message, but you are of course invited to prove and let us know about the contrary (Sorry, no cash rewards). Typing errors in the input file should be spotted by TALYS, e.g. if you write **projectile n**, it will tell you the keyword is not in our list.

## 6.2 Keywords

The four-line input file given above was an example of a minimum input file for TALYS. In general, you probably want to be more specific, as in the following example:

```
projectile  n
element    nb
mass       93
energy     1.
Ltarget    1
relativistic n
widthmode  2
outinverse y
a 41 93 13.115
a 41 94 13.421
```

which will simulate the reaction of a 1 MeV neutron incident on  $^{93}\text{Nb}$ , with the target in its first excited state (**Ltarget 1**, a 16-year isomer), using non-relativistic kinematics, the HRTW-model for width fluctuation corrections (**widthmode 2**) in the compound nucleus calculation, with the particle transmission coefficients and inverse reaction cross sections written on the output file (**outinverse y**) and with user-defined level density parameters at the binding energy **a** for  $^{93}\text{Nb}$  and  $^{94}\text{Nb}$ .

In this Section, we will explain all the possible keywords. We have classified according to their meaning and importance. For each keyword, we give an explanation, a few examples, the default value, and the theoretically allowed numerical range. As the input file above shows, there is usually one value per keyword. Often, however, in cases where several residual nuclides are involved, nuclear model parameters differ from nuclide to nuclide. Then, the particular nuclide under consideration must also be given in the input line. In general, for these model parameters, we read keyword, *Z*, *A*, a physical value and sometimes a possible further index (e.g. the fission barrier, index for the giant resonance, etc.), all separated by blanks. As the example above shows for the level density parameter *a*, the same keyword can appear more than once in an input file, to cover several different nuclides. Again, remember that all such keywords, if you don't specify them, have a default value from either the nuclear structure and model parameter database or from systematics. The usual reason to change them is to fit experimental data, to use new information that is not yet in the database, or simply because the user may not agree with our default values. A final important point to note is that some keywords induce defaults for other keywords. This may seem confusing, but in practice this is not so. As an example, for a  $^{56}\text{Fe}$  target the **fission** keyword is automatically disabled whereas for  $^{232}\text{Th}$  it is by default enabled. Hence, the default value of the **fission** keyword is mass dependent. In the input description that follows, you will find a few similar cases. Anyway, you can always find all adopted default values for all parameters at the top of the *output* file and overrule them in a new input file.

### 6.2.1 Four main keywords

As explained above there are 4 basic keywords that form the highest level of input. They determine the fundamental parameters for any nuclear reaction induced by a light particle.

**projectile**

Seven different symbols can be given as **projectile**, namely **n, p, d, t, h, a** and **g**, representing neutron, proton, deuteron, triton,  $^3\text{He}$ , alpha and gamma, respectively.

*Examples:*

**projectile n**

**projectile d**

*Range:* **projectile** must be equal to **n, p, d, t, h, a** or **g**.

*Default:* None.

**element**

Either the nuclear symbol or the charge number  $Z$  of the target nucleus can be given. Possible values for **element** range from Li (3) to Mt (109).

*Examples:*

**element pu**

**element 41**

**element V**

*Range:*  $3 \leq \text{element} \leq 109$  or  $\text{Li} \leq \text{element} \leq \text{Mt}$ .

*Default:* None.

**mass**

The target mass number  $A$ . The case of a natural element can be specified by **mass 0**. Then, a TALYS calculation for each naturally occurring isotope will be performed (see also the **abundance** keyword, p. 126), after which the results will be properly weighted and summed.

*Examples:*

**mass 239**

**mass 0**

*Range:* **mass 0** or  $5 \leq \text{mass} \leq 339$ . The extra condition is that the target nucleus, i.e. the combination of **mass** and **element** must be present in the mass database, which corresponds to all nuclei between the proton and neutron drip lines.

*Default:* None.

**energy**

The incident energy in MeV. The user has two possibilities: (1) A single incident energy is specified in the input as a real number, (2) A filename is specified, where the corresponding file contains a series of incident energies, with one incident energy per line. Any name can be given to this file, provided it starts with a character and it is present in your working directory. Option (2) is helpful for the calculation of excitation functions or for the creation of data libraries.

*Examples:*

**energy 140.**

**energy 0.002**

**energy range**

*Range:*  $10^{-11}$  MeV  $\leq$  **energy**  $<$  250 MeV or a *filename*, whereby the corresponding file contains at least 1 and a maximum of **numenin** incident energies, where **numenin** is an array dimension specified in *talys.cmb*. Currently **numenin=125**.

*Default:* None.

**Using the four main keywords**

To summarize the use of the four basic keywords, consider the following input file

```
projectile n
element    pd
mass      110
energy range
```

The file *range* looks e.g. as follows

```
0.1
0.2
0.5
1.
1.5
2.
5.
8.
10.
15.
20.
```

In the source code, the number of incident energies, here 11, is known as **numinc**. For the four-line input given above, TALYS will simulate all open reaction channels for  $n + {}^{110}\text{Pd}$  for all incident energies given in the file *range*, using defaults for all models and parameters. The most important cross sections will automatically be written to the output file, see Chapter 8.

The first four keywords are clearly the most important: they do *not* have a default value while they determine default values for some of the other keywords which, in other words, may be projectile-,

energy-, element- or mass-dependent. All the keywords that follow now in this manual have default values and can hypothetically be left out of the input file if you are only interested in a minimal reaction specification. If you want to add keywords, you can enter them one by one in the format that will be described below. Another way is to go to the top of the output file that is generated by the simple input file given above. You will find all the keywords with their values as adopted in the calculation, either user-specified or as defaults. All nuclear model parameters per nucleus are printed in the file *parameters.dat*, provided **partable y** was set in the input. You can copy this part and paste it into the input file, after which the values can be changed.

### 6.2.2 Basic physical and numerical parameters

The keywords described in this subsection are rather general and do not belong to particular nuclear models. They determine the completeness and precision of the calculations and most of them can have a significant impact on the calculation time.

#### ejectiles

The outgoing particles that are considered in competing reaction channels. By default, all competing channels are included even if one is interested in only one type of outgoing particle. This is necessary since there is always competition with other particles that determines the outcome for the particle under study. Furthermore, reaction Q-values automatically keep channels closed at low incident energies. However, for diagnostic or time-economical purposes, or cases where e.g. one is only interested in high-energy ( $p$ ,  $p'$ ) and ( $p$ ,  $n$ ) multi-step direct reactions, one may save computing time and output by skipping certain ejectiles as competing particles. For neutron-induced fission of actinides up to 20 MeV, setting **ejectiles g n** is a rather good approximation that saves time. Also comparisons with computer codes that do not include the whole range of particles will be facilitated by this keyword.

*Examples:*

**ejectiles n**

**ejectiles g n p a**

*Range:* **ejectiles** can be any combination of **g, n, p, d, t, h** and **a**.

*Default:* Include all possible outgoing particles, i.e. **ejectiles g n p d t h a**

#### Ltarget

The excited state of the target as given in the discrete level database. This keyword allows to compute cross sections for isomeric targets.

*Examples:*

**Ltarget 2**

*Range:*  $0 \leq \mathbf{Ltarget} \leq \mathbf{numlev}$ , where **numlev** is specified in the file *talys.cmb*. Currently, **numlev=25**

*Default:* **Ltarget 0**, i.e. the target is in its ground state.

**maxZ**

The maximal number of protons away from the initial compound nucleus that is considered in a chain of nuclides. For example, if **maxZ 3**, then for a  $n + {}^{56}\text{Fe}$  ( $Z=26$ ) reaction, the V-isotopes ( $Z=23$ ) are the last to be considered for further particle evaporation in the multiple emission chain. **maxZ** is normally only changed for diagnostic purposes. For example, if you are only interested in the  $(n, n')$ ,  $(n, 2n)$ , ...,  $(n, xn)$  residual production cross sections, or the associated discrete gamma ray intensities, **maxZ 0** is appropriate. (Note that in this case, the competition of emission of protons up to alpha particles is *still* taken into account for all the nuclides along the  $(n, xn)$  chain, only the decay of the associated residual nuclides are not tracked further).

*Examples:*

**maxZ 6**

*Range:*  $0 \leq \text{maxZ} \leq \text{numZ}-2$ , where we suggest **numZ=2+2\*memorypar** is specified in the file *talys.cmb*, where **memorypar=5** for a computer with at least 256 Mb of memory.

*Default:* Continue until all possible reaction channels are closed or until the maximal possible value for **maxZ** is reached (which rarely occurs). By default **maxZ=numZ-2** where the parameter **numZ** is specified in the file *talys.cmb*. This parameter should be large enough to ensure complete evaporation of all daughter nuclei.

**maxN**

The maximal number of neutrons away from the initial compound nucleus that is considered in a chain of nuclides. For example, if **maxN 3**, then for a  $n + {}^{56}\text{Fe}$  ( $N=31$ ) reaction, residual nuclei with  $N=28$  ( $=31-3$ ) are the last to be considered for further particle evaporation in the multiple emission chain. **maxN** is normally only changed for diagnostic or economical purposes.

*Examples:*

**maxN 6**

*Range:*  $0 \leq \text{maxN} \leq \text{numN}-2$ , where we suggest **numN=2+5\*memorypar** is specified in the file *talys.cmb*, where **memorypar=5** for a computer with at least 256 Mb of memory.

*Default:* Continue until all possible reaction channels are closed or until the maximal possible value for **maxN** is reached (which rarely occurs). By default **maxN=numN-2** where the parameter **numN** is specified in the file *talys.cmb*. This parameter should be large enough to ensure complete evaporation of all daughter nuclei.

**bins**

The number of excitation energy bins in which the continuum of the initial compound nucleus is divided for further decay. The excitation energy region between the last discrete level and the total excitation energy for the initial compound nucleus is divided into **bins** equidistant energy bins. The resulting bin width then also determines that for the neighboring residual nuclei, in the sense that for any residual nucleus we ensure that the bins fit exactly between the last discrete level and the maximal possible excitation energy. For residual nuclides far away from the target, a smaller number of bins is automatically

adopted. It is obvious that **bins** has a large impact on the computation time.

*Examples:*

**bins 25**

*Range:*  $2 \leq \mathbf{bins} \leq \mathbf{numbins}$ , where **numbins** is specified in the file *talys.cmb*. Currently, **numbins=100**

*Default:* **bins 40**

### segment

The number of segments to divide the standard emission energy grid. The basic emission energy grid we use for spectra and transmission coefficient calculations is:

```

0.001, 0.002, 0.005    MeV
0.01,  0.02, 0.05     MeV
0.1-   2 MeV : dE= 0.1 MeV
2  -   4 MeV : dE= 0.2 MeV
4  -  20 MeV : dE= 0.5 MeV
20  - 40 MeV : dE= 1.0 MeV
40  -250 MeV : dE= 2.0 MeV

```

This grid is divided into a finer grid by subdividing each interval by **segment**.

*Examples:*

**segment 3**

*Range:*  $1 \leq \mathbf{segment} \leq 4$ . Extra conditions:  $1 \leq \mathbf{segment} \leq 3$  if the maximum incident energy is larger than 20 MeV,  $1 \leq \mathbf{segment} \leq 2$  if the maximum incident energy is larger than 40 MeV, **segment=1** if the maximum incident energy is larger than 200 MeV. (These rules are imposed due to memory limitations).

*Default:* **segment 1**

### maxlevelstar

The number of included discrete levels for the *target* nucleus that is considered in Hauser-Feshbach decay and the gamma-ray cascade. For nuclides that do not have **maxlevelstar** available in the discrete level file, we take the last known level as the last discrete level in our calculation.

*Examples:*

**maxlevelstar 0**

**maxlevelstar 12**

*Range:*  $0 \leq \mathbf{maxlevelstar} \leq \mathbf{numlev}$ , where **numlev** is specified in the file *talys.cmb*. Currently, **numlev=25**

*Default:* **maxlevelstar 20**

**maxlevelsres**

The number of included discrete levels for all *residual* nuclides that is considered in Hauser-Feshbach decay and the gamma-ray cascade. For nuclides that do not have **maxlevelsres** available in the discrete level file, we take the last known level as the last discrete level in our calculation. This keyword is overruled by **maxlevelsbin** and **maxlevelstar** for specified nuclides.

*Examples:*

**maxlevelsres 0**

**maxlevelsres 12**

*Range:*  $0 \leq \text{maxlevelsres} \leq \text{numlev}$ , where **numlev** is specified in the file *talys.cmb*. Currently, **numlev=25**

*Default:* **maxlevelsres 10**

**maxlevelsbin**

The number of included discrete levels for the nuclides resulting from *binary* emission that is considered in Hauser-Feshbach decay and the gamma-ray cascade. For nuclides that do not have **maxlevelsbin** available in the discrete level file, we take the last known level as the last discrete level in our calculation. On the input line we read **maxlevelsbin**, the symbol of the ejectile and the number of levels of the associated residual nucleus.

*Examples:*

**maxlevelsbin a 8**

**maxlevelsbin p 12**

*Range:*  $0 \leq \text{maxlevelsbin} \leq \text{numlev}$ , where **numlev** is specified in the file *talys.cmb*. Currently, **numlev=25**

*Default:* **maxlevelsbin g 10, maxlevelsbin n 10, maxlevelsbin p 10, maxlevelsbin d 5, maxlevelsbin t 5, maxlevelsbin h 5, maxlevelsbin a 10**. The value for the inelastic channel will however always be overruled by the **maxlevelstar** keyword, for the target nucleus, or the value for its default.

**Nlevels**

The number of included discrete levels for a *specific residual* nucleus that is considered in Hauser-Feshbach decay and the gamma-ray cascade. For nuclides that do not have **Nlevels** available in the discrete level file, we take the last known level as the last discrete level in our calculation. On the input line we read **Nlevels**, *Z*, *A*, and the number of levels.

*Examples:*

**Nlevels 41 93 8**

*Range:*  $0 \leq \text{Nlevels} \leq \text{numlev}$ , where **numlev** is specified in the file *talys.cmb*. Currently, **numlev=25**

*Default:* **Nlevels** has the value specified by the defaults of **maxlevelstar**, **maxlevelsbin**, and **maxlevelsres**.

**levelfile**

File with discrete levels. The format of the file is exactly the same as that of the nuclear structure database *talys/structure/levels/*. In practice, the user can copy a file from this database, e.g. *z026*, to the working directory and change it. In this way, changes in the “official” database are avoided. Note that even if only changes for one isotope are required, the entire file needs to be copied if for the other isotopes the originally tabulated values are to be used. On the input line, we read **levelfile**, *Z*, filename.

*Examples:*

**levelfile 26 z026.loc**

*Range:* **levelfile** can be equal to any filename, provided it starts with a character.

*Default:* If **levelfile** is not given in the input file, the discrete levels are taken from the *talys/structure/levels* database per nucleus.

**isomer**

The definition of an isomer in seconds. In the discrete level database, the lifetimes of most of the levels are given. With **isomer**, it can be specified whether a level is treated as an isomer or not. Use **isomer 0.** to treat all levels, with any lifetime, as isomer and use **isomer 1.e38**, or any other number larger than the longest living isomer present in the problem, to include no isomers at all.

*Examples:*

**isomer 86400.** (86400 sec.=one day)

*Range:* **0. ≤ isomer ≤ 1.e38**

*Default:* **isomer 1.** (second)

**Elow**

Lowest incident energy in MeV for which TALYS performs a full nuclear model calculation. Below this energy, cross sections result from inter- and extrapolation using the calculated values at **Elow** and tabulated values and systematics at thermal energy. This keyword should only be used in the case of several incident energies.

*Examples:*

**Elow 0.001**

*Range:* **1.e – 6 ≤ Elow ≤ 1.**

*Default:* **Elow=D<sub>0</sub>**

**transpower**

A limit for considering transmission coefficients in the calculation. Transmission coefficients  $T_{ij}$  smaller than  $T_{0\frac{1}{2}} \times 10^{-\text{transpower}} / (2l + 1)$  are not used in Hauser-Feshbach calculations, in order to reduce the computation time.

*Examples:*

**transpower 12**

*Range:*  $2 \leq \text{transpower} \leq 20$

*Default:* **transpower 5**

**transeps**

A limit for considering transmission coefficients in the calculation. Transmission coefficients smaller than **transeps** are not used in Hauser-Feshbach calculations, irrespective of the value of **transpower**, in order to reduce the computation time.

*Examples:*

**transeps 1.e-12**

*Range:*  $0. \leq \text{transeps} \leq 1.$

*Default:* **transeps 1.e-8**

**xseps**

The limit for considering cross sections in the calculation, in mb. Reaction cross sections smaller than **xseps** are not used in the calculations, in order to reduce the computation time.

*Examples:*

**xseps 1.e-10**

*Range:*  $0. \leq \text{xseps} \leq 1000.$

*Default:* **xseps 1.e-7**

**popeps**

The limit for considering population cross sections in the multiple emission calculation, in mb. Nuclides which, before their decay, are populated with a total cross section less than **popeps** are skipped, in order to reduce the computation time. From **popeps**, also the criteria for continuation of the decay per excitation energy bin (variable **popepsA**) and per  $(E_x, J, \Pi)$  bin (variable **popepsB**) in Hauser-Feshbach calculations are automatically derived.

*Examples:*

**popeps 1.e-6**

*Range:*  $0. \leq \text{popeps} \leq 1000.$

*Default:* **popeps 1.e-3**

**angles**

Number of emission angles for reactions to discrete states.

*Examples:*

**angles 18**

*Range:*  $1 \leq \text{angles} \leq \text{numang}$ , where **numang** is specified in the file *talys.cmb*. Currently, **numang=90**

*Default:* **angles 90**

**anglescont**

Number of emission angles for reactions to the continuum.

*Examples:*

**anglescont 18**

*Range:*  $1 \leq \text{anglescont} \leq \text{numangcont}$ , where **numangcont** is specified in the file *talys.cmb*. Currently,

**numangcont=36**

*Default:* **anglescont 36**

**channels**

Flag for the calculation and output of all exclusive reaction channel cross sections, e.g.  $(n, 2n)$ ,  $(n, 2npa)$ , etc. The **channels** keyword can be used in combination with the keywords **outspectra** and **outangle** (see next Section) to give the exclusive spectra and angular distributions.

*Examples:*

**channels y**

**channels n**

*Range:* **y** or **n**

*Default:* **channels n**

**maxchannel**

Maximal number of outgoing particles in exclusive channel description, e.g. if **maxchannel 3**, then reactions up to 3 outgoing particles, e.g.  $(n, 2np)$ , will be given in the output. **maxchannel** is only active if **channels y**. We emphasize that, irrespective of the value of **maxchannel** and **channels**, all reaction chains are, by default, followed until all possible reaction channels are closed to determine composite particle production cross sections and residual production cross sections.

*Examples:*

**maxchannel 2**

*Range:*  $0 \leq \text{maxchannel} \leq \text{numchannel}$ , where **numchannel** is specified in the file *talys.cmb*. Currently, **numchannel=3+memorypar**, where we suggest **memorypar=5** for a computer with at least 256 Mb of memory.

*Default:* **maxchannel 4**

**relativistic**

Flag for relativistic kinematics.

*Examples:*

**relativistic y**

**relativistic n**

*Range:* **y** or **n**

*Default:* **relativistic y**

### **recoil**

Flag for the calculation of the recoils of the residual nuclides and the associated corrections to the light-particle spectra.

*Examples:*

**recoil y**

**recoil n**

*Range:* **y** or **n**

*Default:* **recoil n**

### **labddx**

Flag for the calculation of double-differential cross sections in the LAB system. This is only active if **recoil y**. If **labddx n**, only the recoils of the nuclides are computed.

*Examples:*

**labddx y**

**labddx n**

*Range:* **y** or **n**

*Default:* **labddx n**

### **anglesrec**

Number of emission angles for recoiling nuclides.

*Examples:*

**anglesrec 4**

*Range:*  $1 \leq \text{anglesrec} \leq \text{numangrec}$ , where **numangrec** is specified in the file *talys.cmb*. Currently, **numangrec=18**

*Default:* **anglesrec 9** if **labddx y**, **anglesrec 1** if **labddx n**

### **maxenrec**

Number of emission energies for recoiling nuclides.

*Examples:*

**maxenrec 4**

*Range:*  $1 \leq \text{maxenrec} \leq \text{numenrec}$ , where **numenrec** is specified in the file *talys.cmb*. Currently, **numenrec=5\*memorypar**, where we suggest **memorypar=5** for a computer with at least 256 Mb of memory.

*Default:* **maxenrec 10**

**recoilaverage**

Flag to consider only one average kinetic energy of the recoiling nucleus per excitation energy bin (instead of a full kinetic energy distribution). This approximation significantly decreases the calculation time.

*Examples:*

**recoilaverage y**

**recoilaverage n**

*Range:* y or n

*Default:* **recoilaverage n**

**channelenergy**

Flag to use the channel energy instead of the center-of-mass energy for the emission spectrum.

*Examples:*

**channelenergy y**

**channelenergy n**

*Range:* y or n

*Default:* **channelenergy n**

**abundance**

File with tabulated abundances. The **abundance** keyword is only active for the case of a natural target, i.e. if **mass 0**. By default, the isotopic abundances are read from the structure database, see Chapter 5. It can however be imagined that one wants to include only the most abundant isotopes of an element, to save some computing time. Also, **abundance** may be used to analyze experimental data for targets of a certain isotopic enrichment. On the input line, we read **abundance** and the filename. From each line of the file, TALYS reads *Z*, *A* and the isotopic abundance with the format (2i4,f11.6). An example of an abundance file, e.g. *abnew*, different from that of the database, is

```
82 206 24.100000
82 207 22.100000
82 208 52.400000
```

where we have left out the “unimportant”  $^{204}\text{Pb}$  (1.4%). TALYS automatically normalises the abundances to a sum of 1, leading in the above case to 24.44 % of  $^{206}\text{Pb}$ , 22.41 % of  $^{207}\text{Pb}$  and 53.14 % of  $^{208}\text{Pb}$  in the actual calculation.

*Examples:*

**abundance abnew**

*Range:* **abundance** can be equal to any filename and must be present in the working directory.

*Default:* If **abundance** is not given in the input file, abundances are taken from *talys/structure/abundance* and calculations for all isotopes are performed.

**partable**

Flag to write the model parameters per nucleus on a separate file, *parameters.dat*. This can be a very powerful option when one wishes to vary any nuclear model parameter in the input. The file *parameters.dat* has the exact input format, so it can be easily copied and pasted into any input file. This is helpful for a quick look-up of all the parameters used in a calculation while we have used this for automatic (random) TALYS-input generators.

*Examples:*

**partable y**

**partable n**

*Range:* y or n

*Default:* partable n

**6.2.3 Optical model****optmod**

File with tabulated phenomenological optical model parameters as a function of energy. This can be helpful if one wishes to use an optical model parameterisation which is not hardwired in TALYS. One could write a driver to automatically generate a table with parameters. On the input line, we read **optmod**, Z, A, filename, particle type. From each line of the file, TALYS reads  $E$ ,  $v$ ,  $rv$ ,  $av$ ,  $w$ ,  $rw$ ,  $aw$ ,  $vd$ ,  $rvd$ ,  $avd$ ,  $wd$ ,  $rwd$ ,  $awd$ ,  $vso$ ,  $rvso$ ,  $avso$ ,  $wso$ ,  $rwso$ ,  $awso$ , and  $rc$  with the format (f7.3,6(f7.3,2f6.3),f6.3).

*Examples:*

**optmod 40 90 ompzr90 d**

**optmod 94 239 omppu239**

*Range:* **optmod** can be equal to any filename, provided it starts with a character. The particle type must be equal to either **n**, **p**, **d**, **t**, **h** or **a**

*Default:* If the particle type is not given, as in the second example above, it is assumed it concerns neutrons. If **optmod** is not given in the input file, the optical model parameters are taken from the *talys/structure/optical* database per nucleus or, if not present there, from the global optical model.

**optmodfileN**

File with the neutron optical model parameters of Eq. (4.7). The format of the file is exactly the same as that of the nuclear structure database *talys/structure/optical/*. In practice, the user can copy a file from this database, e.g. *z026*, to the working directory and change it. In this way, changes in the “official” database are avoided. Note that even if only changes for one isotope are required, the entire file needs to be copied if for the other isotopes the originally tabulated values are to be used. On the input line, we read **optmodfileN**, Z, filename.

*Examples:*

**optmodfileN 26 z026.loc**

*Range:* **optmodfileN** can be equal to any filename, provided it starts with a character.

*Default:* If **optmodfileN** is not given in the input file, the optical model parameters are taken from the *talys/structure/optical* database per nucleus or, if not present there, from the global optical model.

### **optmodfileP**

File with the proton optical model parameters of Eq. (4.7). The format of the file is exactly the same as that of the nuclear structure database *talys/structure/optical/*. In practice, the user can copy a file from this database, e.g. *z026*, to the working directory and change it. In this way, changes in the “official” database are avoided. Note that even if only changes for one isotope are required, the entire file needs to be copied if for the other isotopes the originally tabulated values are to be used. On the input line, we read **optmodfileP**, *Z*, filename.

*Examples:*

**optmodfileP 26 z026.loc**

*Range:* **optmodfileP** can be equal to any filename, provided it starts with a character.

*Default:* If **optmodfileP** is not given in the input file, the optical model parameters are taken from the *talys/structure/optical* database per nucleus or, if not present there, from the global optical model.

### **localomp**

Flag to overrule the local, nucleus-specific optical model by the global optical model. This may be helpful to study global mass-dependent trends.

*Examples:*

**localomp n**

*Range:* **y** or **n**

*Default:* **localomp y**, i.e. a nucleus-specific optical model, when available.

### **sysreaction**

The types of particles for which the optical model reaction cross section is overruled by values obtained from systematics. The optical model transmission coefficients will be accordingly normalised.

*Examples:*

**sysreaction p**

**sysreaction d a**

*Range:* **sysreaction** can be any combination of **n**, **p**, **d**, **t**, **h** and **a**

*Default:* Take the reaction cross section from systematics for complex particles, i.e. **sysreaction d t h a**

*Warning:* setting e.g. **sysreaction p** will thus automatically disable the default setting. If this needs to be retained as well, set **sysreaction p d t h a**.

**statepot**

Flag for a different optical model parameterisation for each excited state in a DWBA or coupled-channels calculation. This may be appropriate if the emission energy of the ejectile, corresponding to a large excitation energy, differs considerably from the incident energy.

*Examples:*

**statepot y**

*Range:* y or n

*Default:* **statepot n**

**optmodall**

Flag for a new optical model calculation for each compound nucleus in the decay chain. In usual multiple Hauser-Feshbach decay, the transmission coefficients for the first compound nucleus are used for the whole decay chain. When a residual nucleus is far away from the initial compound nucleus, this approximation may become dubious. With **optmodall y**, new optical model calculations are performed for every compound nucleus that is depleted, for all types of emitted particles.

*Examples:*

**optmodall y**

*Range:* y or n

*Default:* **optmodall n**

**autorot**

Flag for automatic rotational coupled-channels calculations for  $A > 150$ . The discrete level file is scanned and the lowest rotational band is automatically identified. Deformation parameters are also read in from the database so automated coupled-channels calculations can be performed. This option is possible for the rare earth and actinide region.

*Examples:*

**autorot y**

*Range:* y or n

*Default:* **autorot n**

**core**

Integer to denote the even-even core for the weak-coupling model for direct scattering of odd- $A$  nuclei. A value of -1 means the even-even core is determined by subtracting a nucleon from the target nucleus, while a value of +1 means a nucleon is added.

*Examples:*

**core 1**

*Range:* -1 or 1

*Default:* **core -1**

**ecissave**

Flag for saving ECIS input and output files. This has two purposes: (a) if the next calculation will be performed with already existing reaction cross sections and transmission coefficients. This is helpful for time-consuming coupled-channels calculations, (b) to study the ECIS input and output files in detail. **ecissave** *must* be set to **y**, if in the next run **inccalc n** or **eciscalc n** will be used. If not, an appropriate error message will be given and TALYS stops.

*Examples:*

**ecissave y**

**ecissave n**

*Range:* **y** or **n**

*Default:* **ecissave n**

**eciscalc**

Flag for the ECIS calculation of transmission coefficients and reaction cross sections for the inverse channels. If this calculation has already been performed in a previous run, it may be helpful to put **eciscalc n**, which avoids a new calculation. This saves time, especially in the case of coupled-channels calculations. We stress that it is the responsibility of the user to ensure that the first run of a particular problem is done with **ecissave y** and **eciscalc y**. If not, an appropriate error message will be given and TALYS stops. You also have to make sure that the same energy grid for inverse channels is used.

*Examples:*

**eciscalc y**

**eciscalc n**

*Range:* **y** or **n**

*Default:* **eciscalc y**

**inccalc**

Flag for the ECIS calculation of transmission coefficients and reaction cross sections for the incident channel. If this calculation has already been performed in a previous run, it may be helpful to put **inccalc n**, which avoids a new ECIS calculation. This saves time, especially in the case of coupled-channels calculations. We stress that it is the responsibility of the user to ensure that the first run of a particular problem is done with **eciscalc y** and **inccalc y**. If not, an appropriate error message will be given and TALYS stops. You also have to make sure that the same grid of incident energies is used.

*Examples:*

**inccalc y**

**inccalc n**

*Range:* **y** or **n**

*Default:* **inccalc y**

### 6.2.4 Direct reactions

#### rotational

Flag to enable or disable the rotational optical model for the various particles appearing in the calculation. This flag is to enable or disable coupled-channels calculations for the inverse channels provided a coupling scheme is given in the deformation database. Using no rotational model at all can be set with another keyword: **spherical y**.

*Examples:*

**rotational n**

**rotational n p a**

*Range:* **rotational** can be any combination of **n, p, d, t, h** and **a**

*Default:* **rotational n p**. Warning: setting e.g. **rotational a** will thus automatically disable the default setting. If this needs to be retained as well, set **rotational n p a**

#### spherical

Flag to enforce a spherical OMP calculation, regardless of the availability of a deformed OMP and a coupling scheme. Direct inelastic scattering will then be treated by DWBA.

*Examples:*

**spherical n**

*Range:* **y** or **n**

*Default:* **spherical n**

#### maxrot

Number of excited levels to be included in a rotational band. For example, use **maxrot 4** if the  $0^+ - 2^+ - 4^+ - 6^+ - 8^+$  band needs to be included.

*Examples:*

**maxrot 4**

*Range:*  $0 \leq \text{maxrot} \leq 20$

*Default:* **maxrot 2**

#### maxband

Maximum number of vibrational bands added to the rotational coupling scheme, regardless of the number of bands specified in the deformation database.

*Examples:*

**maxband 4**

*Range:*  $0 \leq \text{maxband} \leq 100$

*Default:* **maxband 0**

**deformfile**

File with deformation parameters and coupling schemes. The format of the file is exactly the same as that of the nuclear structure database *talys/structure/deformation/*. In practice, the user can copy a file from this database, e.g. *z026*, to the working directory and change it. In this way, changes in the “official” database are avoided. Note that even if only changes for one isotope are required, the entire file needs to be copied if for the other isotopes the originally tabulated values are to be used. On the input line, we read **deformfile**, *Z*, filename.

*Examples:*

**deformfile 26 z026.loc**

*Range:* **deformfile** can be equal to any filename, provided it starts with a character.

*Default:* If **deformfile** is not given in the input file, discrete levels are taken from *talys/structure/deformation*.

**giantresonance**

Flag for the calculation of giant resonance contributions to the continuum part of the spectrum. The GMR, GQR, LEOR and HEOR are included.

*Examples:*

**giantresonance y**

**giantresonance n**

*Range:* **y** or **n**

*Default:* **giantresonance y** for incident neutrons and protons, **giantresonance n** otherwise.

**6.2.5 Compound nucleus****compound**

Flag for compound nucleus calculation. This keyword can be used to disable compound nucleus evaporation if one is for example only interested in high-energy pre-equilibrium spectra.

*Examples:*

**compound y**

**compound n**

*Range:* **y** or **n**

*Default:* **compound y**

**widthfluc**

Enabling or disabling width fluctuation corrections in compound nucleus calculations. For **widthfluc**, the user has 3 possibilities: **y**, **n** or a value for the starting energy. The latter option is helpful in the case of a calculation with several incident energies. Then, the user may want to set the width fluctuation off

as soon as the incident energy is high enough, in order to save computing time. We have taken care of this by the default, **widthfluc=S**, where  $S$  is the projectile separation energy ( $\sim 8$  MeV), of the target nucleus. This default is very safe, since in practice width fluctuation corrections are already negligible for incident energies above a few MeV, because the presence of many open channels reduces the correction to practically zero, i.e. the WFC factors to 1. Note that the disabling of width fluctuations for *any* incident energy can be accomplished by **widthfluc n**, which is equivalent to **widthfluc 0.** or any other energy lower than the (lowest) incident energy. Similarly, **widthfluc y**, equivalent to **widthfluc 20.**, will activate width fluctuations for any incident energy. To avoid numerical problems, width fluctuations are never calculated for incident energies beyond 20 MeV.

*Examples:*

**widthfluc y**

**widthfluc n**

**widthfluc 4.5**

*Range:* **y** or **n** or **0.**  $\leq$  **widthfluc**  $<$  **20.**

*Default:* **widthfluc** is equal to the projectile separation energy  $S$ , i.e. width fluctuation corrections are only used for incident energies below this value.

### **widthmode**

Model for width fluctuation corrections in compound nucleus calculations.

*Examples:*

**widthmode 0:** no width fluctuation, i.e. pure Hauser-Feshbach model

**widthmode 1:** Moldauer model

**widthmode 2:** Hofmann-Richert-Tepel-Weidenmüller model

**widthmode 3:** GOE triple integral model

*Range:* **0**  $\leq$  **widthmode**  $\leq$  **3**

*Default:* **widthmode 1**

### **fullhf**

Flag for Hauser-Feshbach calculation using the full  $j, l$  coupling. This keyword can be used to enable/disable the loop over total angular momentum of the ejectile  $j'$  in Eq. (4.134). If **fullhf n**, the transmission coefficients are averaged over  $j$ , reducing the calculation time of the full Hauser-Feshbach model. In practice, the difference with the results from the full calculation is negligible.

*Examples:*

**fullhf y**

**fullhf n**

*Range:* **y** or **n**

*Default:* **fullhf n**

**eciscompound**

Flag for compound nucleus calculation by ECIS-97, done in parallel with TALYS. This keyword is used for checking purposes only and does not influence the TALYS results. An ECIS input file is created that contains the same discrete levels, level density parameters etc., as the TALYS calculation. The compound nucleus results given by ECIS can be compared with the results from TALYS, but are not used in TALYS. The results are written on a separate ECIS output file.

*Examples:*

**eciscompound y**

**eciscompound n**

*Range:* **y** or **n**

*Default:* **eciscompound n**

**6.2.6 Gamma emission****gammax**

Maximum number of  $l$ -values for gamma multipolarity, whereby  $l = 1$  stands for M1 and E1 transitions,  $l = 2$  for M2 and E2 transitions, etc.

*Examples:*

**gammax 1**

*Range:* **1** ≤ **gammax** ≤ **6**

*Default:* **gammax 2**

**gnorm**

Normalisation factor for gamma-ray transmission coefficient. This adjustable parameter can be used to scale e.g. the  $(n, \gamma)$  cross section.

*Examples:*

**gnorm 1.6**

*Range:* **0.** ≤ **gnorm** ≤ **100.**

*Default:* **gnorm** is given by the normalisation factor of Eq. (4.48).

**strength**

Model for  $E1$  gamma-ray strength function. There are two possibilities.

*Examples:*

**strength 1** : Kopecky-Uhl generalized Lorentzian

**strength 2** : Brink-Axel Lorentzian

*Range:* **1** or **2**

*Default:* **strength 1**

**electronconv**

Flag for the application of an electron-conversion coefficient on the gamma-ray branching ratios from the discrete level file.

*Examples:*

**electronconv y**

**electronconv n**

*Range:* y or n

*Default:* **electronconv n**

**egr**

Energy of the giant dipole resonance in MeV. On the input line, we read **egr**, Z, A, value, type of radiation (the full symbol, i.e. M1, E1, E2, etc.), number of resonance (optional). If the number of the resonance is not given, it is assumed the keyword concerns the first Lorentzian.

*Examples:*

**egr 41 93 16.2 E1**

**egr 94 239 13.7 E1 2**

*Range:*  $1. \leq \text{egr} \leq 100$ . The optional number of the resonance must be either 1 or 2.

*Default:* **egr** is read from the *talys/structure/gamma/* directory. If the value for the first resonance is not present in the directory, it is calculated from systematics, see Section 4.3. If no parameter for the second resonance is given, this term is omitted altogether.

**sgr**

Strength of the giant dipole resonance in millibarns. On the input line, we read **sgr**, Z, A, value, type of radiation (the full symbol, i.e. M1, E1, E2, etc.), number of resonance (optional). If the number of the resonance is not given, it is assumed the keyword concerns the first Lorentzian.

*Examples:*

**sgr 41 93 221. E1**

**sgr 94 239 384. E1 2**

*Range:*  $0. \leq \text{sgr} \leq 10000$ . The optional number of the resonance must be either 1 or 2.

*Default:* **sgr** is read from the *talys/structure/gamma/* directory. If the value for the first resonance is not present in the directory, it is calculated from systematics, see Section 4.3. If no parameter for the second resonance is given, this term is omitted altogether.

**ggr**

Width of the giant dipole resonance in MeV. On the input line, we read **ggr**,  $Z$ ,  $A$ , value, type of radiation (the full symbol, i.e. M1, E1, E2, etc.), number of resonance (optional). If the number of the resonance is not given, it is assumed the keyword concerns the first Lorentzian.

*Examples:*

**ggr 41 93 5.03 E1**

**ggr 94 239 4.25 E1 2**

*Range:*  $1. \leq \text{ggr} \leq 100$ . The optional number of the resonance must be either 1 or 2.

*Default:* **ggr** is read from the *talys/structure/gamma/* directory. If the value for the first resonance is not present in the directory, it is calculated from systematics, see Section 4.3. If no parameter for the second resonance is given, this term is omitted altogether.

**gamgam**

The total radiative width,  $\Gamma_\gamma$  in eV. On the input line, we read **gamgam**,  $Z$ ,  $A$ , value.

*Examples:*

**gamgam 26 55 1.8**

*Range:*  $0. \leq \text{gamgam} \leq 10$ .

*Default:* **gamgam** is read from the *talys/structure/resonances/* directory, or, if not present there, is taken from interpolation, see Section 4.3.

**D0**

The s-wave resonance spacing  $D_0$  in keV. On the input line, we read **D0**,  $Z$ ,  $A$ , value.

*Examples:*

**D0 26 55 13.**

*Range:*  $1.e - 6 \leq \text{D0} \leq 10000$ .

*Default:* **D0** is read from the *talys/structure/resonances/* directory.

**S0**

The s-wave strength function  $S_0$  in units of  $10^{-4}$ . On the input line, we read **S0**,  $Z$ ,  $A$ , value.

*Examples:*

**S0 26 55 6.90**

*Range:*  $0. \leq \text{S0} \leq 10$ .

*Default:* **S0** is read from the *talys/structure/resonances/* directory.

### 6.2.7 Pre-equilibrium

#### preequilibrium

Enabling or disabling the pre-equilibrium reaction mechanism. For **preequilibrium**, the user has 3 possibilities: **y**, **n** or a value for the starting energy. The latter option is helpful in the case of a calculation with several incident energies. Then, the user may want to set pre-equilibrium contributions on as soon as the incident energy is high enough. We have taken care of this by the default, **preequilibrium=Ex(Nm)**, where  $Ex(Nm)$  is the excitation energy of the last discrete level  $Nm$  of the target nucleus. This default is very safe, since in practice the pre-equilibrium contribution becomes only sizeable for incident energies several MeV higher than  $Ex(Nm)$ . Note that the disabling of pre-equilibrium for *any* incident energy can be accomplished by **preequilibrium n**. Similarly, **preequilibrium y**, equivalent to **preequilibrium 0.**, will enable pre-equilibrium for any incident energy.

*Examples:*

**preequilibrium y**

**preequilibrium n**

**preequilibrium 4.5**

*Range:* **y** or **n** or **0.**  $\leq$  **preequilibrium**  $<$  **250.**

*Default:* **preequilibrium** is equal to  $Ex(NL)$ , i.e. pre-equilibrium calculations are included for incident energies above the energy of the last discrete level of the target nucleus.

#### preeqmode

Model for pre-equilibrium reactions. There are four possibilities.

*Examples:*

**preeqmode 1:** Exciton model: Analytical transition rates with energy-dependent matrix element.

**preeqmode 2:** Exciton model: Numerical transition rates with energy-dependent matrix element.

**preeqmode 3:** Exciton model: Numerical transition rates with optical model for collision probability.

**preeqmode 4:** Multi-step direct/compound model

*Range:* **1**  $\leq$  **preeqmode**  $\leq$  **4**

*Default:* **preeqmode 2**

#### multipreeq

Enabling or disabling multiple pre-equilibrium reaction mechanism. For **multipreeq**, the user has 3 possibilities: **y**, **n** or a value for the starting energy. The latter option is helpful in the case of a calculation with several incident energies. Then, the user may want to set multiple pre-equilibrium contributions on as soon as the incident energy is high enough. We have taken care of this by the default, **multipreeq 20.**

This default is very safe, since in practice the multiple pre-equilibrium contribution becomes only sizeable for incident energies a few tens of MeV higher than the default. Note that the disabling of multiple pre-equilibrium for *any* incident energy can be accomplished by **multipreeq n**. Similarly, **multipreeq y**, equivalent to **multipreeq 0.**, will activate multiple pre-equilibrium for any incident energy.

*Examples:*

**multipreeq y**

**multipreeq n**

**multipreeq 40.**

*Range:* **y** or **n** or **0.**  $\leq$  **multipreeq**  $<$  **250.**

*Default:* **multipreeq 20.**, i.e. multiple pre-equilibrium calculations are included for incident energies above this value. TALYS always sets **multipreeq n** if **preequilibrium n**.

### mpreeqmode

Model for multiple pre-equilibrium reactions. There are two possibilities, see Section 4.6.2 for an explanation.

*Examples:*

**mpreeqmode 1:** Multiple exciton model

**mpreeqmode 2:** Transmission coefficient method

*Range:* **1**  $\leq$  **mpreeqmode**  $\leq$  **2**

*Default:* **mpreeqmode 1**

### preeqspin

Flag to use the pre-equilibrium (y) or compound nucleus (n) spin distribution for the pre-equilibrium population of the residual nuclides.

*Examples:*

**preeqspin y**

**preeqspin n**

*Range:* **y** or **n**

*Default:* **preeqspin n**

### preeqsurface

Flag to use surface corrections in the exciton model.

*Examples:*

**preeqsurface y**

**preeqsurface n**

*Range:* **y** or **n**

*Default:* **preeqsurface y**

**Esurf**

Effective well depth for surface effects in MeV in the exciton model, see Eq. (4.66).

*Examples:*

**Esurf 25.**

*Range:*  $0. \leq \text{Esurf} \leq \text{Efermi}$ , where **Efermi** = 38 MeV is the Fermi well depth.

*Default:* **Esurf** is given by Eq. (4.66).

**preeqcomplex**

Flag to use the Kalbach model for pickup, stripping and knockout reactions, in addition to the exciton model, in the pre-equilibrium region.

*Examples:*

**preeqcomplex y**

**preeqcomplex n**

*Range:* **y** or **n**

*Default:* **preeqcomplex y**

**twocomponent**

Flag to use the two-component (**y**) or one-component (**n**) exciton model.

*Examples:*

**twocomponent y**

**twocomponent n**

*Range:* **y** or **n**

*Default:* **twocomponent y**

**M2constant**

Overall constant for the matrix element, or the optical model strength, in the exciton model. The parameterisation of the matrix element is given by Eq. (4.101) for the one-component model, and by Eq. (4.81) for the two-component model. **M2constant** is also used to scale the MSD cross section (preeqmode 4).

*Examples:*

**M2constant 1.22**

*Range:*  $0. \leq \text{M2constant} \leq 100.$

*Default:* **M2constant 1.**

**M2limit**

Constant to scale the asymptotic value of the matrix element in the exciton model. The parameterisation of the matrix element is given by Eq. (4.101) for the one-component model, and by Eq. (4.81) for the two-component model.

*Examples:*

**M2limit 1.22**

*Range:*  $0. \leq \text{M2limit} \leq 100.$

*Default:* **M2limit 1.**

**M2shift**

Constant to scale the energy shift of the matrix element in the exciton model. The parameterisation of the matrix element is given by Eq. (4.101) for the one-component model, and by Eq. (4.81) for the two-component model.

*Examples:*

**M2shift 1.22**

*Range:*  $0. \leq \text{M2shift} \leq 100.$

*Default:* **M2shift 1.**

**Rpinu**

Proton-neutron ratio for the matrix element in the two-component exciton model, see Eq. (4.79).

*Examples:*

**Rpinu 1.6**

*Range:*  $0. \leq \text{Rpinu} \leq 100.$

*Default:* **Rpinu 1.**

**Rgamma**

Adjustable parameter for pre-equilibrium gamma decay.

*Examples:*

**Rgamma 1.22**

*Range:*  $0. \leq \text{Rgamma} \leq 100.$

*Default:* **Rgamma 2.**

**ecisdwba**

Flag for DWBA calculations for multi-step direct calculations. If this calculation has already been performed in a previous run, it may be helpful to put **ecisdwba n**, which avoids a new calculation and thus saves time. We stress that it is the responsibility of the user to ensure that the first run of a particular problem is done with **ecisdwba y**. If not, an appropriate error message will be given and TALYS stops.

*Examples:*

**ecisdwba y**

**ecisdwba n**

*Range:* **y** or **n**

*Default:* **ecisdwba y**

**onestep**

Flag for inclusion of *only* the one-step direct contribution in the continuum multi-step direct model. This is generally enough for incident energies up to about 14 MeV, and thus saves computing time.

*Examples:*

**onestep y**

**onestep n**

*Range:* **y** or **n**

*Default:* **onestep n**

**msdbins**

The number of emission energy points for the DWBA calculation for the multi-step direct model.

*Examples:*

**msdbins 8**

*Range:*  $2 \leq \text{msdbins} \leq \text{numenmsd}/2-1$ , where **numenmsd** is specified in the file *talys.cmb*. Currently, **numenmsd=18**

*Default:* **msdbins 6**

**Emsdmin**

The minimal emission energy in MeV for the multi-step direct calculation.

*Examples:*

**Emsdmin 8.**

*Range:*  $0. \leq \text{Emsdmin}$

*Default:* **Emsdmin** is equal to **eninc/5**. where **eninc** is the incident energy.

### 6.2.8 Level densities

#### ldmodel

Model for level densities. There are 2 phenomenological Fermi gas models for high energies, which are matched with the constant temperature description at low energies, and one option for microscopic level densities.

*Examples:*

**ldmodel 1:** Fermi gas level density: Effective level density for ground state and collective effects on the barrier determined relative to the ground state.

**ldmodel 2:** Fermi gas level density: Explicit rotational and vibrational enhancement on ground state and fission barrier.

**ldmodel 3:** Microscopic level densities from Goriely's table

*Range:*  $1 \leq \text{ldmodel} \leq 3$

*Default:* **ldmodel 1**

#### asys

Flag to use all level density parameters from systematics by default, i.e. to neglect the connection between  $a$  and  $D_0$ , even if an experimental value is available for the latter.

*Examples:*

**asys y**

*Range:* **y** or **n**

*Default:* **asys y**

#### a

The level density parameter **a** at the neutron separation energy in  $\text{MeV}^{-1}$ . On the input line, we read **a**, **Z**, **A**, value.

*Examples:*

**a 41 93 11.220**

**a 94 239 28.385**

*Range:*  $1. \leq \mathbf{a} \leq 100.$

*Default:* **a** is read from the *talys/structure/density/* directory or, if not present, is calculated from systematics, see Eq. (4.201).

**alimit**

The asymptotic level density parameter  $\tilde{a}$ , for a particular nucleus, in  $\text{MeV}^{-1}$ , see Eq. (4.201). On the input line, we read **alimit**,  $Z$ ,  $A$ , value.

*Examples:*

**alimit 41 93 10.8**

**alimit 94 239 28.010**

*Range:*  $1. \leq \text{alimit} \leq 100.$

*Default:* **alimit** is determined from the systematics given by Eq. (4.204).

**alphald**

Constant for the global expression for the asymptotic level density parameter  $\tilde{a}$ , see Eq. (4.204).

*Examples:*

**alphald 0.054**

*Range:*  $0.01 \leq \text{alphald} \leq 0.1$

*Default:* **alphald** is determined from the systematics given by Eq. (4.205) or (4.236), depending on the used level density model.

**betald**

Constant for the global expression for the asymptotic level density parameter  $\tilde{a}$ , see Eq. (4.204).

*Examples:*

**betald 0.15**

*Range:*  $0. \leq \text{betald} \leq 0.5$

*Default:* **betald** is determined from the systematics given by Eq. (4.205) or (4.236), depending on the used level density model.

**gammald**

The damping parameter for shell effects in the level density parameter, for a particular nucleus, in  $\text{MeV}^{-1}$ , see Eq. (4.201). On the input line, we read **gammald**,  $Z$ ,  $A$ , value.

*Examples:*

**gammald 41 93 0.051**

*Range:*  $0. \leq \text{gammald} \leq 1.$

*Default:* **gammald** is determined from either Eq. (4.206) or (4.209).

**gammashell1**

Constant for the global expression for the damping parameter for shell effects in the level density parameter  $\gamma$ , see Eq. (4.207).

*Examples:*

**gammashell1 0.5**

**gammashell1 0.**

*Range:*  $0. \leq \text{gammashell1} \leq 1.$

*Default:* **gammashell1** is determined from the systematics given by Eq. (4.206) or Eq. (4.236).

**gammashell2**

Constant for the global expression for the damping parameter for shell effects in the level density parameter  $\gamma$ , see Eq. (4.207).

*Examples:*

**gammashell2 0.054**

**gammashell2 0.**

*Range:*  $0. \leq \text{gammashell2} \leq 0.2$

*Default:* **gammashell2=0.**

**pair**

The pairing correction in MeV. On the input line, we read **pair**,  $Z$ ,  $A$ , value.

*Examples:*

**pair 94 239 0.76**

*Range:*  $0. \leq \text{pair} \leq 10.$

*Default:* **pair** is determined from Eq. (4.196).

**deltaW**

Shell correction of the mass in MeV, see Eq. (4.201). On the input line, we read **deltaW**,  $Z$ ,  $A$ , value, the ground state or fission barrier to which it applies (optional). If the fission barrier is not given or is equal to 0, it concerns the ground state of the nucleus.

*Examples:*

**deltaW 41 93 0.110**

**deltaW 94 239 -0.262 1**

*Range:*  $-20. \leq \text{deltaW} \leq 20.$

*Default:* **deltaW** is determined from Eq. (4.202).

**Nlow**

Lower level to be used in the temperature matching problem of the Gilbert and Cameron formula. On the input line, we read **Nlow**,  $Z$ ,  $A$ , value, the ground state or fission barrier to which it applies (optional). If the fission barrier is not given or equal to 0, it concerns the ground state of the nucleus.

*Examples:*

**Nlow 41 93 4**

**Nlow 94 239 2 1**

*Range:*  $0 \leq \text{Nlow} \leq 200$

*Default:* **Nlow 2**

**Ntop**

Upper level to be used in the temperature matching problem of the Gilbert and Cameron formula. On the input line, we read **Ntop**,  $Z$ ,  $A$ , value, the ground state or fission barrier to which it applies (optional). If the fission barrier is not given or equal to 0, it concerns the ground state of the nucleus.

*Examples:*

**Ntop 41 93 14**

**Ntop 94 239 20 1**

*Range:*  $0 \leq \text{Ntop} \leq 200$

*Default:* **Ntop** is read from the *talys/structure/density/nmax* directory. If not present there, **Ntop** is equal to the last discrete level used for the Hauser-Feshbach calculation.

**Exmatch**

The matching energy between the constant temperature and Fermi gas region in MeV, see Eq. (4.218). On the input line, we read **Exmatch**,  $Z$ ,  $A$ , value, the ground state or fission barrier to which it applies (optional). If the fission barrier is not given or is equal to 0, it concerns the ground state of the nucleus.

*Examples:*

**Exmatch 41 93 4.213**

**Exmatch 94 239 5.556 2**

*Range:*  $0.1 \leq \text{Exmatch} \leq 20$ .

*Default:* **Exmatch** is determined from Eq. (4.225).

**T**

The temperature of the Gilbert-Cameron formula in MeV, see Eq. (4.222). On the input line, we read **T**,  $Z$ ,  $A$ , value, the ground state or fission barrier to which it applies (optional). If the fission barrier is not given or is equal to 0, it concerns the ground state of the nucleus.

*Examples:*

**T 41 93 0.332**

**T 94 239 0.673 1**

*Range:*  $0.001 \leq T \leq 10$ .

*Default:* T is determined from Eq. (4.222).

### E0

The "back-shift" energy of the four-component formula in MeV, see Eq. (4.219). On the input line, we read **E0**, Z, A, value, the ground state or fission barrier to which it applies (optional). If the fission barrier is not given or is equal to 0, it concerns the ground state of the nucleus.

*Examples:*

**E0 41 93 0.101**

**E0 94 239 -0.451 1**

*Range:*  $-10. \leq E0 \leq 10$ .

*Default:* **E0** is determined from Eq. (4.219).

### colldamp

Flag for the enabling or disabling of the phenomenological function (4.213) for the damping of collective effects in level densities.

*Examples:*

**colldamp y**

**colldamp n**

*Range:* y or n

*Default:* **colldamp n**

### Ufermi

Constant  $U_f$  of the phenomenological function (4.213) for damping of collective effects, in MeV.

*Examples:*

**Ufermi 45.**

*Range:*  $0. \leq Ufermi \leq 1000$ .

*Default:* **Ufermi 30.**

### cfermi

Width  $C_f$  of the phenomenological Fermi distribution (4.213) for damping of collective effects, in MeV.

*Examples:*

**cfermi 16.**

*Range:*  $0. \leq cfermi \leq 1000$ .

*Default:* **cfermi 10.**

**Ufermibf**

Constant  $U_f$  of the phenomenological function (4.213) for damping of collective effects on the fission barrier, in MeV.

*Examples:*

**Ufermibf 90.**

*Range:* **0. ≤ Ufermibf ≤ 1000.**

*Default:* **Ufermibf 45.**

**cfermibf**

Width  $C_f$  of the phenomenological Fermi distribution (4.213) for damping of collective effects on the fission barrier, in MeV.

*Examples:*

**cfermibf 16.**

*Range:* **0. ≤ cfermibf ≤ 1000.**

*Default:* **cfermibf 10.**

**Rspincut**

Adjustable constant for spin cutoff factor. Eq. (4.198) is multiplied by **Rspincut**.

*Examples:*

**Rspincut 0.8**

*Range:* **0. ≤ Rspincut ≤ 10.**

*Default:* **Rspincut 1.**

**beta2**

Deformation parameter for moment of inertia for the ground state or fission barrier, see Eq. (4.243). On the input line, we read **beta2**, Z, A, value, fission barrier. If the number of the fission barrier is not given or is equal to 0, it concerns the ground state.

*Examples:*

**beta2 90 232 0.3**

**beta2 94 239 1.1 2**

*Range:* **0. ≤ beta2 ≤ 2.**

*Default:* **beta2 0.** for the ground state, **beta2 0.6** for the first barrier, **beta2 0.8** for the second barrier, and **beta2 1.** for the third barrier.

**Krotconstant**

Normalization constant for rotational enhancement for the ground state or fission barrier, to be multiplied with the r.h.s. of Eq. (4.242). On the input line, we read **Krotconstant**,  $Z$ ,  $A$ , value, fission barrier. If the number of the fission barrier is not given or is equal to 0, it concerns the ground state.

*Examples:*

**Krotconstant 90 232 0.4**

**Krotconstant 94 239 1.1 2**

*Range:*  $0.01 \leq \text{Krotconstant} \leq 100$ .

*Default:* **Krotconstant 1.**

**c1table**

Constant  $c_1$  of the adjustment function (4.247) for tabulated level densities. On the input line, we read **c1table**,  $Z$ ,  $A$ , value.

*Examples:*

**c1table 29 65 2.8**

*Range:*  $0. < \text{c1table} \leq 10^6$

*Default:* **c1table 1.**

**c2table**

Constant  $c_2$  of the adjustment function (4.247) for tabulated level densities. On the input line, we read **c2table**,  $Z$ ,  $A$ , value.

*Examples:*

**c2table 29 65 -0.6**

*Range:*  $-10. \leq \text{c2table} \leq 10$ .

*Default:* **c2table 0.**

**Kph**

Value for the constant of the single-particle level density parameter, i.e.  $g = A/K_{ph}$ , or  $g_\pi = Z/K_{ph}$  and  $g_\nu = N/K_{ph}$

*Examples:*

**Kph 12.5**

*Range:*  $1. \leq \text{Kph} \leq 100$ .

*Default:* **Kph 15.**

**g**

The single-particle level density parameter  $g$  in  $\text{MeV}^{-1}$ . On the input line, we read  $g$ ,  $Z$ ,  $A$ , value.

*Examples:*

**g 41 93 7.15**

**g 94 239 17.5**

*Range:*  $0.1 \leq g \leq 100$ .

*Default:*  $g = A/Kph$

**gp**

The single-particle proton level density parameter  $g_{\pi}$  in  $\text{MeV}^{-1}$ . On the input line, we read  $gp$ ,  $Z$ ,  $A$ , value.

*Examples:*

**gp 41 93 3.15**

**gp 94 239 7.2**

*Range:*  $0.1 \leq gp \leq 100$ .

*Default:*  $gp = Z/Kph$

**gn**

The single-particle neutron level density parameter  $g_{\nu}$  in  $\text{MeV}^{-1}$ . On the input line, we read  $gn$ ,  $Z$ ,  $A$ , value.

*Examples:*

**gn 41 93 4.1**

**gn 94 239 11.021**

*Range:*  $0.1 \leq gn \leq 100$ .

*Default:*  $gn = N/Kph$

**gshell**

Flag to include the damping of shell effects with excitation energy in single-particle level densities. The Ignatyuk parameterisation for total level densities is also applied to the single-particle level density parameters.

*Examples:*

**gshell y**

**gshell n**

*Range:* **y** or **n**

*Default:* **gshell n**

## 6.2.9 Fission

### fission

Flag for the enabling or disabling of fission. By default **fission** is enabled if the target mass is above 209. Hence, for lower masses, it is necessary to set **fission y** manually at high incident energies (subactinide fission).

*Examples:*

**fission y**

**fission n**

*Range:* **y** or **n**. Fission is not allowed for  $A \leq 56$

*Default:* **fission y** for  $A > 209$ , **fission n** for  $A \leq 209$ . The default enabling or disabling of fission is thus mass dependent.

### fismodel

Model for fission barriers. **fismodel** is only active if **fission y**. There are 4 possibilities:

*Examples:*

**fismodel 1** : experimental fission barriers

**fismodel 2** : theoretical fission barriers, Mamdouh table

**fismodel 3** : theoretical fission barriers, Sierk model

**fismodel 4** : theoretical fission barriers, rotating liquid drop model

*Range:*  $1 \leq \text{fismodel} \leq 4$

*Default:* **fismodel 1**

### fismodelalt

”Back-up” model for fission barriers, for the case that the parameters of the tables used in **fismodel 1-2** are not available. There are two possibilities:

*Examples:*

**fismodelalt 3** : theoretical fission barriers, Sierk model

**fismodelalt 4** : theoretical fission barriers, rotating liquid drop model

*Range:*  $3 \leq \text{fismodelalt} \leq 4$

*Default:* **fismodelalt 4**

**axtype**

Type of axiality of the fission barrier. There are two options: **axtype 1** for an axial barrier and **axtype 2** for a tri-axial barrier. On the input line, we read **axtype**,  $Z$ ,  $A$ , value, fission barrier. This keyword overrules the value given in the nuclear structure database. If the number of the fission barrier is not given or is equal to 0, it concerns the first barrier.

*Examples:*

**axtype 90 232 2**

**axtype 94 239 1 2**

*Range:* **1** or **2**

*Default:* **axtype 2** for the first barrier and  $N > 144$ , **axtype 1** for the rest.

**fi sbar**

Fission barrier in MeV. On the input line, we read **fisbar**,  $Z$ ,  $A$ , value, fission barrier. This keyword overrules the value given in the nuclear structure database. If the number of the fission barrier is not given or is equal to 0, it concerns the first barrier.

*Examples:*

**fisbar 90 232 5.6**

**fisbar 94 239 6.1 2**

*Range:* **0.**  $\leq$  **fisbar**  $\leq$  **100.**

*Default:* **fisbar** is read from the *talys/structure/fission/* directory, or determined by systematics according to the choice of **fismodel**.

**fi shw**

Fission barrier width in MeV. On the input line, we read **fishw**,  $Z$ ,  $A$ , value, fission barrier. This keyword overrules the value given in the nuclear structure database. If the number of the fission barrier is not given or is equal to 0, it concerns the first barrier.

*Examples:*

**fishw 90 232 0.8**

**fishw 94 239 1.1 2**

*Range:* **0.01**  $\leq$  **fishw**  $\leq$  **10.**

*Default:* **fishw** is read from the *talys/structure/fission/* directory or determined by systematics, according to the choice of **fismodel**.

**Rtransmom**

Normalization constant for moment of inertia for transition states, see Eq. (4.243). On the input line, we read **Rtransmom**,  $Z$ ,  $A$ , value, fission barrier. If the number of the fission barrier is not given or is equal to 0, it concerns the first barrier.

*Examples:*

**Rtransmom 90 232 1.15**

**Rtransmom 94 239 1.1 2**

*Range:*  $0.1 \leq \mathbf{Rtransmom} \leq 10$ .

*Default:* **Rtransmom 0.6** for the first barrier, **Rtransmom 1.0** for the other barriers.

**hbtransfile**

File with head band transition states. The format of the file is exactly the same as that of the nuclear structure database *talys/structure/fission/barrier/*. In practice, the user can copy a file from this database, e.g. *z092*, to the working directory and change it. In this way, changes in the “official” database are avoided. Note that one file in the working directory can only be used for one isotope. On the input line, we read **hbtransfile**,  $Z$ ,  $A$ , filename.

*Examples:*

**hbtransfile 92 238 u238.hb**

*Range:* **hbtransfile** can be equal to any filename, provided it starts with a character.

*Default:* If **hbtransfile** is not given in the input file, the head band transition states are taken from the *talys/structure/fission/states* database.

**class2**

Flag for the enabling or disabling of class II/III states in fission. **class2** is only active if **fission y**.

*Examples:*

**class2 y**

**class2 n**

*Range:* **y** or **n**

*Default:* **class2 n**

**Rclass2mom**

Normalization constant for moment of inertia for class II/III states, see Eq. (4.243). On the input line, we read **Rclass2mom**,  $Z$ ,  $A$ , value, fission barrier. If the number of the fission barrier is not given or is equal to 0, it concerns the first barrier well.

*Examples:*

**Rclass2mom 90 232 1.15**

**Rclass2mom 94 239 1.1 2**

*Range:*  $0.1 \leq \mathbf{Rclass2mom} \leq 10$ .

*Default:* **Rclass2mom 1**.

### class2width

Width of class II/III states. On the input line, we read **class2width**, Z, A, value, fission barrier. If the number of the fission barrier is not given or is equal to 0, it concerns the first barrier well.

*Examples:*

**class2width 90 232 0.35**

**class2width 94 239 0.15 2**

*Range:*  $0.01 \leq \mathbf{class2width} \leq 10$ .

*Default:* **class2width 0.2**

### class2file

File with class II/III transition states. The format of the file is exactly the same as that of the nuclear structure database *talys/structure/fission/states/*. In practice, the user can copy a file from this database, e.g. *z092*, to the working directory and change it. In this way, changes in the “official” database are avoided. Note that one file in the working directory can only be used for one isotope. On the input line, we read **class2file**, Z, A, filename.

*Examples:*

**class2file 92 238 u238.c2**

*Range:* **class2file** can be equal to any filename, provided it starts with a character.

*Default:* If **class2file** is not given in the input file, the head band transition states are taken from the *talys/structure/fission/states* database.

### Rfiseps

Ratio for limit for fission cross section per nucleus. This parameter determines whether the mass distribution for a residual fissioning nucleus will be calculated. Cross sections smaller than **Rfiseps** times the fission cross section are not used in the calculations, in order to reduce the computation time.

*Examples:*

**Rfiseps 1.e-5**

*Range:*  $0. \leq \mathbf{Rfiseps} \leq 1$ .

*Default:* **Rfiseps 1.e-3**

**massdis**

Flag for the calculation of the fission-fragment mass distribution with the Brosa model.

*Examples:*

**massdis y**

**massdis n**

*Range:* y or n

*Default:* **massdis n**

**ffevaporation**

Flag to enable phenomenological correction for evaporated neutrons from fission fragments with the Brosa model.

*Examples:*

**ffevaporation y**

**ffevaporation n**

*Range:* y or n

*Default:* **ffevaporation n**

**6.2.10 Output**

The output can be made as compact or as extensive as you like. This can be specified by setting the following keywords. We especially wish to draw your attention to the several keywords that start with "file", at the end of this section. They can be very helpful if you directly want to have specific results available in a single file. Note that if you perform calculations with several incident energies, the files produced with these "file" keywords are incremented *during* the calculation. In other words, you can already plot intermediate results before the entire calculation has finished.

**outmain**

Flag for the main output. The header of TALYS is printed, together with the input variables and the automatically adopted default values. Also the most important computed cross sections are printed.

*Examples:*

**outmain y**

**outmain n**

*Range:* y or n

*Default:* **outmain y**

**outbasic**

Flag for the output of *all* basic information needed for the nuclear reaction calculation, such as level/bin populations, numerical checks, optical model parameters, transmission coefficients, inverse reaction cross sections, gamma and fission information, discrete levels and level densities. If **outbasic** is set to **y** or **n**, the keywords **outpopulation**, **outcheck**, **outlevels**, **outdensity**, **outomp**, **outdirect**, **outdiscrete**, **outinverse**, **outgamma** and **outfission** (see below for their explanation) will all be set to the same value automatically. Setting **outbasic y** is generally not recommended since it produces a rather large output file. Less extensive output files can be obtained by enabling some of the aforementioned keywords individually.

*Examples:*

**outbasic y**

**outbasic n**

*Range:* **y** or **n**

*Default:* **outbasic n**

**outpopulation**

Flag for the output of the population, as a function of excitation energy, spin and parity, of each compound nucleus in the reaction chain before it decays.

*Examples:*

**outpopulation y**

**outpopulation n**

*Range:* **y** or **n**

*Default:* the same value as **outbasic**: **outpopulation n**

**outcheck**

Flag for the output of various numerical checks. This is to check interpolation schemes for the transformation from the emission grid to the excitation energy grid and vice versa, and to test the WFC method by means of flux conservation in the binary compound nucleus calculation. Also, the emission spectra integrated over energy are compared with the partial cross sections, and summed exclusive channel cross sections are checked against total particle production cross sections and residual production cross sections.

*Examples:*

**outcheck y**

**outcheck n**

*Range:* **y** or **n**

*Default:* the same value as **outbasic**: **outcheck n**

**outlevels**

Flag for the output of discrete level information for each nucleus. All level energies, spins parities, branching ratios and lifetimes will be printed.

*Examples:*

**outlevels y**

**outlevels n**

*Range:* y or n

*Default:* the same value as **outbasic: outlevels n**

**outdensity**

Flag for the output of level density parameters and level densities for each residual nucleus.

*Examples:*

**outdensity y**

**outdensity n**

*Range:* y or n

*Default:* the same value as **outbasic: outdensity n**

**outomp**

Flag for the output of optical model parameters for each particle and energy.

*Examples:*

**outomp y**

**outomp n**

*Range:* y or n

*Default:* the same value as **outbasic: outomp n**

**outdirect**

Flag for the output of the results from the direct reaction calculation of ECIS (DWBA, giant resonances and coupled-channels).

*Examples:*

**outdirect y**

**outdirect n**

*Range:* y or n

*Default:* the same value as **outbasic: outdirect n**

**outinverse**

Flag for the output of particle transmission coefficients and inverse reaction cross sections.

*Examples:*

**outinverse y**

**outinverse n**

*Range:* y or n

*Default:* the same value as **outbasic**: **outinverse n**

**outtransenergy**

Flag for the output of transmission coefficients sorted per energy (**y**) or per angular momentum (**n**). **outtransenergy** is only active if **outinverse y**.

*Examples:*

**outtransenergy y**

**outtransenergy n**

*Range:* y or n

*Default:* **outtransenergy y**

**outecis**

Flag for keeping the various ECIS output files produced during a TALYS run. This is mainly for diagnostic purposes.

*Examples:*

**outecis y**

**outecis n**

*Range:* y or n

*Default:* **outecis n**

**outgamma**

Flag for the output of gamma-ray parameters, strength functions, transmission coefficients and reaction cross sections.

*Examples:*

**outgamma y**

**outgamma n**

*Range:* y or n

*Default:* the same value as **outbasic**: **outgamma n**

**outpreequilibrium**

Flag for the output of pre-equilibrium parameters and cross sections. **outpreequilibrium** is only active if **preequilibrium y**.

*Examples:*

**outpreequilibrium y**

**outpreequilibrium n**

*Range:* y or n

*Default:* **outpreequilibrium n**

**outfission**

Flag for the output of fission parameters, transmission coefficients and partial cross sections. **outfission** is only active if **fission y**.

*Examples:*

**outfission y**

**outfission n**

*Range:* y or n

*Default:* the same value as **outbasic**: **outfission n**

**outdiscrete**

Flag for the output of cross sections to each individual discrete state. This is given for both the direct and the compound component.

*Examples:*

**outdiscrete y**

**outdiscrete n**

*Range:* y or n

*Default:* the same value as **outbasic**: **outdiscrete n**

**adddiscrete**

Flag for the addition of energy-broadened non-elastic cross sections for discrete states to the continuum spectra. **adddiscrete** is only active if **outspectra y**.

*Examples:*

**adddiscrete y**

**adddiscrete n**

*Range:* y or n

*Default:* **adddiscrete y**

**addelastic**

Flag for the addition of energy-broadened elastic cross sections to the continuum spectra. This case is treated separately from **adddiscrete**, since sometimes the elastic contribution is already subtracted from the experimental spectrum. **addelastic** is only active if **outspectra y**.

*Examples:*

**addelastic y**

**addelastic n**

*Range:* **y** or **n**

*Default:* the same value as **adddiscrete**: **addelastic y**

**outspectra**

Flag for the output of angle-integrated emission spectra.

*Examples:*

**outspectra y**

**outspectra n**

*Range:* **y** or **n**

*Default:* **outspectra y** if only one incident energy is given in the input file, and **outspectra n** for more than one incident energy.

**elwidth**

Width of elastic peak in MeV. For comparison with experimental angle-integrated and double-differential spectra, it may be helpful to include the energy-broadened cross sections for discrete states in the high-energy tail of the spectra. **elwidth** is the width of the Gaussian spreading that takes care of this. **elwidth** is only active if **outspectra y** or if **ddxmode 1, 2** or **3**.

*Examples:*

**elwidth 0.2**

*Range:*  $1.e - 6 \leq \text{elwidth} \leq 100$

*Default:* **elwidth 0.5**

**outangle**

Flag for the output of angular distributions for scattering to discrete states.

*Examples:*

**outangle y**

**outangle n**

*Range:* **y** or **n**

*Default:* **outangle n**

**outlegendre**

Flag for the output of Legendre coefficients for the angular distributions for scattering to discrete states.

**outlegendre** is only active if **outangle y**.

*Examples:*

**outlegendre y**

**outlegendre n**

*Range:* **y** or **n**

*Default:* **outlegendre n**

**ddxmode**

Option for the output of double-differential cross sections. There are 4 possibilities.

*Examples:*

**ddxmode 0:** No output.

**ddxmode 1:** Output per emission energy as a function of angle (angular distributions).

**ddxmode 2:** Output per emission angle as a function of energy (spectra).

**ddxmode 3:** Output per emission energy and per emission angle.

*Range:*  $0 \leq \text{ddxmode} \leq 3$

*Default:* **ddxmode 0**. If there is a **fileddxe** keyword, see p. 163, in the input file, **ddxmode 1** will be set automatically. If there is a **fileddxa** keyword, see p. 164, in the input file, **ddxmode 2** will be set automatically. If both **fileddxe** and **fileddxa** are present, **ddxmode 3** will be set automatically.

**outdwba**

Flag for the output of DWBA cross sections for the multi-step direct model.

*Examples:*

**outdwba y**

**outdwba n**

*Range:* **y** or **n**

*Default:* **outdwba n**

**outgamdis**

Flag for the output of discrete gamma-ray intensities. All possible discrete gamma transitions for all nuclei are followed. In the output they are given in tables per nuclide and for each decay from state to state.

*Examples:*

**outgamdis y**

**outgamdis n**

*Range:* y or n

*Default:* **outgamdis n**

### **outexcitation**

Flag for the output of excitation functions, i.e. cross sections as a function of incident energy, such as residual production cross sections, inelastic cross sections, etc.

*Examples:*

**outexcitation y**

**outexcitation n**

*Range:* y or n

*Default:* **outexcitation y** if only one incident energy is given in the input file, and **outexcitation n** for more than one incident energy.

### **endf**

Flag for the creation of various output files needed for the assembling of an ENDF-6 formatted file. Apart from the creation of various files that will be discussed for the following keywords, a file *endf.tot* is created which contains the reaction, elastic and total cross sections (calculated by ECIS) on a fine energy grid. Also a file *decay.X* will be created, with X the ejectile symbol in (a1) format, that contains the discrete gamma decay probabilities for the binary residual nuclides. This will be used for gamma-ray production from discrete binary levels. In addition to all the output detailed below, the continuum gamma-ray spectra per residual nucleus and incident energy will be stored in files *gamZZZA-AAEYYY.YYY.tot*, where where ZZZ is the charge number and AAA is the mass number in (i3.3) format, and YYY.YYY is the incident energy in (f7.3) format. Setting **endf y** will automatically enable many of the “file” keywords given below.

*Examples:*

**endf y**

**endf n**

*Range:* y or n

*Default:* **endf n**

### **fi leelastic**

Flag to write the elastic angular distribution on a separate file *XXYYY.YYYang.L00*, where XX is the particle symbol in (2a1) format (e.g. *nn* for elastic scattering), and YYY.YYY the incident energy in (f7.3) format. The file contains the angle, and 3 columns containing the total, shape elastic, and compound

elastic angular distribution, respectively. If in addition **outlegendre y**, the elastic scattering Legendre coefficients will be written on a file *XXYYY.YYYleg.L00*. This file contains the *L*-value, and 4 columns containing the total, direct, compound and normalized Legendre coefficient. **fileelastic** is only active if **outangle y**.

*Examples:*

**fileelastic y**, giving files *nn014.000ang.L00*, and (if **outlegendre y**) *nn014.000leg.L00*, for an incident energy of 14 MeV.

**fileelastic n**

*Range:* **y** or **n**

*Default:* **fileelastic n**

### fi leangle

Designator for the output of the non-elastic angular distribution of one specific level on a separate file *PXYYY.YYYang.LMM*, where P and X are the particle symbols in (a1) format for the projectile and ejectile, respectively, YYY.YYY is the incident energy in (f7.3) format, and MM is the level number in (i2.2) format. The file contains the angle and 3 columns with the total inelastic, direct inelastic and compound inelastic angular distribution to the specified level. On the input line we read the level number. The **fileangle** keyword can appear more than once in an input file, one for each level that one is interested in. It will automatically produce files for all ejectiles. If in addition **outlegendre y**, the non-elastic scattering Legendre coefficients will be written on a file *PXYYY.YYYleg.LMM*. This file contains the *L*-value, and 4 columns containing the total, direct, compound and normalized Legendre coefficient. **fileangle** is only active if **outdiscrete y** and **outangle y**.

*Examples:*

**fileangle 2**, giving files *np014.000ang.L02* and (**outlegendre y**) *np014.000leg.L02*, for the (*n, p*) reaction to the second discrete level and an incident energy of 14 MeV, and similarly for the other ejectiles.

*Range:* **0 < fileangle < numlev**. Currently, **numlev=25**

*Default:* **fileangle** not active.

### fi lechannels

Flag to write the exclusive channel cross sections as a function of incident energy on separate files. The files will be called *xsNPDTHA.tot*, where N is the neutron number of the exclusive channel, P the proton number, etc., in (a1) format. For example *xs210000.tot* contains the excitation function for  $\sigma(n, 2np)$ , if the incident particle was a neutron. The files contain the incident energy and 3 columns with the exclusive cross section, the associated gamma-ray production cross section, and the fraction of this cross section relative to the total residual production cross section. If in addition isomers can be produced, files called *xsNPDTHA.LMM* will be created with MM the isomeric level number in (i2.2) format. If **filechannels y**, the exclusive binary continuum cross sections, such as continuum inelastic scattering, will also be written to files *PX.con*, where P and X are the particle symbols in (a1) format for

the projectile and ejectile, respectively. If *outspectra y*, the exclusive channel spectra will be written on files *spNPDTHAEYYY.YYY.tot* where *YYY.YYY* is the incident energy in (f7.3) format. The files contain the incident energy and 6 columns, with the spectra per outgoing particle type. **filechannels** is only active if **channels y**.

*Examples:*

**filechannels y**

**filechannels n**

*Range:* **y** or **n**

*Default:* **filechannels n**

### **fi lespectrum**

Designator for the output of the composite particle spectrum for a specific particle type on a separate file. On the input line we read the particle symbols. This will result in files *XspecYYY.YYY.tot*, where *X* is the outgoing particle symbol in (a1) format, and *YYY.YYY* the incident energy in (f7.3) format. The file contains the emission energy and 5 columns with the total, direct, pre-equilibrium, multiple pre-equilibrium and compound spectrum, respectively. **filespectrum** is only active if **outspectra y**.

*Examples:*

**filespectrum n p a**, giving files *nspec014.000.tot*, *pspec014.000.tot* and *aspec014.000.tot*, for an incident energy of 14 MeV.

*Range:* **n p d t h a**

*Default:* **filespectrum** not active.

### **fi leddxe**

Designator for the output of double-differential cross sections per emission energy for a specific particle type. On the input line we read the particle type and the emission energy. This will result in files *XddxYYY.Y.mev*, where *X* is the particle symbol in (a1) format and *YYY.Y* the emission energy in (f5.1) format. The file contains the emission angle and 5 columns with the total, direct, pre-equilibrium, multiple pre-equilibrium and compound spectrum, respectively. The **fileddxe** keyword can appear more than once in an input file, one for each outgoing energy that one is interested in. If there is at least one **fileddxe** keyword in the input **ddxmode**, see p. 160, will automatically be enabled.

*Examples:*

**fileddxe n 60.** (giving a file *nddx060.0.mev*).

*Range:* **n p d t h a** for the particles and **0.** -  $E_{inc}$  for outgoing energies.

*Default:* **fileddxe** not active.

**fileddxa**

Designator for the output of double-differential cross sections per emission angle for a specific particle type. On the input line we read the particle type and the emission angle. This will result in files *XddxYYY.Y.deg*, where X is the particle symbol in (a1) format and YYY.Y the emission angle in (f5.1) format. The file contains the emission energy and 5 columns with the total, direct, pre-equilibrium, multiple pre-equilibrium and compound spectrum, respectively. The **fileddxa** keyword can appear more than once in an input file, one for each outgoing angle that one is interested in. If there is at least one **fileddxa** keyword in the input **ddxmode**, see p. 160, will automatically be enabled.

*Examples:*

**fileddxa n 30.** (giving a file *nddx030.0.deg*).

*Range:* **n p d t h a** for the particles and **0. - 180.** for outgoing angles.

*Default:* **fileddxa** not active.

**filegamdis**

Flag to write the discrete gamma-ray intensities as a function of incident energy to separate files. This will result in files *gamZZZAAALYYLMM.tot*, where ZZZ is the charge number and AAA is the mass number in (i3.3) format, YY is the number of the initial discrete state and MM the number of the final discrete state. **filegamdis** is only active if **outgamdis y**.

*Examples:*

**filegamdis y**

**filegamdis n**

*Range:* **y** or **n**

*Default:* **filegamdis n**

**filetotal**

Flag to write all the total cross sections as a function of incident energy on a separate file *total.tot*. The file contains the incident energy, and 9 columns containing the non-elastic, total elastic, total, compound elastic, shape elastic, reaction, compound non-elastic, direct and pre-equilibrium cross section. In addition, the total particle production cross sections will be written on files *Xprod.tot*, with X the particle symbol in (a1) format. **filetotal** is only active if **outexcitation y** or **endf y**.

*Examples:*

**filetotal y**

**filetotal n**

*Range:* **y** or **n**

*Default:* **filetotal n**

**fi leresidual**

Flag to write all the residual production cross sections as a function of incident energy on separate files. The files for the total (i.e. the sum over ground state + isomers) residual production cross sections have the name *rpZZZAAA.tot* where ZZZ is the charge number and AAA is the mass number in (i3.3) format. If a residual nuclide contains one or more isomeric states, there are additional files *rpZZZAAA.LMM*, where MM is the number of the isomer (ground state=0) in (i2.2) format. The files contain the incident energy and the residual production cross section. **fileresidual** is only active if **outexcitation y** or **endf y**.

*Examples:*

**fileresidual y**

**fileresidual n**

*Range:* y or n

*Default:* **fileresidual n**

**fi lerecoil**

Flag to write the recoil spectra of the residual nuclides as a function of incident energy on separate files. The files for the recoil spectra have the name *recZZZAAAspecYYY.YYY.tot* where ZZZ is the charge number and AAA is the mass number in (i3.3) format and YYY.YYY the incident energy in (f7.3) format. If in addition **flagchannels y**, there are additional files *spNPDTHAEYYY.YYY.rec*, where N is the neutron number of the exclusive channel, P the proton number, etc. The files contain the incident energy and the recoil.

*Examples:*

**filerecoil y**

**filerecoil n**

*Range:* y or n

*Default:* **filerecoil n**

**fi lefission**

Flag to write all the fission cross sections as a function of incident energy on a separate file *fission.tot*. The file contains the incident energy and the total fission cross section. If in addition *filechannels y*, the exclusive fission cross sections will be written to files *fisNPDTHA.tot*, where N is the neutron number of the exclusive channel, P the proton number, etc., in (a1) format. For example, *fis200000.tot* contains the excitation function for  $\sigma(n, 2nf)$ , also known as the third chance fission cross section. **filefission** is only active if **fission y**.

*Examples:*

**filefission y**

**filefission n**

*Range:* y or n

*Default:* **filefission n**

**filediscrete**

Designator for the output of the excitation function of one specific non-elastic level on a separate file *PX.LMM*, where P and X are the particle symbols in (a1) format for the projectile and ejectile, respectively, and MM is the level number in (i2.2) format. The file contains the incident energy and 3 columns with the total inelastic, direct inelastic and compound inelastic cross section to the specified level. On the input line we read the level number. The **filediscrete** keyword can appear more than once in an input file, one for each level that one is interested in. It automatically produces a file for each ejectile. **filediscrete** is only active if **outdiscrete y**.

*Examples:*

**filediscrete 2** , giving files *nn.L02*, *np.L02*, etc. for the excitation functions of (inelastic and other) neutron scattering to the second discrete level.

*Range:* **0 < filediscrete < numlev**. Currently, **numlev=25**

*Default:* **filediscrete** not active.

**6.2.11 Input parameter table**

From all the keywords given above you can see that certain default values depend on mass, energy or other parameters. In table 6.1 we summarize all these dependencies and give the full table of keywords including their relation with each other.

Table 6.1: The keywords of TALYS.

Keyword	Range	Default	Page
a	1. - 100.	table or systematics	142
abundance	filename	no default	126
addiscrete	y,n	y	158
addelastic	y,n	y	159
alimit	1. - 100.	systematics	143
alphald	0.01 - 0.1	systematics	143
angles	1-numang (90)	90	123
anglescont	1-numangcont (36)	36	124
anglesrec	1-numangrec (18)	9	125
asys	y,n	n	142
autorot	y,n	n	129
axtype	1,2	1 and 2 for $N > 144$	151
beta2	0. - 2.	0.-1.0 (barrier dep.)	147
betald	0. - 0.5	systematics	143
bins	2 - numbins (100)	40	119
c1table	0. - 1.e6	1.	148
c2table	-10. - 10.	0.	148
cfermi	0. - 1000.	10.	146
cfermibf	0. - 1000.	10.	147
channelenergy	y,n	n	126
channels	y,n	n	124
class2	y,n	n	152
class2file	filename	no default	153
class2width	0.01 - 10.	0.2	153
colldamp	y,n	n	146
compound	y,n	y	132
core	-1,1	-1	129
D0	1.e-6 - 10000.	table	136
ddxmode	0 - 3	0	160
deformfile	filename	no default	132
deltaW	-20. - 20.	calculated	144
E0	-10. - 10.	calculated	146
eciscalc	y,n	y	130
eciscompound	y,n	n	134

Continuation of **Table 6.1.**

Keyword	Range	Default	Page
ecisdwba	y,n	y	141
ecissave	y,n	n	130
egr	1. - 100.	table or systematics	135
ejectiles	g n p d t h a	g n p d t h a	118
electronconv	y,n	n	135
element	3 - 109 or Li - Mt	no default	116
Elow	1.e-6 - 1.	$D_0$	122
elwidth	1.e-6 - 100.	0.5	159
Emsdmin	>0.	Eninc/5.	141
endf	y,n	n	161
energy	1.e-11 - 250.	no default	117
Esurf	0. - 38.	systematics	139
Exmatch	0.1 - 20.	calculated	145
ffevaporation	y,n	n	154
fileangle	0 - numlev(25)	no default	162
filechannels	y,n	n	162
fileddxa	n,...,a 0. - 180.	no default	164
fileddxe	n,...,a 0. - energy	no default	163
filediscrete	0 - numlev(25)	no default	166
fileelastic	y,n	n	161
filefission	y,n	n	165
filegamdis	y,n	n	164
filerecoil	y,n	n	165
fileresidual	y,n	n	165
filespectrum	g n p d t h a	no default	163
filetotal	y,n	n	164
fisbar	0. - 100.	table or systematics	151
fishw	0.01 - 10.	table or systematics	151
fismodel	1 - 4	1	150
fismodelalt	3 - 4	4	150
fission	y,n,A $\geq$ 56	y for mass > 209, n for mass $\leq$ 209	150
fullhf	y,n	n	133
g	0.1-100.	systematics	149

Continuation of **Table 6.1.**

Keyword	Range	Default	Page
gamgam	0. - 10.	table or systematics	136
gammald	0.01 - 1.	systematics	143
gammashell1	0. - 1.	systematics	144
gammashell2	0. - 0.2	0.	144
gammax	1 - 6	2	134
ggr	1. - 100.	table or systematics	136
giantresonance	y,n	y for n,p; n otherwise	132
gn	0.1 - 100.	systematics	149
gnorm	0. - 100.	calculated	134
gp	0.1 - 100.	systematics	149
gshell	y,n	n	149
hbtransfile	filename	no default	152
inccalc	y,n	y	130
isomer	0. - 1.e38	1.	122
Kph	1. - 100.	15.	148
Krotconstant	0.01 - 100.	1.	148
labddx	y,n	n	125
ldmodel	1 - 3	1	142
levelfile	filename	no default	122
localomp	y,n	y	128
Ltarget	0 - numlev (25)	0	118
M2constant	0. - 100.	1.	139
M2limit	0. - 100.	1.	140
M2shift	0. - 100.	1.	140
mass	0, 5 - 339	no default	116
massdis	y,n	n	154
maxband	0 - 100	0	131
maxchannel	0 - numchannel (8)	4	124
maxenrec	0 - numenrec (25)	10	125
maxlevelsbin	0 - numlev (25)	10 (g,n,p,a) and 5 (d,t,h)	121
maxlevelsres	0 - numlev (25)	10	121
maxlevelstar	0 - numlev (25)	20	120
maxN	0 - numN-2 (25)	25	119
maxrot	0 - 20	2	131

Continuation of **Table 6.1.**

Keyword	Range	Default	Page
maxZ	0 - numZ-2 (10)	10	119
mpreeqmode	1 - 2	1	138
msdbins	2 - numenmsd/2-1 (8)	6	141
multipreeq	y,n or 0.001 - 250.	20.	137
Nlevels	0 - numlev (25)	equal to maxlevelsres	121
Nlow	0 - 200	2	145
Ntop	0 - 200	table or equal to Nlevels	145
onestep	y,n	n	141
optmod	filename	no default	127
optmodall	y,n	n	129
optmodfileN	filename	no default	127
optmodfileP	filename	no default	128
outangle	y,n	y for one energy, n for many	159
outbasic	y,n	n	155
outcheck	y,n	equal to outbasic	155
outdensity	y,n	equal to outbasic	156
outdirect	y,n	equal to outbasic	156
outdiscrete	y,n	equal to outbasic	158
outdwba	y,n	n	160
outecis	y,n	n	157
outexcitation	y,n	n for one energy, y for many	161
outfission	y,n	equal to outbasic	158
outgamdis	y,n	n	160
outgamma	y,n	equal to outbasic	157
outinverse	y,n	equal to outbasic	157
outlegendre	y,n	n	160
outlevels	y,n	equal to outbasic	156
outmain	y,n	y	154
outomp	y,n	equal to outbasic	156
outpopulation	y,n	equal to outbasic	155
outpreequilibrium	y,n	n	158
outspectra	y,n	y for one energy, n for many	159
outtransenergy	y,n	y	157
pair	0. - 10.	systematics	144

Continuation of **Table 6.1.**

Keyword	Range	Default	Page
partable	y,n	n	127
popeps	0. - 1000.	1.e-3	123
preeqcomplex	y,n	y	139
preeqmode	1 - 4	2	137
preeqspin	y,n	n	138
preeqsurface	y,n	y	138
preequilibrium	y,n or 0.001 - 250.	Ex(NL)	137
projectile	n,p,d,t,h,a,g	no default	116
Rclass2mom	0.1 - 10.	1.	152
recoil	y,n	n	125
recoilaverage	y,n	n	126
relativistic	y,n	y	124
Rfiseps	0. - 1.	1.e-3	153
Rgamma	0. - 100.	2.	140
rotational	n p d t h a	n p	131
Rpinu	0. - 100.	1.	140
Rspincut	0. - 10.	1.	147
Rtransmom	0.1 - 10.	1.	152
S0	0. - 10.	table	136
segment	1 - 4	1	120
sgr	0. - 10000.	table or systematics	135
spherical	y,n	n	131
statepot	y,n	n	129
strength	1 - 2	1	134
sysreaction	n p d t h a	d t h a	128
T	0.001 - 10.	calculated	145
transeps	0. - 1.	1.e-8	123
transpower	2 - 20	5	122
twocomponent	y,n	n	139
Ufermi	0. - 1000.	30.	146
Ufermibf	0. - 1000.	45.	147
widthfluc	y,n or 0.001 - 20.	S(projectile)	132
widthmode	0 - 3	1	133
xseps	0. - 1000.	1.e-7	123



## Chapter 7

# Computational structure of TALYS

### 7.1 General structure of the source code

The source of TALYS-0.64 is written in Fortran77, and we assume it can be successfully compiled with any f77 or f90/f95 compiler. We have aimed at a setup that is as modular as Fortran77 allows it to be, using programming procedures that are consistent throughout the whole code. In total, there are 253 Fortran subroutines, which are connected through one file, *talys.cmb*, in which all global variables are declared and stored in common blocks. This adds up to a total of more than 40000 lines, of which about 45% are comments. These numbers do not include the *ecis97t* subroutine (20202 lines), see below. On a global level, the source of TALYS consists of 3 main parts: Input, initialisation and reaction calculation. This structure can easily be recognized in the main program, *talys*, which consists merely of calls to the following 5 subroutines:

```
TALYS
|--machine
|--constants
|--talysinput
|--talysinitial
|--talysreaction
|--natural
```

#### 7.1.1 machine

In this subroutine, the database is set for the directories with nuclear structure information. This subroutine may contain the only machine-dependent statements.

#### 7.1.2 constants

In this subroutine the fundamental constants are defined. First, in the block data module **constants0** the nuclear symbols and the fundamental properties of particles are defined. Also, the magic numbers, character strings for the two possible parity values and a few fundamental constants are initialized. From these constants, other constants that appear in various reaction formulae are directly defined in subroutine

*constants*. Examples are  $2\pi/\hbar$ ,  $\hbar c$ ,  $1/\pi^2\hbar^2c^2$ ,  $1/\pi^2\hbar^3c^2$  and  $amu/\pi^2\hbar^3c^2$ . In the initialisation, they are directly defined in units of MeV and mb. Also, a few other constants are set.

### 7.1.3 talysinput

Subroutine for the user input of keywords and their defaults.

### 7.1.4 talysinitial

Subroutine for the initialisation of nuclear structure and other basic parameters.

### 7.1.5 talysreaction

Subroutine with reaction models.

### 7.1.6 natural

For calculations of reactions on natural elements a fifth subroutine may be called, namely a subroutine to handle natural elements as target. In this subroutine, another loop over *talysinput*, *talysinitial* and *talysreaction* is performed, for each isotope of the element.

### 7.1.7 ecis97t

Another integral part of TALYS that should explicitly be mentioned is Raynal's multi-disciplinary reaction code ECIS-97, which we have included as a subroutine. It is called several times by TALYS for the calculation of basic reaction cross sections, angular distributions and transmission coefficients, for either spherical or deformed nuclei. To enable the communication between ECIS-97 and the rest of TALYS, a few extra lines were added to the original ECIS code. These include a few extra write statements that put information on an ECIS output file, which is not done by the original code. In the source *ecis97t.f* our modifications, not more than 30 lines, can be recognized by the extension *ak000000* in columns 73-80.

We will now describe the main tasks of the three main subroutines mentioned above. We will start with the calling sequence of the subroutines, followed by an explanation of each subroutine. A subroutine will only be explained the first time it appears in the calling tree. Moreover, if a subtree of subroutines has already been described before in the text, we put a ">" behind the name of the subroutine, indicating it can be found in the text above.

## 7.2 Input: talysinput

The subroutine *talysinput* deals with the user input of keywords and their defaults and consists of calls to the following subroutines:

```
talysinput
|--readinput
|--input1
```

```

|--abundance
|--input2
|--input3
|--input4
|--input5
|--input6
|--checkkeyword
|--checkvalue

```

### 7.2.1 readinput

This subroutine reads in all the lines from the user input file as character strings and transfers them to lower case, for uniformity. The actual reading of the keywords from these lines is done in the next six subroutines.

### 7.2.2 input1

In *input1*, the four main keywords **projectile**, **element**, **mass** and **energy** are read and it is determined whether there is only one incident energy (directly given as a number in the input file) or a range of incident energies (given in an external file), after which the energy or range of energies are read in. The maximal incident energy is determined, the incident particle is identified, and the numerical  $Z$ ,  $N$  and  $A$  values for the target are set. For natural targets, *input1* also calls the following subroutine,

#### abundance

In *abundance*, the isotopic abundances are read from the database or from a user input file, if present.

### 7.2.3 input2, input3, input4, input5, input6

In the other 5 subroutines, all other keywords that can be present in the input file are identified. Most of them are first set to their default values at the beginning of the subroutine, after which these values can be overwritten by means of a read statement. In all input subroutines, checks are built in for the most flagrant input errors. For example, if a character string is read from the input file where a numerical value is expected, TALYS warns the user and gracefully stops. Subroutine *input2* deals with general physical parameters, *input3* deals with choices for nuclear models, *input4* deals with choices for the output, *input5* deals with nuclear model parameters, and *input6* deals with output to be written to specific files. The order of these subroutines, and the information in them, is important since sometimes defaults are set according to previously set flags.

### 7.2.4 checkkeyword

In this subroutine, we check whether all keywords given by the user are valid. If for example the wrongly typed keyword **projjectile** appears in the input, TALYS stops after giving an error message.

### 7.2.5 checkvalue

This subroutine performs a more intelligent check on erroneous input values. Values of parameters which are out of the ranges that were specified in Chapter 6, and are thus beyond physically reasonable values, are detected here. In such cases the program also gives an error message and stops. Sufficiently wide ranges are set, i.e. the input values have to be really ridiculous before TALYS stops.

## 7.3 Initialisation: talysinitial

In subroutine *talysinitial*, nuclear structure and other basic parameters are initialised. It consists of calls to the following subroutines:

```
talysinitial
|--particles
|--nuclides
|--grid
|--mainout
```

### 7.3.1 particles

In *particles*, it is determined, on the basis of the **ejectiles** keyword (page 118), which particles are included and which are skipped as competing particles in the calculation. The default is to include all particles from photons to alpha's as competing channels. If specific outgoing particles in the input are given, only those will be included as competing channels. This sets the two logical variables **parinclude** and **parskip**, which are each others' opposite and are used throughout TALYS.

### 7.3.2 nuclides

In *nuclides* the properties of the involved nuclides are set. The following subroutines are called:

```
nuclides
|--strucinitial
|--masses
|--separation
|--structure
|--weakcoupling
|--sumrules
|--kalbachsep
```

First, in *nuclides* we assign the Z, N, and A of all possible residual nuclei. In TALYS we make use of both absolute and relative designators to describe the nuclides. This is illustrated in Fig. 7.1.

ZZ, NN, AA, Zinit, Ninit, Ainit, Ztarget, Ntarget, Atarget, represent true values of the charge, neutron and mass number. The extension 'init' indicates the initial compound nucleus and 'target' corresponds to the target properties. Zix, Nix, Zcomp and Ncomp are indices relative to the initial compound nucleus. The initial compound nucleus (created by projectile + target) has the indices (0,0). The first index represents the number of protons and the second index the number of neutrons away from the initial

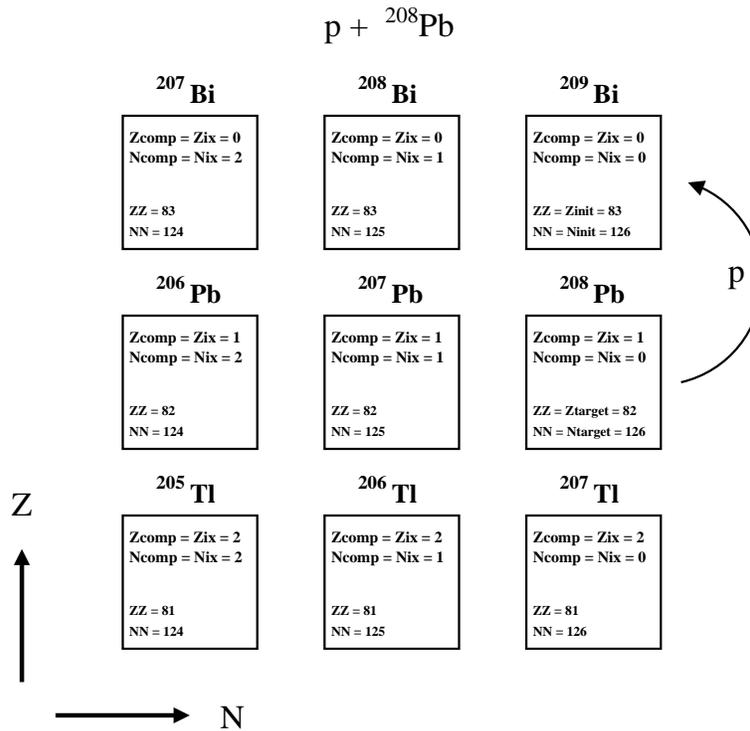


Figure 7.1: Illustration of the various nuclide designators used throughout TALYS.

compound nucleus. Example: For the reaction  $p + {}^{208}\text{Pb}$ , the set (0,0) represents  ${}^{209}\text{Bi}$  and the set (1,2) represents  ${}^{206}\text{Pb}$ . In the calculation  $Z_{ix}$  and  $N_{ix}$  are used in loops over daughter nuclides and  $Z_{comp}$  and  $N_{comp}$  are used in loops over decaying mother nuclides. In addition, TALYS makes use of the arrays  $Z_{index}$  and  $N_{index}$ , which are the first two indices of many other arrays. At any point in the reaction calculation, given the indices of the mother nucleus  $Z_{comp}$ ,  $N_{comp}$  and the particle type, these relative nuclide designators will be directly known through the arrays we initialize in this subroutine.

As an example for the  ${}^{56}\text{Fe}(n,p){}^{56}\text{Mn}$  reaction:  $Z_{target}=26$ ,  $N_{target}=30$ ,  $Z_{comp}=0$  (primary compound nucleus),  $N_{comp}=0$  (primary compound nucleus),  $Z_{index}=1$ ,  $N_{index}=0$ ,  $Z_{init}=26$ ,  $N_{init}=31$ ,  $ZZ=25$ ,  $NN=31$ . Next, many structure and model parameters are set. This is done by calling the subroutines mentioned above. Nuclear structure properties for the target,  $Q$ -values and the Coulomb barriers are also set in *nuclides*. Finally, some set-off energies for pre-equilibrium and width fluctuation corrections are set here. The subroutines called are:

### strucinitial

This subroutine merely serves to initialize a lot of arrays. Also, the energy grid for tabulated level densities are set.

### masses

In *masses* the nuclear masses are read from the mass table. The following subroutines are called:

```
masses
|--duflo
```

We read both the experimental masses, of Audi-Wapstra, and the theoretical masses, of Möller, from the mass table. The experimental nuclear mass is adopted, when available. We also read the experimental and theoretical mass excess, to enable a more precise calculation of separation energies. If a residual nucleus is not in the experimental/theoretical mass table, we use the analytical formula of Duflo-Zuker. Finally, the so-called reduced and specific masses are calculated for every nucleus.

*duflo*

Subroutine with the analytical mass formula of Duflo-Zuker.

### separation

In *separation*, the separation energies for all light particles on all involved nuclides are set. For consistency, separation energies are always calculated using two nuclear masses of the same type, i.e. both experimental or both theoretical. Hence if nucleus A is in the experimental part of the table but nucleus B is not, for both nuclides the theoretical masses are used.

### structure

This is a very important subroutine. In *structure*, for each nuclide that can be reached in the reaction chain the nuclear structure properties are read in from the nuclear structure and model database. If the nuclear parameters are not available in tabular form they are computationally determined. TALYS is written such that a call to *structure* only occurs when a new nuclide is encountered in the reaction chain. First, it is called for the binary reaction. Later on, in *multiple*, the call to *structure* is repeated for nuclides that can be reached in multiple emission. The full calling tree is as follows:

```
structure
|--levels
|--gammadecay
|--deformpar
|--resonancepar
|--gammapar
|--omppar
|--fissionpar
|--densitypar
|--densitymatch
|--densitytable
|--d0theory
|--partable
```

*levels*

In *levels*, the discrete level information is read. First, for any nuclide, we assign a 0+ ground state to even-even and odd-odd nuclei and a 1/2+ ground state to odd nuclei. Of course, if there is information in

the discrete level file, this will be overwritten by the full discrete level info. The amount of information that is read in is different for the first several levels and higher lying levels. For the discrete levels that explicitly appear in the multiple Hauser-Feshbach decay (typically the first 20 levels), we need all information, i.e. the energy, spin, parity, lifetime and branching ratio's. We also read extra levels which are used only for the level density matching problem or for direct reactions (deformation parameters) in the continuum. The branching ratios and lifetimes are not read for these higher levels. In *levels*, it is also determined whether the target nucleus is in an excited state, in which case the level properties are read in.

#### *gammadecay*

For ENDF-6 data files, specific information on gamma-ray branching ratios, namely the cumulated flux originating from a starting level, needs to be handled. This is performed in *gammadecay*.

#### *deformpar*

In *deformpar*, the deformation parameters or deformation lengths are read, together with the associated coupling scheme for the case of coupled-channels calculations. In the case of vibrational nuclides, simple systematical formulae are used for the first few excited states if no experimental information is available. Spherical (S), vibrational (V) or rotational (R) coupled-channels calculations are automated. Finally, the deformation parameter for rotational enhancement of fission barrier level densities is read in from the nuclear structure database.

#### *resonancepar*

The experimental values from the resonance parameter file,  $D_0$ ,  $\Gamma_\gamma$ , and  $S_0$  are read here. A simple systematics for  $\Gamma_\gamma$  derived by Kopecky (2002), is provided in the block data module **gamdata** for nuclides not present in the table.

#### *gammapar*

In *gammapar*, the default giant dipole resonance parameters for gamma-ray strength functions are read from the database. Also the default values for M1, E1, E2 etc., are set using systematics if no value is present in the database [36].

#### *omppar*

The optical model parameters for nucleons are read from the database. If there are no specific parameters for a nuclide, they are determined by a global optical model for neutrons and protons. Also possible user-supplied input files with optical model parameters are read here.

#### *fissionpar*

In *fissionpar*, the fission barrier parameters are read, using the following subroutines:

```
fissionpar
|--barsierk
  |--plegendre
|--rldm
|--rotband
|--rotclass2
```

Several databases with fission barrier parameters can be read. There are also calls to two subroutines, *barsierk* and *rldm*, which provide systematical predictions for fission barrier parameters from Sierk's model and the rotating liquid drop model, respectively. As usual, it is also possible to overrule these parameters with choices from the user input. If *fismodel 1*, also the head band states and possible class II states are read in this subroutine. Finally, rotational bands are built on transition and class II states. Note that next to the chosen fission model (**fismodel**), there is always an alternative fission model (**fismodelalt**) which comes into play if fission parameters for the first choice model are not available.

#### *barsierk*

Using the rotating finite range model, the  $l$ -dependent fission barrier heights are estimated with A.J. Sierk's method. This subroutine returns the fission barrier height in MeV. It is based on calculations using yukawa-plus-exponential double folded nuclear energy, exact Coulomb diffuseness corrections, and diffuse-matter moments of inertia [91]. The implementation is analogous to the subroutine "asierk" written by A.J. Sierk (LANL, 1984). This subroutine makes use of the block data module *fisdata*.

#### *plegendre*

This function calculates the Legendre polynomial.

#### *rldm*

Using the rotating liquid drop model [92], the fission barrier heights are estimated. This subroutine returns the fission barrier height in MeV and is based on the subroutine FISROT incorporated in ALICE-91 [32]. This subroutine makes use of the block data module *fisdata*.

#### *rotband*

Here, the rotational bands are built from the head band transition states, for fission calculations.

#### *rotclass2*

Here, the rotational bands are built from the class II states. For this, the maximum energy of class II states is first determined.

#### *densitypar*

In *densitypar*, parameters for the level density are set, or read from the database. The following subroutines are called:

```
densitypar
|--mliquid
```

All parameters of the Ignatyuk formula are determined, either from systematics or from mutual relations. There are many input possibilities for the energy-dependent level density parameter of the Ignatyuk formula. The required parameters are *alev*, *alimit*, *gammald* and *deltaW*. The Ignatyuk formula implies that these parameters can not *all* be given at the same time in the input file, or in a table. All possibilities are handled in this subroutine. Also, the single-particle state density parameters are set.

#### *mliquid*

Function to calculate the Myers-Swiatecki liquid drop mass for spherical nuclei.

#### *densitymatch*

The following subroutines are called:

```
densitymatch
|--ignatyuk
|--aldmatch
|--fermi
|--matching
|--poll
```

In *densitymatch*, the matching levels for the temperature and Fermi gas level densities are determined, and the level density matching problem is solved for both ground-state level densities and level densities on fission barriers. For this, the spin cutoff parameter for the discrete energy region is also determined. The matching problem is solved by calling *matching*.

#### *ignatyuk*

The level density parameter as function of excitation energy is calculated here. A Fermi distribution for the asymptotic level density parameter is also built in. This takes the damping of collective effects into account in a phenomenological way. The level density parameters are then equal to  $A/13$  in the high-energy limit rather than  $A/8$ , if **colldamp y**.

#### *aldmatch*

For fission, the effective level density parameter is obtained in three steps: (1) create the total level density in Fermi gas region, (2) apply a rotational enhancement to the total level density (3) determine the effective level density parameter by equating the rotational enhanced level density by a new effective total level density. The calling tree is:

```
aldmatch
|--ignatyuk
|--fermi
|--spindis
```

```
--colenhance
--spincut
```

### *fermi*

In *fermi*, the Fermi gas level density is calculated. The calling tree is:

```
fermi
  |--spincut
    |--ignatyuk
```

### *spincut*

In *spincut*, the spin-cutoff factor is calculated. Above the matching energy, this is done by an energy-dependent systematical formula. Below the matching energy, the value for the spin cutoff parameters is interpolated from the value at the matching energy and the value from the discrete energy region.

### *spindis*

In *spindis*, the Wigner spin distribution is calculated. The calling tree is:

```
spindis
  |--spincut >
```

### *colenhance*

In *colenhance*, the collective (vibrational and rotational) enhancement for fission level densities is calculated. Here, a distinction is made between (a) **ldmodel 1**: collective effects for the ground state are included implicitly in the intrinsic level density, and collective effects on the barrier are determined relative to the ground state, and (b) **ldmodel 2**: both ground state and barrier collective effects are included explicitly. The calling tree is:

```
colenhance
  |--ignatyuk
```

### *matching*

In *matching*, the matching problem of Eq. (4.225) is solved. First, we determine the possible region of the roots of the equation, then we determine the number of solutions and finally we choose the solution for our problem. The calling tree is:

```
matching
  |--ignatyuk
  |--zbrak
  |--rtbis
  |--match
    |--ignatyuk
    |--aldmatch >
```

```

|--poll
|--fermi >

```

*zbrak*

This subroutine finds the region in which the matching equation has a root (“bracketing” a function).

*rtbis*

This function finds the roots of a function.

*match*

This function represents Eq. (4.225).

*poll*

Subroutine for interpolation of first order.

*densitytable*

This subroutine reads in the tabulated level densities from Goriely.

*d0theory*

Subroutine to calculate the theoretical average resonance spacing  $D_0$  from the level density. The following subroutines are called:

```

d0theory
|--density

```

*density*

This is the function for the level density. It is calculated as a function of the excitation energy, spin, parity, fission barrier and model identifier. On the basis of **ldmodel**, the level density model is chosen. The following subroutines are called:

```

density
|--ignatyuk
|--rotenhance
|--colenhance >
|--gilcam
|--fermi >
|--spindis >
|--locate

```

*gilcam*

In *gilcam*, the Gilbert-Cameron level density formula is calculated with the constant temperature and the Fermi gas expression.

*locate*

Subroutine to find a value in an ordered table.

*partable*

Subroutine to write model parameters per nucleus to a separate output file.

**weakcoupling**

Subroutine *weakcoupling* is only called for odd target nuclides. The even-even core is determined and its deformation parameters, if any, are retrieved. These are then re-distributed over the levels of the odd-nucleus, so that later on DWBA calculations with the even core can be made. The selection of the odd-nucleus levels is automatic, and certainly not full proof. The following subroutines are called:

```
weakcoupling
|--deformpar >
|--levels >
```

**sumrules**

Using sum rules for giant resonances, the collective strength in the continuum is determined. The deformation parameters of the collective low lying states are subtracted from the sum, so that the final GR deformation parameters can be determined.

**kalbachsep**

In *kalbachsep*, the separation energies for the Kalbach systematics are computed. We use the Myers-Swiatecki parameters as used by Kalbach [72].

**7.3.3 grid**

In subroutine *grid*, the outgoing energy grid to be used for spectra and the transmission coefficients and inverse reaction cross section calculation is fixed. This non-equidistant grid ensures that the calculation for outgoing energies of a few MeV (around the evaporation peak) is sufficiently precise, whereas at higher energies a somewhat coarser energy grid can be used. For the same reason, this energy grid is used for the calculation of transmission coefficients. The begin and end of the energy grid for charged particles is set. The energy grid for which TALYS uses extrapolation (basically from thermal energies up to the first energy where we believe in a nuclear model code) is set. Also a few parameters for the angular grid and the transmission coefficient numerical limit are set here. The following subroutines are called:

```

grid
|--energies
  |--locate
|--locate

```

### energies

This subroutine is called for each new incident energy. The center-of-mass energy and the wave number are calculated (relativistic and non-relativistic), the upper energy limit for the energy grid is set, as well as the outgoing energies that belong to discrete level scattering. Finally, several incident energy-dependent flags are disabled and enabled.

#### 7.3.4 mainout

Subroutine *mainout* takes care of the first part of the output. The output of general information such as date, authors etc., is printed first. Next, the basic reaction parameters are printed. The following subroutines are called:

```

mainout
|--inputout
  |--yesno
|--levelsout
|--densityout
  |--rotenhance
  |--colenhance >
  |--spincut >
  |--ignatyuk
  |--gilcam >
  |--density >
|--fissionparout

```

### inputout

In this subroutine, the (default) values of all input keywords are written. This will appear at the top of the output file.

*yesno*

Function to assign the strings 'y' and 'n' to the logical values .true. and .false..

### levelsout

In *levelsout*, all discrete level information for the nucleus under consideration is printed.

### densityout

In *densityout*, all level density parameters are written, together with a table of the level density itself. For fissile nuclides, also the level densities on top of the fission barriers are printed.

**fissionparout**

In this subroutine, we write the main fission parameters, such as barrier heights and widths, and the head band transition states, rotational band transition states and class II states.

**7.4 Nuclear models: talysreaction**

The main part of TALYS, *talysreaction*, contains the implementation of all the nuclear reaction models. First it calls *basicxs*, for the calculation of transmission coefficients, inverse reaction cross sections, etc. which are to be calculated only once (i.e. regardless of the number of incident energies). Next, for either one or several incident energies, subroutines for the nuclear reaction models are called according to the flags set by default or by input. During these nuclear model calculations, information such as cross sections, spectra, angular distributions, and nuclide populations, is collected and stored. At the end, all results are collected and transferred to the requested output. Finally, a message that the calculation was successful should be printed. The following subroutines are called:

```
talysreaction
|--basicxs
|--preeqinit
|--excitoninit
|--compoundinit
|--energies >
|--reacinitial
|--incident
|--exgrid
|--recoilinit
|--direct
|--preeq
|--population
|--compnorm
|--comptarget
|--binary
|--angdis
|--multiple
|--channels
|--totalxs
|--spectra
|--massdis
|--residual
|--totalrecoil
|--thermal
|--output
|--finalout
|--endf
|--timer
```

### 7.4.1 basicxs

The transmission coefficients and inverse reaction cross sections for the outgoing energy grid need to be calculated only once for all particles and gamma's, for energies up to the maximal incident energy. The following subroutines are called:

```
basicxs
|--basicinitial
|--inverse
|--gamma
```

#### **basicinitial**

In *basicinitial*, all arrays that appear in this part of the program are initialized.

#### **inverse**

Subroutine *inverse* organises the calculation of total, reaction and elastic cross sections and transmission coefficients for all outgoing particles and the whole emission energy grid (the inverse channels). The following subroutines are called:

```
inverse
|--inverseecis
|--inverseread
|--inversenorm
|--inverseout
```

#### *inverseecis*

In this subroutine the loop over energy and particles is performed for the basic ECIS calculations. For each particle and energy, the optical model parameters are determined by calling *optical*. The subroutine *ecisinput* is called for the creation of the ECIS input files. At the end of this subroutine, *ecis97t* is called to perform the actual ECIS calculation. The following subroutines are called:

```
inverseecis
|--ecisinput
  |--optical
|--optical
|--ecis97t >
```

#### *ecisinput*

This subroutine creates a standard ECIS input file for spherical or coupled-channels calculations.

*optical*

This is the main subroutine for the determination of optical model parameters. The following subroutines are called:

```

optical
|--opticaln
|--opticalp
|--opticald
  |--opticaln
  |--opticalp
|--opticalt
  |--opticaln
  |--opticalp
|--opticalh
  |--opticaln
  |--opticalp
|--opticala
  |--opticaln
  |--opticalp

```

*opticaln, opticalp*

Subroutines for the neutron and proton optical model parameters. If an optical model file is given with the **optmod** keyword, see page 127, we interpolate between the tabulated values. In most cases, the general energy-dependent form of the optical potential is applied, using parameters per nucleus or from the global optical model, both from subroutine *omppar*.

*opticald, opticalt, opticalh, opticala*

Subroutines for deuteron, triton, helion and alpha optical potentials. In the current version of TALYS, we use the Watanabe method [41] to make a composite particle potential out of the proton and neutron potential.

*inverseread*

In this subroutine the results from ECIS are read. For every particle and energy we first read the reaction (and for neutrons the total and elastic) cross sections. Next, the transmission coefficients are read into the array Tjl, which has four indices: particle type, energy, spin and l-value. For spin-1/2 particles, we use the array indices -1 and 1 for the two spin values. For spin-1 particles, we use -1, 0 and 1 and for spin-0 particles we use 0 only. For rotational nuclei, we transform the rotational transmission coefficients into their spherical equivalents for the compound nucleus calculation. Also, transmission coefficients averaged over spin are put into separate arrays. For each particle and energy, the maximal l-value is determined to constrain loops over angular momentum later on in the code.

*inversenorm*

In *inversenorm*, a semi-empirical formula for the reaction cross section can be invoked to overrule the results from the optical model. This is sometimes appropriate for complex particles. The normalization is only performed if the option for semi-empirical reaction cross sections is enabled. The semi-empirical results have a too sharp cutoff at low energies. Therefore, for the lowest energies the optical model results are renormalized with the ratio at the threshold. The following subroutines are called:

```
inversenorm
|--tripathi
   |--radius
```

*tripathi*

Function for semi-empirical formula for the reaction cross section by Tripathi et al.. The original coding (which is hard to understand) does not coincide with the formulae given in Ref. [43] though the results seem to agree with the plotted results.

*radius*

Function for the radius, needed for the Tripathi systematics.

*inverseout*

This subroutine takes care of the output of reaction cross sections and transmission coefficients. Depending on the **outtransenergy** keyword, see page 157, the transmission coefficients are grouped per energy or per angular momentum.

**gamma**

This subroutine deals with calculations for gamma cross sections, strength functions and transmission coefficients. The following subroutines are called:

```
gamma
|--gammanorm
|--gammaout
```

*gammanorm*

In this subroutine, we normalise the gamma-ray strength functions by imposing the condition that the transmission coefficients integrated from zero up to neutron separation energy are equal to the ratio of the experimental mean gamma width and mean level spacing for s-wave neutrons. The gamma transmission coefficients are generated through calls to the strength function *fstrength*. The gamma-ray cross sections are also normalised. The following subroutines are called:

```

gammanorm
|--density >
|--fstrength
|--gammaws
  |--fstrength

```

### *fstrength*

In *fstrength*, the gamma-ray strength functions according to Kopecky-Uhl or Brink-Axel are calculated.

### *gammaws*

In *gammaws*, the photo-absorption cross sections are calculated. They consist of a GDR part and a quasi-deuteron part.

### *gammaout*

In *gammaout*, the gamma-ray strength functions, transmission coefficients and cross sections are written to output. The following subroutines are called:

```

gammaout
|--fstrength

```

## 7.4.2 preeqinit

General quantities needed for pre-equilibrium calculations are set, such as factorials, spin distribution functions and Pauli correction factors. The following subroutines are called:

```

preeqinit
|--bonetti
  |--optical >

```

### **bonetti**

In this subroutine, the average imaginary volume potential for the internal transition rates is calculated.

## 7.4.3 excitoninit

Quantities needed for exciton model calculations are set, such as preformation factors, factors for the emission rates and charge conserving Q-factors.

## 7.4.4 compoundinit

Quantities needed for compound nucleus model calculations are set, such as factors for width fluctuation and angular distribution calculations. The following subroutines are called:

```

compoundinit
|--gaulag
|--gauleg

```

**gaulag**

This subroutine is for Gauss-Laguerre integration.

**gauleg**

This subroutine is for Gauss-Legendre integration.

**7.4.5 reacinitial**

In *reacinitial*, all arrays that appear in the nuclear reaction model part of the program are initialized.

**7.4.6 incident**

Subroutine *incident* handles the calculation of total, reaction, elastic cross section, transmission coefficients and elastic angular distribution for the incident energy. Also, some main parameters for the current incident energy are set. The following subroutines are called:

```
incident
|--yesno
|--incidentecis
    |--optical    >
    |--ecisinput
|--incidentread
|--incidentnorm
    |--tripathi  >
|--incidentgamma
    |--fstrength
    |--gammaxs   >
|--spr
|--incidentout
```

**incidentecis**

In this subroutine the basic ECIS calculation for the incident particle and energy is performed for either a spherical or a deformed nucleus. The optical model parameters are determined by calling *optical*. The subroutine *ecisinput* is called for the creation of the ECIS input files. At the end of this subroutine, *ecis97t* is called to perform the actual ECIS calculation.

**incidentread**

In this subroutine the results from ECIS are read for the incident particle and energy. We first read the reaction (and for neutrons the total and elastic) cross section. Next, the transmission coefficients are read into the array *Tjline*, which has four indices: particle type, energy, spin and l-value. For spin-1/2 particles, we use the indices -1 and 1 for the two spin values. For spin-1 particles, we use -1, 0 and 1 and for spin-0 particles we use 0 only. For rotational nuclei, we transform the rotational transmission

coefficients into their spherical equivalents for the compound nucleus calculation. Also, transmission coefficients averaged over spin are put into separate arrays. The maximal  $l$ -value is determined to constrain loops over angular momentum later on in the code. The direct reaction Legendre coefficients and angular distribution are also read in. For coupled-channels calculations, we also read the discrete inelastic angular distributions and cross sections.

### **incidentnorm**

In *incidentnorm*, the transmission coefficients can be normalized with values obtained from semi-empirical systematics for the reaction cross section, if required.

### **incidentgamma**

Here, the transmission coefficients for the incident gamma channel, in the case of photo-nuclear reactions, are generated.

### **spr**

In *spr*, the S, P and R resonance parameters for low incident neutron energies are calculated and, if requested, written to file.

### **incidentout**

In this subroutine the basic cross sections, transmission coefficients and possible resonance parameters for the incident channel are written to output.

## **7.4.7 exgrid**

In *exgrid*, the possible routes to all reachable residual nuclei are followed, to determine the maximum possible excitation energy for each nucleus, given the incident energy. From this, the equidistant excitation energy grid for each residual nucleus is determined. The first  $NL$  values of the excitation energy grid  $E_x$  correspond to the discrete level excitation energies of the residual nucleus. The  $NL+1$ th value corresponds to the first continuum energy bin. The continuum part of the nuclides are then divided into equidistant energy bins. The  $Q$ -values for the residual nuclides are also determined. Finally, the calculation of level densities in TALYS can be done outside many loops of various quantum numbers performed in other subroutines. Therefore, in *exgrid* we store the level density as function of residual nucleus, excitation energy, spin and parity. The following subroutines are called:

```
exgrid
|--density >
|--spincut >
```

**7.4.8 recoilinit**

In this subroutine the basic recoil information is initialized. Various arrays are initialized and the maximum recoil energies for all residual nuclides are determined. Recoil energy and angular bins are determined.

**7.4.9 direct**

Subroutine *direct* takes care of the calculation of direct cross sections to discrete states that have not already been covered as coupled-channels for the incident channel, such as DWBA and giant resonance cross sections. The following subroutines are called:

```
direct
|--directecis
    |--ecisinput
|--directread
|--giant
|--directout
```

**directecis**

In this subroutine the basic DWBA calculation for a spherical nucleus is performed. The subroutine *ecisinput* is called for the creation of the ECIS input files. At the end of this subroutine, *ecis97t* is called to perform the actual ECIS calculation.

**directread**

In this subroutine the results from ECIS are read for the DWBA calculation. We first read the direct cross section for the collective discrete states. The direct reaction Legendre coefficients and angular distribution are also read in. The procedure is repeated for the giant resonance states.

**giant**

In *giant*, the DWBA cross sections for the continuum are smeared into spectra. The same is done for other collective states that are in the continuum.

**directout**

In this subroutine the direct cross sections for discrete states and giant resonances are written to output.

**7.4.10 preeq**

Subroutine *preeq* is the general module for pre-equilibrium reactions. Particle-hole numbers for the reaction under consideration are initialized. Depending on the chosen pre-equilibrium model, the following subroutines may be called:

```

preeq
|--surface
|--exciton
|--excitonout
|--exciton2
|--exciton2out
|--msd
|--msdplusmsc
|--preeqcomplex
|--preeqcorrect
|--preeqtotal
|--preeqang
|--preeqout

```

### **surface**

This function evaluates the effective well depth for pre-equilibrium surface effects.

### **exciton**

This is the main subroutine for the one-component exciton model. For each exciton number, we subsequently calculate the emission rates and the lifetime of the exciton state according to the never-come-back approximation. There is also a possibility to create J-dependent pre-equilibrium cross sections using the spin distribution. As an alternative (which is the default), the Hauser-Feshbach spin distribution is adopted. The following subroutines are called:

```

exciton
|--emissionrate
  |--ignatyuk
  |--preeqpair
  |--phdens
    |--finitewell
|--lifetime
  |--lambdaplus
    |--matrix
    |--ignatyuk
    |--preeqpair
    |--finitewell
    |--phdens      >

```

### *emissionrate*

This subroutine delivers the particle and photon emission rates (4.90), (4.94), (4.111) for the one-component exciton model.

### *preeqpair*

In this subroutine, the pre-equilibrium pairing correction according to Fu, see Eq. 4.60, is calculated.

*phdens*

The function *phdens* computes the one-component particle-hole state density (4.92).

*finitewell*

The function *finitewell* computes the finite well function (4.65).

*lifetime*

In this subroutine, the lifetime of the exciton state (4.95) is calculated, according to the never-come-back approximation.

*lambdaplus*

The function *lambdaplus* delivers the transition rates (4.98) in either analytical or numerical form, for the one-component exciton model based on matrix elements or on the optical model.

*matrix*

This function computes the matrix element (4.101) for the one-component model, and (4.81) for the two-component model.

**excitonout**

In *excitonout* all information of the one-component exciton model, such as matrix elements, emission rates and lifetimes, is written.

**exciton2**

This is the main subroutine for the two-component exciton model. For each exciton number, we subsequently calculate the emission rates and exchange terms (both in subroutine *exchange2*) and the lifetime of the exciton state. There is also a possibility to create J-dependent pre-equilibrium cross sections using the spin distribution. As an alternative (which is the default), the Hauser-Feshbach spin distribution is adopted. The following subroutines are called:

```
exciton2
|--exchange2
  |--emissionrate2
    |--ignatyuk
    |--preeqpair
    |--phdens2
      |--finitewell
  |--lambdapiplus
    |--matrix
    |--ignatyuk
    |--preeqpair
```

```

|--finitewell
|--phdens2    >
|--lambdanuplus
|--matrix
|--ignatyuk
|--preeqpair
|--finitewell
|--phdens2    >
|--lambdapinu
|--matrix
|--ignatyuk
|--preeqpair
|--finitewell
|--phdens2    >
|--lambdanupi
|--matrix
|--ignatyuk
|--preeqpair
|--finitewell
|--phdens2    >
|--lifetime2

```

### *exchange2*

In *exchange2*, the probabilities (4.70) for the strength of the exciton state are calculated.

### *phdens2*

The function *phdens2* computes the two-component particle-hole state density (4.59).

### *emissionrate2*

This subroutine delivers the particle and photon emission rates for the two-component exciton model.

### *lambdapiplus, lambdanuplus*

The function *lambdapiplus* delivers the proton transition rates (4.72) in either analytical or numerical form, for the two-component exciton model based on matrix elements or the optical model. Similarly for *lambdanuplus*.

### *lambdapinu, lambdanupi*

The function *lambdapinu* delivers the proton-neutron transition rates (4.72) in either analytical or numerical form, for the two-component exciton model based on matrix elements or the optical model. Similarly for *lambdanupi*.

*lifetime2*

In this subroutine, the lifetime of the exciton state through the quantity of Eq. (4.69) is calculated.

**exciton2out**

In *exciton2out* all information of the two-component exciton model, such as matrix elements, emission rates and lifetimes, is written.

**msd**

This subroutine calculates pre-equilibrium cross sections according to the macroscopic multi-step direct (MSD) model. The MSD model is implemented for neutrons and protons only. The following subroutines are called:

```
msd
|--msdinit
|  |--interangle
|--dwbaecis
|  |--ecisdwbamac
|    |--optical    >
|--dwbaread
|--dwbaout
|--dwbaint
|--onecontinuumA
|  |--ignatyuk
|  |--omega
|    |--phdens    >
|--onestepA
|  |--ignatyuk
|  |--omega      >
|  |--locate
|  |--pol2
|--msdcalc
|  |--onestepB
|    |--cmsd
|--onecontinuumB
|  |--cmsd
|--multistepA
|--multistepB
|  |--locate
|  |--pol2
|--msdtotal
|--msdout
```

*msdinit*

This subroutine initializes various arrays for the multi-step direct calculation, such as the MSD energy grid and the intermediate angles through a call to *interangle*.

*interangle*

Subroutine *interangle* produces the intermediate angles for MSD model, by the addition theorem. For multi-step reactions, this is necessary to transform the ingoing angle of the second step and link it with the outgoing angle of the first step.

*dwbaecis*

This subroutine takes care of all the ECIS calculations that need to be performed for the various steps of the multi-step reaction. Subsequently, DWBA calculations are performed for the first exchange one-step reaction, the inelastic one-step reaction and the second exchange one-step reaction. For this, various subroutines are called.

*dwbaecis*

Subroutine *ecisdwbamac* creates the ECIS input file for a macroscopic DWBA calculation. Potentials for the incident, transition and outgoing channel are calculated.

*dwbaread*

In this subroutine the results from ECIS are read. For every energy and spin we read the total DWBA cross section and the angle-differential DWBA cross section.

*dwbaread*

This subroutine takes care of the output of the DWBA cross sections.

*dwbaint*

In *dwbaint*, the DWBA cross sections are interpolated on the appropriate energy grid.

*onecontinuumA*

In *onecontinuumA*, the continuum one-step cross sections to be used in multi-step calculations are calculated by multiplying the DWBA cross sections by particle-hole state densities.

*omega*

This is a function of the particle-hole state density per angular momentum.

*onestepA*

In *onestepA*, the unnormalized one-step direct cross sections for the outgoing energy grid are calculated (these will be renormalized in subroutine *onestepB*).

*pol2*

Subroutine for interpolation of second order.

*msdcalc*

This is the general subroutine for the final MSD calculations.

*onestepB*

In *onestepB*, the one-step direct cross sections are calculated using a final normalization.

*onecontinuumB*

In *onecontinuumB*, the final one-step direct cross sections for use in the multi-step calculations are computed using the final normalization.

*multistepA*

In *multistepA*, the multi-step direct cross sections (second and higher steps) are calculated using a final normalization.

*multistepB*

In *multistepB*, the multi-step direct cross sections are interpolated on the final outgoing energy grid.

*msdtotal*

In *msdtotal*, the total multi-step direct cross sections are calculated.

*msdout*

In *msdout*, the multi-step direct cross sections are written to output.

**msdplumsc**

In this subroutine, the MSD cross sections are put in the general pre-equilibrium cross sections.

**preeqcomplex**

Subroutine *preeqcomplex* handles pre-equilibrium complex particle emission. The implemented complex particle emission model is described in Ref. [70], see also Section 4.4.4. Note that several purely empirical fixes to the model were needed to prevent divergence of certain cross section estimates. The subroutine consists of two main parts: One for stripping/pickup and one for alpha knock-out reactions. The following subroutines are called:

```
preeqcomplex
|--phdens2    >
```

**preeqcorrect**

This subroutine handles the correction of pre-equilibrium cross sections for direct discrete cross sections. If the cross sections for discrete states have *not* been calculated by a direct reaction model, we collapse the continuum pre-equilibrium cross sections in the high-energy region on the associated discrete states. After this, the pre-equilibrium cross sections in the discrete energy region are set to zero. The following subroutines are called:

```
preeqcorrect
|--locate
```

**preeqtotal**

In *preeqtotal*, the total pre-equilibrium cross sections are calculated. The pre-equilibrium spectra and spectra per exciton number are summed to total pre-equilibrium cross sections. Special care is taken for the continuum bin with the highest outgoing energy, i.e. the one that overlaps with the energy corresponding to the last discrete state. In line with unitarity, the summed direct + pre-equilibrium cross section may not exceed the reaction cross section. In these cases, we normalize the results. Also, the discrete pre-equilibrium contribution is added to the discrete state cross sections.

**preeqang**

In *preeqang*, the pre-equilibrium angular distribution is calculated. Also here, there is a correction of the pre-equilibrium cross sections for direct discrete angular distributions. If the angular distributions for discrete states have *not* been calculated by a direct reaction model, we collapse the continuum pre-equilibrium angular distributions in the high energy region on the associated discrete states. For the exciton model, the pre-equilibrium angular distributions are generated with the Kalbach systematics. The following subroutines are called:

```
preeqang
|--kalbach
```

*kalbach*

This is the function for the Kalbach systematics [72].

**preeqout**

In *preeqout*, the output of pre-equilibrium cross sections is handled. The following subroutines are called:

```
preeqout
|--ignatyuk
|--phdens      >
|--phdens2     >
```

### 7.4.11 population

In *population*, the pre-equilibrium spectra are processed into population bins. The pre-equilibrium cross sections have been calculated on the emission energy grid. They are interpolated on the excitation energy grids of the level populations (both for the total and the spin/parity-dependent cases) to enable further decay of the residual nuclides. also, the pre-equilibrium population cross section are normalized. Due to interpolation, the part of the continuum population that comes from pre-equilibrium is not exactly equal to the total pre-equilibrium cross section. The normalization is done over the whole excitation energy range. The following subroutines are called:

```
population
|--locate
|--poll
```

### 7.4.12 compnorm

There is a small difference between the reaction cross section as calculated by ECIS and the sum over transmission coefficients. We therefore normalize the level population accordingly in this subroutine. The compound nucleus formation cross section *xsflux* and the associated normalization factors are created.

### 7.4.13 comptarget

In *comptarget*, the compound reaction for the initial compound nucleus is calculated. First, the level densities and transmission coefficients are prepared before the nested loops over all quantum numbers are performed. Next the following nested loops are performed:

- compound nucleus parity
- total angular momentum  $J$  of compound nucleus
- $j$  of incident channel
- $l$  of incident channel
- outgoing particles and gammas
- outgoing excitation energies
- residual parity
- residual spin
- $j$  of outgoing channel
- $l$  of outgoing channel

There are two possible types of calculation for the initial compound nucleus. If either width fluctuation corrections or compound nucleus angular distributions are wanted, we need to sum explicitly over all possible quantum numbers before we calculate the width fluctuation or angular factor. If not, the sum over  $j$  and  $l$  of the transmission coefficients can be lumped into one factor, which decreases the calculation time. In the latter case, the partial decay widths `enumhf` are calculated in subroutine `comppprepare`.

In order to get do-loops running over integer values, certain quantum numbers are multiplied by 2, which can be seen from a 2 present in the corresponding variable names. For each loop, the begin and end point is determined from the triangular rule.

For every  $J$  and  $P$  (parity), first the denominator (total width) `denomhf` for the Hauser-Feshbach formula is constructed in subroutine `comppprepare`. Also width fluctuation variables that only depend on  $J$  and  $P$  and not on the other angular momentum quantum numbers are calculated in subroutine `widthprepare`. For the width fluctuation calculation, all transmission coefficients need to be placed in one sequential array. Therefore, a counter `tnum` needs to be followed to keep track of the proper index for the transmission coefficients.

Inside the nested loops listed above, compound nucleus calculations for photons, particles and fission are performed. In the middle of all loops, we determine the index for the width fluctuation calculation and call the subroutine that calculates the correction factor. Also, compound angular distributions, i.e. the Legendre coefficients, for discrete states are calculated.

The following subroutines are called:

```
comptarget
|--densprepare
|--tfission
|--comppprepare
|--widthprepare
|--widthfluc
|--clebsch
|--racah
|--tfissionout
|--raynalcomp
```

### **densprepare**

In `densprepare`, we prepare the energy grid, level density and transmission coefficient information for the compound nucleus and its residual nuclides. For various types of decay (continuum to discrete, continuum to continuum, etc.) we determine the energetically allowed transitions. These are then taken into account for the determination of integrated level densities. To get the transmission coefficients on the excitation energy grid from those on the emission energy grid, we use interpolation of the second order. Finally, the fission level densities are calculated.

The following subroutines are called:

```
densprepare
|--fstrength
|--locate
|--pol2
|--density    >
```

**tfission**

In this subroutine, the fission transmission coefficients are calculated. The fission transmission coefficients decrease very rapidly with excitation energy. Therefore, we calculate them at the end points and at the middle of each excitation energy bin. With this information, we can do logarithmic integration. Calls to subroutine *t1barrier* are done for 1, 2 and 3 barriers. Also transmission coefficients corrected for the presence of class II states are calculated.

The following subroutines are called:

```
tfission
|--t1barrier
  |--thill
```

**t1barrier**

Subroutine *t1barrier* handles the fission transmission coefficient for one barrier. Both discrete states and the continuum are taken into account.

**thill**

Function for the Hill-Wheeler formula.

**compprepare**

In *compprepare*, information for the initial compound nucleus is prepared. The transmission coefficients are put in arrays for possible width fluctuation calculations. Also the total width denomhf appearing in the denominator of the compound nucleus formula is created. Note that the complete subroutine is performed inside the loop over compound nucleus spin  $J$  and parity  $P$  in subroutine *comptarget*.

**widthprepare**

In this subroutine, the preparation of width fluctuation calculations is done. All width fluctuation variables that only depend on  $J$  and  $P$  and not on the other angular momentum quantum numbers are calculated. The following subroutines are called:

```
widthprepare
|--molprepare
|--hrtwprepare
|--goeprepare
  |--prodm
  |--prodp
```

**molprepare**

This subroutine takes care of the preparation of the Moldauer width fluctuation correction (information only dependent on  $J$  and  $P$ ).

**hrtwprepare**

This subroutine takes care of the preparation of the HRTW width fluctuation correction (information only dependent on  $J$  and  $P$ ).

**goeprepare**

This subroutine takes care of the preparation of the GOE triple integral width fluctuation correction (information only dependent on  $J$  and  $P$ ).

**prodm, prodp**

Functions to calculate a product for the GOE calculation.

**widthfluc**

General subroutine for width fluctuation corrections. The following subroutines are called:

```
widthfluc
|--moldauer
|--hrtw
|--goe
  |--func1
```

**moldauer**

Subroutine for the Moldauer width fluctuation correction.

**hrtw**

Subroutine for the HRTW width fluctuation correction.

**goe**

Subroutine for the GOE width fluctuation correction.

**clebsch**

Function for the calculation of Clebsch-Gordan coefficients.

**racah**

Function for the calculation of Racah coefficients.

**tfissionout**

Subroutine *tfissionout* takes care of the output of fission transmission coefficients.

**raynalcomp**

Using subroutine *raynalcomp*, a compound nucleus run by ECIS can be performed, in addition to the calculation by TALYS. The results as calculated by ECIS will however not be used for TALYS but are just for comparison. The following subroutines are called:

```
raynalcomp
|--eciscompound
  |--optical    >
```

**eciscompound**

In *eciscompound*, an ECIS input file for a compound nucleus calculation is prepared.

**7.4.14 binary**

In *binary*, the binary reaction cross section are accumulated. The direct and pre-equilibrium cross sections are processed into population arrays. Binary feeding channels, necessary for exclusive cross sections, are determined. Also the population after binary emission is printed. The following subroutines are called:

```
binary
|--ignatyuk
|--spindis    >
|--binaryspectra
  |--binemission
    |--locate
    |--poll
|--binaryrecoil
```

**binaryspectra**

Subroutine to interpolate decay, from one bin to another, on the emission spectrum. The binary and compound emission spectra are constructed.

**binemission**

In *binemission*, the decay from the primary compound nucleus to residual nuclei is converted from the excitation energy grid to emission energies. Due to interpolation errors, there is always a small difference between the binary continuum cross section and the integral of the spectrum over the continuum. The spectrum is accordingly normalized. The interpolation is performed for both inclusive and exclusive channels.

**binaryrecoil**

Subroutine *binaryrecoil* calculates the recoil and ejectile spectra in the LAB frame from the ejectile spectra calculated in the CM frame. The following subroutines are called:

```

binaryrecoil
|--cm2lab
|--labsurface
  |--belongs
  |--binsurface
    |--intri
      |--sideline
        |--intersection
          |--belongs
            |--invect
              |--belongs

```

### **cm2lab**

Subroutine *cm2lab* performs the classical kinematical transformation from the center of mass frame to the LAB frame. For massive ejectiles the CM emission energy is converted into a CM emission velocity and is then vectorially coupled with the CM velocity to deduce the LAB velocity. No coupling is performed for photons. The same subroutine is used to calculate the recoil velocities.

### **labsurface**

Subroutine *labsurface* is used to calculate the way the area of a triangle defined by three points is distributed in a given bidimensional grid.

### **belongs**

This function tests if a real number is inside or outside a given bin.

### **binsurface**

This subroutine returns the area of a given bidimensional bin covered by a triangle.

### **intri**

This function tests if a point is inside or outside a triangle.

### **sideline**

This function tells if a point is on one side or on the other side of a given line.

### **intersection**

Subroutine *intersection* determines the intersection points of a straight line with a given bidimensional bin.

### **invect**

This function tests if a point is within a segment or not.

**7.4.15 angdis**

In *angdis*, angular distributions for discrete states are calculated. This is done through Legendre polynomials for direct, compound and the total contribution per discrete state. The following subroutines are called:

```
angdis
|--plegendre
|--angdisrecoil
```

**angdisrecoil**

Subroutine *angdisrecoil* calculates the recoil and ejectile spectra in the LAB frame from the ejectile spectra calculated in the CM frame. The following subroutines are called:

```
angdisrecoil
|--cm2lab
|--labsurface >
```

**7.4.16 multiple**

This is the subroutine for multiple emission. We loop over all residual nuclei, starting with the initial compound nucleus ( $Z_{\text{comp}}=0$ ,  $N_{\text{comp}}=0$ ), and then according to decreasing  $Z$  and  $N$ . For each encountered residual nuclide in the chain, we determine its nuclear structure properties. In total, the following nested loops are performed for multiple Hauser-Feshbach decay:

- compound nuclides  $Z_{\text{comp}}, N_{\text{comp}}$
- mother excitation energy bins
- compound nucleus parity
- total angular momentum  $J$  of compound nucleus
- (in *compound*) outgoing particles and gammas
- (in *compound*) outgoing excitation energies
- (in *compound*) residual parity
- (in *compound*) residual spin
- (in *compound*)  $j$  of outgoing channel
- (in *compound*)  $l$  of outgoing channel

Before the *compound subroutine* is entered there is a call to the multiple pre-equilibrium subroutine *multipreeq(2)* to deplete the flux if enough fast-particle flux is present. The following subroutines are called:

```

multiple
|--structure >
|--exgrid >
|--basicxs >
|--levelsout
|--densityout >
|--fissionparout
|--cascade
|--densprepare >
|--multipreeq2
|--multipreeq
|--tfission >
|--compound
|--tfissionout
|--compemission
|--kalbach

```

### **cascade**

Subroutine for the gamma-ray cascade. The discrete gamma line intensities are stored.

### **multipreeq2**

Subroutine for the two-component multiple preequilibrium model. A loops over all possible particle-hole excitations of the mother bin is performed. From each configuration, a new exciton model calculation is launched (**mpreeqmode 1**) or a simple transmission coefficient method is used (**mpreeqmode 2**). The particle-hole configurations of all residual nuclides are populated with the emitted pre-equilibrium flux. The depletion factor to be used for multiple compound emission is determined. The following subroutines are called:

```

multipreeq2
|--ignatyuk
|--phdens2 >
|--exchange2
|--lifetime2
|--locate

```

### **multipreeq**

Subroutine for the one-component multiple preequilibrium model. A loops over all possible particle-hole excitations of the mother bin is performed. From each configuration, a new exciton model calculation is launched (**mpreeqmode 1**) or a simple transmission coefficient method is used (**mpreeqmode 2**). The particle-hole configurations of all residual nuclides are populated with the emitted pre-equilibrium flux. The depletion factor to be used for multiple compound emission is determined. The following subroutines are called:

```

multipreeq

```

```

|--ignatyuk
|--phdens      >
|--emissionrate >
|--lifetime >
|--locate

```

### compound

Subroutine with the Hauser-Feshbach model for multiple emission. the nested loops are the same as those described for *comptarget*, with the exception of  $j$  and  $l$  of the incident channel, since we start from an excitation energy bin with a  $J, P$  value. In order to get do-loops running over integer values, certain quantum numbers are multiplied by 2, which can be seen from a 2 present in the corresponding variable names. For each loop, the begin and end point is determined from the triangular rule.

For every  $J$  and  $P$  (parity), first the denominator (total width) *denomhf* for the Hauser-Feshbach formula is constructed. Inside the nested loops, compound nucleus calculations for photons, particles and fission are performed.

### compemission

In *compemission*, the compound nucleus emission spectra are determined from the multiple Hauser-Feshbach decay scheme. The decay from compound to residual nuclei is converted from the excitation energy grid to emission energies. The spectrum is obtained by spreading the decay over the mother bin and, in the case of continuum-continuum transitions, the residual bin. For each mother excitation energy bin, we determine the highest possible excitation energy bin for the residual nuclei. As reference, we take the top of the mother bin. The maximal residual excitation energy is obtained by subtracting the separation energy from this. Various types of decay are possible:

- Decay from continuum to continuum. For most residual continuum bins, no special care needs to be taken and the emission energy that characterizes the transition is simply the average between the highest energetic transition that is possible and the lowest.
- Decay from continuum to discrete. The lowest possible mother excitation bin can not entirely decay to the discrete state. For the residual discrete state, it is checked whether the mother excitation bin is such a boundary case. This is done by adding the particle separation energy to the excitation energy of the residual discrete state.

When the decay type has been identified, the decay from the population is distributed over the emission energy bins. All possible end point problems are taken into account. The following subroutines are called:

```

compemission
|--locate
|--comprecoil

```

**comprecoil**

If **recoil y**, the recoil and/or light particle spectra in the LAB frame are calculated in *comprecoil*. The following subroutines are called:

```
comprecoil
|--kalbach
|--cm2lab
|--labsurface >
```

**7.4.17 channels**

In *channels*, the exclusive reaction cross sections and spectra as outlined in Section 3.2.2 are calculated. A loop over all residual nuclides is performed and it is determined whether the residual nucleus under consideration can be reached by a certain particle combination. The associated gamma-ray production and isomeric exclusive cross sections are also computed. Finally, numerical checks with the total cross sections are performed. The following subroutines are called:

```
channels
|--specemission
  |--locate
```

**specemission**

In *specemission*, the exclusive emission spectra are computed. The procedure is analogous to that of *compemission*.

**7.4.18 totalxs**

In this subroutine, a few total cross sections are cumulated, such as the continuum exclusive cross section, the total particle production cross section and the total fission cross section.

**7.4.19 spectra**

In *spectra*, smoothed discrete cross sections are added to the emission spectra. A more precise energy grid at the high-energy tail is created to account for the structure of discrete states. This is done for both angle-integrated and double-differential spectra. The following subroutines are called:

```
spectra
|--locate
```

**7.4.20 massdis**

In *massdis* the fission fragment and product yields are calculated. A loop over all fissioning systems is performed. Some of the excitation energy bins are lumped into larger energy bins to save computation time. The fission yields per fissioning system are weighted with the fission cross section and added to form the total yield. The following subroutines are called:

```

massdis
|--brosafy
  |--spline
  |--ignatyuk
  |--trans
    |--funcfismode
      |--ignatyuk
      |--splint
      |--density    >
    |--trapzd
      |--funcfismode
  |--splint
  |--neck
    |--bdef
      |--fcoul
      |--fsurf
    |--ignatyuk
    |--fmin
    |--rpoint
      |--vr2
    |--vr1
    |--vr2
    |--vr3
    |--rtbis
    |--evap
      |--bdef
    |--sform
    |--rhodi
    |--fi
      |--vr1
      |--vr2
      |--vr3

```

**brosafy**

In this subroutine the fission fragment and product mass yields are determined per fissioning system. The relative contribution of each fission mode is calculated. Subsequently, the fission yields per fission mode are calculated and summed with the fission mode weight.

**spline**

This subroutine performs a spline fit to the fission mode barrier parameters and the deformation parameters used in the subroutine *neck*.

**trans**

This subroutine calculates the fission transmission coefficient per fission mode to determine the relative contribution of each fission mode.

**funcfismode**

This function corresponds to the expression of the fission transmission coefficient.

**splint**

This subroutine uses the spline fit obtained in the subroutine *spline* to interpolate.

**neck**

In this subroutine the actual fission fragment and product mass yield per fission mode is computed based on the Random-neck Rupture model.

**bdef**

This subroutine computes the binding energy of a deformed nucleus with an eccentricity by the droplet model without shell corrections.

**fcoul**

This function contains the form factor for the Coulomb self energy.

**fsurf**

This function contains the form factor for the surface energy.

**fmin**

This subroutine searches the minimal value of a function.

**rpoint**

This subroutine is used to calculate the rupture point  $z_{riss}$  for a given nucleon number hidden in the left-hand side of the dinuclear complex.

**vr1**

This function gives the volume of the projectile-like section.

**vr2**

This function gives the volume of the neck.

**vr3**

This function gives the volume of the target-like section.

**evap**

This function is used to determine the number of evaporated neutrons for a given fission fragment.

**sform**

This function determines the form factor for the coulomb interaction energy between two spheroids.

**rhodi**

This function computes the shape of the dinuclear system.

**fi**

This function determines the exact shape of the dinuclear complex.

**7.4.21 residual**

In *residual*, the residual production cross sections, both total and isomeric, are stored in arrays.

**7.4.22 totalrecoil**

In this subroutine, the total recoil results are assembled.

**7.4.23 thermal**

In *thermal*, the cross sections down to thermal energies are estimated. For non-threshold channels, the cross sections are extrapolated down to 1.e-5 eV. Capture values at thermal energies are used. For energies up to 1 eV, the 1/sqrt(E) law is used. Between 1 eV and the first energy at which TALYS performs the statistical model calculation, we use logarithmic interpolation. The following subroutines are called:

```
thermal
|--poll
```

**7.4.24 output**

Subroutine *output* handles the output of all cross sections, spectra, angular distributions, etc. per incident energy. The following subroutines are called:

```
output
|--totalout
|--binaryout
|--productionout
|--residualout
|--fissionout
|--discreteout
|--channelsout
```

```
|--spectraout  
|--recoilout  
|--angleout  
|--ddxout  
  |--locate  
|--gamdisout
```

**totalout**

Subroutine for the output of total cross sections, such as total, non-elastic, pre-equilibrium, direct, etc.

**binaryout**

Subroutine for the output of the binary cross sections.

**productionout**

Subroutine for the output of particle production cross sections and total fission cross section.

**residualout**

Subroutine for the output of residual production cross sections.

**fissionout**

Subroutine for the output of fission cross sections per fissioning nuclide.

**discreteout**

Subroutine for the output of cross sections for discrete states for inelastic and other non-elastic channels.

**channelsout**

Subroutine for the output of exclusive channel cross sections and spectra, including ground state and isomer production and fission.

**spectraout**

Subroutine for the output of angle-integrated particle spectra.

**recoilout**

Subroutine for the output of recoil information.

**angleout**

Subroutine for the output of angular distributions for elastic scattering, inelastic scattering to discrete states and non-elastic scattering to other discrete states.

**ddxout**

Subroutine for the output of double-differential cross sections.

**gamdisout**

Subroutine for the output of discrete gamma-ray production.

**7.4.25 finalout**

In *finalout*, all results are printed as a function of incident energy, i.e. all excitation functions. This information appears in the main output file and/or in separate output files per reaction channel. Also, general nuclear model parameters are written to the parameter file.

**7.4.26 endf**

Subroutine for the output of cross sections and information for the production of an ENDF-6 file. The following subroutines are called:

```
endf
|--endfinfo
|--endfenergies
|--endfecis
  |--optical >
  |--ecisinput >
|--endfread
  |--tripathi >
```

**endfinfo**

Subroutine for writing the general information (i.e. the main reaction parameters) needed to create an ENDF-6 file.

**endfenergies**

Subroutine to create the energy grid for cross sections for an ENDF-6 file. This grid ensures that the total, elastic and reaction cross section are calculated on a sufficiently precise energy grid. Thresholds for all partial cross sections are also added to this grid.

**endfecis**

In this subroutine the loop over the energy grid created in *endfenergies* is done to perform basic ECIS calculations. The optical model parameters are determined by calling *optical*. The subroutine *ecisinput* is called for the creation of the ECIS input files. At the end of this subroutine, *ecis97t* is called to perform the actual ECIS calculation.

**endfread**

In this subroutine the results from ECIS are read. For every incident energy we read the reaction (and for neutrons the total and elastic) cross sections. These are then written to a separate file for ENDF-6 formatting.

**7.4.27 timer**

Subroutine for the output of the execution time and a congratulation for the successful calculation.

**7.5 Programming techniques**

In general, we aim to apply a fixed set of programming rules consistently throughout the whole code. Here are some of the rules we apply to enforce readability and robustness:

- We use suggestive variable names as much as possible.
- Every variable in a subroutine, apart from dummy variables appearing in e.g. a do loop, is explained once in the comment section. In addition, we aim to give as much explanation as possible for the used algorithms.
- We use **implicit none** as the first line of *talys.cmb* and all stand-alone subroutines and functions. This means that every variable must be declared, which is a powerful recipe against typing errors.
- We program directly “from the physics”, as much as possible, i.e. we use array indices which correspond one-to-one to the indices of the physical formulae from articles and books.
- Cosmetical features:
  - Different tasks within a subroutine are clearly separated. A block, which contains one sub-task, is separated by asterisks, e.g.
 

```
c
c ***** Constants *****
c
```

The last asterisk is always in column 72. In the first block, the labels are numbered 10, 20, 30, etc. In the second block, the labels are numbered 110, 120, 130, etc.
  - We indent two blanks in do loops and if statements.
- In the file *talys.cmb*, we systematically store variables of type logical, character, integer, real and double precision in separate common blocks. The order of appearance of variables in *talys.cmb* follows that of the subroutines.
- Every subroutine has the same heading structure: We give the author, date and task of the subroutine. Next, the file *talys.cmb* is included, followed by the inclusion of declarations for possible local variables.

- We use nuclear model parameterisations that are as general as possible within the programmed nuclear reaction mechanisms, to enable easy implementation of future refinements. For example, level densities will never be hardwired “on the spot”, but will be called by a function *density*. An improvement, or alternative choice, of a level density model will then have a consistent impact throughout the whole code.

As a general rule, although we aim to program as clever as possible, we always prefer readability over speed and memory economy. Some nuclear physicists are more expensive than computers, or at least should be.

## 7.6 Changing the array dimensions

As explained in the previous sections, almost all arrays are defined in the common block file *talys.cmb*. At the top of *talys.cmb*, the parameters are set for the dimensions of the various arrays. Their names all start with **num**. Most of these parameters should be left untouched, because they determine basic quantities of a nuclear model calculation. Some of them can however be changed. They can be reduced, for the case that the working memory of your computer is too small, or be increased, in cases where you want to perform more extensive or precise calculations than we thought were necessary. However, in normal cases you only need to change the keyword values in the input file and not the parameters in *talys.cmb*. In the standard version of TALYS, the latter already have reasonable values. Nevertheless, the following parameters can be changed and will have a significant effect:

- **memorypar**: general multiplication factor for dimensions of several arrays. Use a small value for a small computer. Normally, changing this parameter does not require any further changes of the parameters that follow below.
- **numbins**: the maximum number of continuum excitation energy bins in the decay chains. Obviously, this could be increased to allow for more precision.
- **numchannel** and **numchantot**: the depth to which exclusive reaction channels are followed can be set by these parameters. However, as mentioned in Section 3.2.2, exclusive channels that go beyond a value of **numchannel=4** (**numchantot=210**) are rarely of interest. Also, since the exclusive reaction calculation involves some large arrays, one may easily run into memory problems by choosing too large values. If one works on e.g. a 64 Mb machine it may be helpful, or even necessary, to choose smaller values if one is not interested in exclusive calculations at all. Table 7.1 displays the values that are theoretically possible. In this table, we use

$$\mathbf{numchantot} = \sum_{m=0}^{\mathbf{numchannel}} \binom{m+5}{m} \quad (7.1)$$

which is the total number of channels for 6 different outgoing particles (neutrons up to alpha particles). In practice, less are needed since many channels never open up.

- **numZ** and **numN**: The maximum number of proton and neutron units, respectively, away from the initial compound nucleus that can be reached after multiple emission. If you want to try your luck with TALYS at very high incident energies, these parameters may need to be increased.

- **numlev**: The maximum number of included discrete levels.
- **numang**: The maximum number of outgoing angles for discrete states.
- **numangcont**: The maximum number of outgoing angles for the continuum.

Obviously, after increasing these values you still need to set the associated keywords in the input file to use the increased limits, although some of them, e.g. **maxZ**, are always by default set to their maximum value. You could increase a parameter and simultaneously reduce another one that is of no relevance to the particular problem under study, to remain within the available memory of your computer. Of course, you should always completely re-compile TALYS after changing anything in *talys.cmb*.

Table 7.1: Number of exclusive channels for outgoing particles of 6 different types

numchannel	number of channels	numchantot
0	1	1
1	6	7
2	21	28
3	56	84
4	126	210
5	252	462
6	462	924
7	792	1716
8	1287	3003
9	2002	5005
10	3003	8008

## Chapter 8

# Verification and validation, sample cases and output

TALYS has been tested both formally ("computational robustness") and by comparison of calculational results with experimental data. This will be described in the present Chapter. Also a description of the output will be given.

### 8.1 Robustness test with DRIP

One way to test a nuclear model code is to let it calculate results for a huge number of nuclides, and the whole range of projectiles and energies. We have written a little code DRIP, not included in the release, that launches TALYS for complete calculations for all nuclides, from dripline to dripline. Besides checking whether the code crashes, visual inspection of many curves simultaneously, e.g. 50 (n,2n) excitation functions, may reveal non-smooth behaviour. Various problems, not only in the TALYS source code itself, but also in the nuclear structure database, were revealed with this approach in the initial development stages.

### 8.2 Robustness test with MONKEY

Chapter 6 contains a description of the more than 150 keywords that can be used in a problem for TALYS. Some of them are flags which can only be set to **y** or **n**. Other keywords can be set to a few or several integer values and there are also keywords whose values may cover a quasi-continuous range between the minimum and maximum possible value that we allow for them. Strictly speaking, the total number of possible input files for TALYS is huge (though theoretically finite, because of the finite precision of a computer), and obviously only a small subset of them corresponds to physically meaningful cases. Indeed, as with any computer code it is not too difficult to bring a TALYS calculation to a formally successful end, i.e. without crashing, with an input file that represents a completely unphysical case. Obviously, there is no way to prevent this - the user is supposed to have full responsibility for what she or he is doing - and we can never anticipate what input files are made by other users. Nevertheless, to test the robustness of our code, we wrote a little program called MONKEY which remotely simulates TALYS in

the hands of an evil user: It creates an input file for TALYS, using all the keywords, with *random* values, and starts a run with it. Each keyword in this input file has a value that remains within the allowed (and very broad) range as specified in Chapter 6. If TALYS is compiled with all checking options (i.e. array out-of-bounds problems, divisions by zero, other over/underflow errors, etc.) enabled and completes say, 1000 cases without crashing, we can at least say we have tested *computational* robustness to some extent, and that we *may* have probed every corner of the code. We realize that this is not a full-proof method to test TALYS formally on the Fortran level (if there exists such a test!), but MONKEY has helped us to discover a few bugs during development which otherwise would have come to the surface sooner or later. We think it is better that *we* find them first. The ideal result of this procedure would be that TALYS never crashes or stops without giving an appropriate error message. We emphasize that this test alone does obviously not guarantee any physical quality of the results. For that, much more important are the input files that *are* physically meaningful. These are discussed in the next Section.

### 8.3 Validation with sample cases

With this manual, we hope to convince you that a large variety of nuclear reaction calculations can be handled with TALYS. To strengthen this statement, we will discuss many different sample cases. In each case, the TALYS input file, the relevant output and, if available, a graphical comparison with experimental data will be given. The description of the first sample case is the longest, since the output of TALYS will be discussed in complete detail. Obviously, that output description is also applicable to the other sample cases. The entire collection of sample cases serves as (a) verification of TALYS: the sample output files should coincide, apart from numerical differences of insignificant order, with the output files obtained on your computer, and (b) validation of TALYS: the results should be comparable to experimental data for a widely varying set of nuclear reactions. Table 8.1 tells you what to expect in terms of computer time, and this shows that it thus may take a while (about one and a half hour on our PC) before all sample cases have finished. Running the *verify* script will be worth the wait, since a successful execution of all sample cases will put you on safer ground for your own calculations. In general, we will explain the keywords again as they appear in the input files below. If not, consult Table 6.1, which will tell you where to find the explanation of a keyword.

#### 8.3.1 Sample 1: All results for 14 MeV n + $^{93}\text{Nb}$

We have included 9 different versions of this sample case, in order to give an impression of the various types of information that can be retrieved from TALYS. Most, but not all, output options will be described, while the remaining will appear in the other sample cases. We have chopped the sample output after column 80 to let it fit within this manual. We suggest to consult the output files in the *samples/* directory for the full results.

##### Case 1a: The simplest input file

The first sample problem concerns the simplest possible TALYS calculation. Consider the following input file that produces the results for a 14 MeV neutron on  $^{93}\text{Nb}$ :

#

Sample case	Time
1a	0 m 4.60 sec
1b	0 m 4.80 sec
1c	0 m 18.37 sec
1d	0 m 4.61 sec
1e	0 m 4.74 sec
1f	0 m 6.64 sec
1g	0 m 4.66 sec
1h	0 m 6.86 sec
1i	0 m 4.00 sec
2	3 m 54.35 sec
3a	0 m 1.37 sec
3b	0 m 1.34 sec
3c	0 m 1.35 sec
3d	18 m 46.17 sec
4a	0 m 58.85 sec
4b	0 m 40.92 sec
5	12 m 14.91 sec
6a	1 m 28.35 sec
6b	1 m 28.37 sec
7	1 m 34.65 sec
8	23 m 1.17 sec
9	0 m 8.05 sec
10a	1 m 12.31 sec
10b	1 m 54.19 sec
11	2 m 17.67 sec
12	0 m 20.27 sec
13	4 m 55.04 sec
14	33 m 49.54 sec
15	0 m 50.47 sec

Table 8.1: Computation time for the sample cases, run on a 2GHz Pentium processor, and TALYS compiled with the Lahey/Fujitsu f95 compiler under Linux Red Hat-9.

```
# General
#
projectile n
element nb
mass 93
energy 14.
```

where the purpose of the lines starting with a “#” is purely cosmetic. This input file called *input* can simply be run as follows:

**talys < input > output**

An output file of TALYS consists of several blocks. Whether these blocks are printed or not depends on the status of the various keywords that were discussed in Chapter 6. By default, the so-called main output is always given (through the default **outmain y**), and we discuss this output in the present sample case. For a single incident energy, a default calculation gives the most important cross sections only. “Most important” is obviously subjective, and probably every user has an own opinion on what should always appear by default in the output. We will demonstrate in the other sample problems how to extract all information from TALYS. The output file starts with a display of the version of TALYS you are using, the name of the authors, and the Copyright statement. Also the physics dimensions used in the output are given:

```
TALYS-0.64 (Version: December 5, 2004)
```

```
Copyright (C) 2004  A.J. Koning, S. Hilaire and M.C. Duijvestijn
                   NRG           CEA           NRG
```

```
Dimensions - Cross sections: mb, Energies: MeV, Angles: degrees
```

The next output block begins with:

```
##### USER INPUT #####
```

Here, the first section of the output is a print of the keywords/input parameters. This is done in two steps: First, in the block

```
USER INPUT FILE
```

```
#
# General
#
projectile n
element nb
mass 93
energy 14.
```

an exact copy of the input file as given by the user is returned. Next, in the block

## USER INPUT FILE + DEFAULTS

Keyword	Value	Variable	Explanation
#			
# Four main keywords			
#			
projectile	n	ptype0	type of incident particle
element	Nb	Starget	symbol of target nucleus
mass	93	mass	mass number of target nucleus
energy	14.000	eninc	incident energy in MeV
#			
# Basic physical and numerical parameters			
#			
ejectiles	g n p d t h a	outtype	outgoing particles
.....			

a table with all keywords is given, not only the ones that you have specified in the input file, but also all the defaults that are set automatically. The corresponding Fortran variables are also printed, together with a short explanation of their meaning. This table can be helpful as a guide to change further input parameters for a next run. You may also copy and paste the block directly into your next input file.

In the next output block

## ##### BASIC REACTION PARAMETERS #####

Projectile	: neutron	Mass in a.m.u.	: 1.008665
Target	: 93Nb	Mass in a.m.u.	: 92.906377

## Included channels:

gamma  
neutron  
proton  
deuteron  
triton  
helium-3  
alpha

## 1 incident energy (LAB):

14.000

## Q-values for binary reactions:

Q(n,g): 7.22747  
Q(n,n): 0.00000  
Q(n,p): 0.69099  
Q(n,d): -3.81858  
Q(n,t): -6.19608

Q(n,h): -7.72232

Q(n,a): 4.92553

we print the main parameters that characterize the nuclear reaction: the projectile, target and their masses and the outgoing particles that are included as competitive channels. The incident energy or range of incident energies in the LAB system is given together with the binary reaction Q-values.

The block with final results starts with

```
##### RESULTS FOR E= 14.00000 #####
```

Energy dependent input flags

```
Width fluctuations (flagwidth)      : n
Preequilibrium (flagpreeq)         : y
Multiple preequilibrium (flagmulpre): n
```

with no further information for the present sample case since no further output was requested. When all nuclear model calculations are done, the most important cross sections are summarized in the main part of the output, in which we have printed the center-of-mass energy, the main (total) cross sections, the inclusive binary cross sections  $\sigma_{n,k}^{inc,bin}$ , see Eq. (3.19), the total particle production cross sections  $\sigma_{n,xn}$  of Eq. (3.20) and the multiplicities  $Y_n$  of Eq. (3.22), and the residual production cross sections. The latter are given first per produced nuclide and isomer. Next, nuclides with the same mass are summed to give mass yield curves. Also, the sum over all the residual cross sections is compared with the non-elastic cross section. Obviously, these two values should be approximately equal.

```
##### REACTION SUMMARY FOR E= 14.000 #####
```

Center-of-mass energy: 13.849

#### 1. Total (binary) cross sections

```
Total          = 3.98190E+03
Shape elastic   = 2.21130E+03
Reaction        = 1.77060E+03
  Compound elastic= 1.05478E-03
  Non-elastic     = 1.77060E+03
    Direct        = 4.53222E+01
    Pre-equilibrium = 4.24545E+02
    Giant resonance = 6.33243E+01
    Compound non-el = 1.23741E+03
  Total elastic   = 2.21130E+03
```

#### 2. Binary non-elastic cross sections (non-exclusive)

```
gamma    = 2.97252E+00
neutron  = 1.66248E+03
proton   = 5.67462E+01
deuteron = 1.56242E+01
```

triton = 1.69988E+00  
helium-3= 1.18587E-08  
alpha = 3.10767E+01

## 3. Total particle production cross sections

gamma = 2.05606E+03      Multiplicity= 1.16122E+00  
neutron = 3.02632E+03      Multiplicity= 1.70921E+00  
proton = 5.99929E+01      Multiplicity= 3.38828E-02  
deuteron= 1.56242E+01      Multiplicity= 8.82426E-03  
triton = 1.69988E+00      Multiplicity= 9.60061E-04  
helium-3= 1.18587E-08      Multiplicity= 6.69756E-12  
alpha = 3.21314E+01      Multiplicity= 1.81472E-02

## 4. Residual production cross sections

## a. Per isotope

Z	A	nuclide	total cross section	level	isomeric cross section	isomeric ratio	lifetime
41	94	( 94Nb)	1.32555E+00	0	6.47368E-01	0.48838	
				1	6.78179E-01	0.51162	3.76000E+02 sec.
41	93	( 93Nb)	3.17521E+02	0	2.70943E+02	0.85331	
				1	4.65780E+01	0.14669	5.09000E+08 sec.
40	93	( 93Zr)	4.26957E+01	0	4.26957E+01	1.00000	
41	92	( 92Nb)	1.34230E+03	0	8.36701E+02	0.62333	
				1	5.05602E+02	0.37667	8.77000E+05 sec.
40	92	( 92Zr)	3.29213E+01	0	3.29213E+01	1.00000	
40	91	( 91Zr)	1.69988E+00	0	1.69988E+00	1.00000	
39	90	( 90Y )	2.52339E+01	0	1.55004E+01	0.61427	
				2	9.73356E+00	0.38573	1.15000E+04 sec.
39	89	( 89Y )	6.89745E+00	0	2.73554E+00	0.39660	
				1	4.16191E+00	0.60340	1.61000E+01 sec.

## b. Per mass

## A cross section

94 1.32555E+00  
93 3.60217E+02  
92 1.37523E+03  
91 1.69988E+00  
90 2.52339E+01  
89 6.89745E+00

Total residual production cross section: 1770.59851  
Non-elastic cross section : 1770.59888

At the end of the output, the total calculation time is printed, followed by a message that the calculation has been successfully completed:

```
Execution time:  0 hours  0 minutes  4.60 seconds
```

The TALYS team congratulates you with this successful calculation.

### Case 1b: Discrete state cross sections and spectra

As a first extension to the simple input/output file given above, we will request the output of cross sections per individual discrete level of the residual nuclides. Also, the cumulated angle-integrated and double-differential particle spectra are requested. This is obtained with the following input file:

```
#
# General
#
projectile n
element nb
mass 93
energy 14.
#
# Output
#
outdiscrete y
outspectra y
ddxmode 2
filespectrum n p a
fileddxa n 30.
fileddxa n 60.
fileddxa a 30.
fileddxa a 60.
```

In addition to the information printed for case 1a, the cross sections per discrete state for each binary channel are given, starting with the  $(n, \gamma)$  channel,

#### 5. Binary reactions to discrete levels and continuum

(n,g) cross sections:

Inclusive:

Level	Energy	E-out	J/P	Direct	Compound	Total	Origin
0	0.00000	21.07601	6.0+	0.00000	0.00000	0.00000	Preeq
1	0.04090	21.03511	3.0+	0.00000	0.00000	0.00000	Preeq
.....							

after which the inelastic cross section to every individual discrete state of the target nucleus is printed, including the separation in direct and compound, see Eq. (3.16). These are summed, per contribution, to

the total discrete inelastic cross section, see Eq. (3.15). To these cross sections, the continuum inelastic cross sections of Eq. (3.17) are added to give the total inelastic cross section (3.14). Finally, the  $(n, \gamma n)$  cross section is also printed. This output block looks as follows

Inelastic cross sections:

Inclusive:

Level	Energy	E-out	J/P	Direct	Compound	Total	Origin
1	0.03082	13.81772	0.5-	0.00670	0.00022	0.00692	Direct
2	0.68700	13.16154	1.5-	0.02617	0.00041	0.02658	Direct
3	0.74391	13.10463	3.5+	4.28590	0.00083	4.28673	Direct
4	0.80858	13.03996	2.5+	0.34804	0.00062	0.34866	Direct
5	0.81041	13.03813	2.5-	3.20590	0.00061	3.20651	Direct
6	0.94983	12.89871	6.5+	7.42960	0.00123	7.43083	Direct
7	0.97000	12.87854	1.5-	0.24587	0.00040	0.24627	Direct
8	0.97894	12.86960	5.5+	6.35960	0.00113	6.36073	Direct
9	1.08267	12.76587	4.5+	5.27330	0.00099	5.27429	Direct
10	1.12685	12.72169	2.5-	0.08584	0.00059	0.08643	Direct
11	1.28440	12.56414	0.5+	0.01592	0.00020	0.01612	Direct
12	1.29000	12.55854	0.5-	0.11359	0.00020	0.11379	Direct
13	1.29724	12.55130	4.5+	0.52801	0.00097	0.52898	Direct
14	1.31514	12.53340	2.5-	0.08983	0.00058	0.09042	Direct
15	1.33000	12.51854	1.5+	0.40952	0.00040	0.40992	Direct
16	1.33519	12.51335	8.5+	0.96755	0.00121	0.96876	Direct
17	1.36400	12.48454	2.5-	0.31557	0.00058	0.31615	Direct
18	1.36970	12.47884	1.5+	0.03000	0.00040	0.03041	Direct
19	1.39512	12.45342	2.5+	0.02125	0.00060	0.02185	Direct
20	1.45420	12.39434	1.5+	0.21369	0.00040	0.21409	Direct
				-----	-----	-----	
Discrete Inelastic:				29.97186	0.01257	29.98442	
Continuum Inelastic:				423.00357	1209.48877	1632.49231	
				-----	-----	-----	
Total Inelastic:				452.97543	1209.50134	1662.47888	

$(n, \gamma n)$  cross section: 1.64203

This is repeated for the  $(n, p)$  and other channels,

$(n, p)$  cross sections:

Inclusive:

Level	Energy	E-out	J/P	Direct	Compound	Total	Origin
0	0.00000	14.53953	2.5+	0.41392	0.00042	0.41435	Preeq
1	0.26688	14.27265	1.5+	1.38195	0.00027	1.38222	Preeq
2	0.94714	13.59239	0.5+	1.06122	0.00012	1.06134	Preeq

```

3   1.01800  13.52153   0.5+   0.30259   0.00012   0.30271   Preeq
.....

```

The last column in these tables specifies the origin of the direct contribution to the discrete state. “Direct” means that this is obtained with coupled-channels, DWBA or, as in this case, weak coupling, whereas “Preeq” means that the pre-equilibrium cross section is collapsed onto the discrete states, as an approximate method for more exact direct reaction approaches for charge-exchange and pick-up reactions. We note here that the feature of calculating, and printing, the inelastic cross sections for a specific state is of particular interest in the case of excitations, i.e. to obtain this particular cross section for a whole range of incident energies. This will be handled in another sample case.

Since **outspectra y** was specified in the input file, the composite particle spectra for the continuum are also printed. Besides the total spectrum, the division into direct (i.e. smoothed collective effects and giant resonance contributions), pre-equilibrium, multiple pre-equilibrium and compound is given. First we give the photon spectrum,

#### 7. Composite particle spectra

Spectra for outgoing gamma

Energy	Total	Direct	Pre-equil.	Mult. preeq	Compound
0.001	1.07448E+01	0.00000E+00	7.77957E-14	0.00000E+00	1.07448E+01
0.002	1.08660E+01	0.00000E+00	6.20080E-13	0.00000E+00	1.08660E+01
0.005	1.12280E+01	0.00000E+00	9.58372E-12	0.00000E+00	1.12280E+01
0.010	1.18320E+01	0.00000E+00	7.53227E-11	0.00000E+00	1.18320E+01
0.020	1.30421E+01	0.00000E+00	5.82478E-10	0.00000E+00	1.30421E+01
0.050	1.68667E+01	0.00000E+00	8.30360E-09	0.00000E+00	1.68667E+01
0.100	3.33188E+01	0.00000E+00	5.84042E-08	0.00000E+00	3.33188E+01

.....

followed by the neutron spectrum

Spectra for outgoing neutron

Energy	Total	Direct	Pre-equil.	Mult. preeq	Compound
0.001	1.80043E+01	7.61374E-03	9.24702E-02	0.00000E+00	1.79042E+01
0.002	3.59551E+01	7.62584E-03	1.39595E-01	0.00000E+00	3.58079E+01
0.005	8.98079E+01	7.66226E-03	2.62957E-01	0.00000E+00	8.95373E+01
0.010	1.45532E+02	7.72330E-03	4.71854E-01	0.00000E+00	1.45053E+02
0.020	2.60310E+02	7.84672E-03	9.49223E-01	0.00000E+00	2.59353E+02
0.050	5.09727E+02	8.22780E-03	2.79126E+00	0.00000E+00	5.06928E+02

.....

and the spectra for the other outgoing particles. Depending on the value of **ddxmode**, the double-differential cross sections are printed as angular distributions or as spectra per fixed angle. For the present sample case, **ddxmode 2**, which gives

## 9. Double-differential cross sections per outgoing angle

DDX for outgoing neutron at 0.000 degrees

E-out	Total	Direct	Pre-equil.	Mult. preeq	Compound
0.001	1.43656E+00	1.49563E-03	1.02952E-02	0.00000E+00	1.42477E+00
0.002	2.86654E+00	1.49801E-03	1.55424E-02	0.00000E+00	2.84950E+00
0.005	7.15593E+00	1.50516E-03	2.92805E-02	0.00000E+00	7.12515E+00
0.010	1.15970E+01	1.51715E-03	5.25511E-02	0.00000E+00	1.15429E+01
0.020	2.07460E+01	1.54139E-03	1.05755E-01	0.00000E+00	2.06387E+01
0.050	4.06530E+01	1.61625E-03	3.11320E-01	0.00000E+00	4.03400E+01
0.100	6.26393E+01	1.74839E-03	7.35296E-01	0.00000E+00	6.19022E+01
.....					

followed by the other angles and other particles. A final important feature of the present input file is that some requested information has been written to separate output files, i.e. besides the standard output file, TALYS also produces the ready-to-plot files

```

aspec014.000.tot
nspec014.000.tot
pspec014.000.tot

```

containing the angle-integrated neutron, proton and alpha spectra, and

```

addx030.0.deg
addx060.0.deg
nndx030.0.deg
nndx060.0.deg

```

containing the double-differential neutron and alpha spectra at 30 and 60 degrees.

**Case 1c: Exclusive channels and spectra**

As another extension of the simple input file we can print the exclusive cross sections at one incident energy and the associated exclusive spectra. This is accomplished with the input file

```

#
# General
#
projectile n
element nb
mass 93
energy 14.
#
# Output
#
channels y
outspectra y

```

Contrary to the previous sample case, in this case no double-differential cross sections or results per separate file are printed (since it only concerns one incident energy). The exclusive cross sections are given in one table, per channel and per ground or isomeric state. It is checked whether the exclusive cross sections add up to the non-elastic cross section. Note that this sum rule, Eq. (3.25), is only expected to hold if we include enough exclusive channels in the calculation. If **maxchannel 4**, this equality should always hold for incident energies up to 20 MeV. This output block looks as follows:

## 6. Exclusive cross sections

## 6a. Total exclusive cross sections

Emitted particles						cross section	reaction	level	isomeric	i
n	p	d	t	h	a			cross section		
0	0	0	0	0	0	1.32555E+00	(n,g)			
								0	6.47368E-01	0
								1	6.78179E-01	0
1	0	0	0	0	0	3.16052E+02	(n,n')			
								0	2.69685E+02	0
								1	4.63666E+01	0
0	1	0	0	0	0	4.26930E+01	(n,p)			
0	0	1	0	0	0	1.56242E+01	(n,d)			
0	0	0	1	0	0	1.69988E+00	(n,t)			
0	0	0	0	0	1	2.52320E+01	(n,a)			
								0	1.54992E+01	0
								2	9.73280E+00	0
2	0	0	0	0	0	1.34213E+03	(n,2n)			
								0	8.36589E+02	0
								1	5.05542E+02	0
1	1	0	0	0	0	1.72966E+01	(n,np)			
1	0	0	0	0	1	6.89726E+00	(n,na)			
								0	2.73542E+00	0
								1	4.16185E+00	0
0	1	0	0	0	1	3.43325E-05	(n,pa)			
Sum over exclusive channel cross sections:						1768.95142				
(n,gn) + (n,gp) + ... (n,ga) cross sections:						1.64698				
Total						:	1770.59839			
Non-elastic cross section						:	1770.59888			

Note that the  $(n, np)$  and  $(n, d)$  cross sections add up to the residual production cross section for  $^{92}\text{Zr}$ , as given in the first sample case.

Since **outspectra y**, for each exclusive channel the spectrum per outgoing particle is given. This output block begins with:

## 6b. Exclusive spectra

Emitted particles						cross section	reaction	gamma cross section
n	p	d	t	h	a			

1 0 0 0 0 0 3.16052E+02 (n,n') 9.12016E+02

Outgoing spectra

Energy	gamma	neutron	proton	deuteron	triton	helium-3
0.001	3.57321E+00	2.59740E-03	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.002	3.58633E+00	5.11581E-03	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.005	3.62547E+00	1.26479E-02	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.010	3.69087E+00	2.52061E-02	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.020	3.82229E+00	5.04091E-02	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.050	4.24220E+00	1.26614E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.100	8.50673E+00	2.54669E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00

.....

Emitted particles						cross section	reaction	gamma cross section
n	p	d	t	h	a			
1	1	0	0	0	0	1.72966E+01	(n,np)	3.30569E+01

Outgoing spectra

Energy	gamma	neutron	proton	deuteron	triton	helium-3
0.001	1.16492E+00	3.20739E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.002	1.18673E+00	6.41270E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.005	1.25184E+00	1.60280E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.010	1.36049E+00	3.21639E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.020	1.57827E+00	6.60275E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.050	2.23543E+00	1.08376E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.100	3.33191E+00	1.63093E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.200	3.42848E+00	1.86920E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.300	4.60475E+00	1.64815E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.400	4.04534E+00	1.51041E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.500	2.25828E+00	1.36434E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.600	9.77059E+00	1.23647E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.700	1.54627E+01	1.04796E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.800	8.29432E+00	9.30014E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.900	3.81049E+00	8.06707E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
1.000	3.41791E+00	6.49638E+00	1.42922E-07	0.00000E+00	0.00000E+00	0.00000E+00
1.100	3.27169E+00	5.60680E+00	1.61977E-06	0.00000E+00	0.00000E+00	0.00000E+00
1.200	5.63783E+00	4.92774E+00	1.27749E-05	0.00000E+00	0.00000E+00	0.00000E+00

.....

Note, as explained in Section 3.3.2, the (n,np) cross section is characterized by both a neutron and a proton spectrum.

**Case 1d: Nuclear structure**

It is possible to have all the nuclear structure information in the output file. The simplest way is to set **outbasic y**, which means that about everything that can be printed, will be printed. This may be a bit

overdone if one is only interested in e.g. discrete levels or level densities. If the keywords **outlevels** and/or **outdensity** are set to **y**, discrete level and level density information will always be given for the target nucleus and the primary compound nucleus. With **outgamma y**, photon strength function information is also given. If we would set, in addition, **outpopulation y**, this info will also be given for all the other residual nuclides that are reached in the reaction chain. The input file for this sample case is

```
#
# General
#
projectile n
element nb
mass 93
energy 14.
#
# Output
#
outlevels y
outdensity y
outgamma y
```

In addition to the output of case 1a, the separation energies for the six light particles are printed.

NUCLEAR STRUCTURE INFORMATION FOR Z= 41 N= 52 ( 93Nb)

Separation energies:

Particle	S
neutron	8.83111
proton	6.04315
deuteron	12.45333
triton	13.39060
helium-3	15.65209
alpha	1.93155

In the next output block, the discrete level scheme is printed for the first **maxlevelstar** levels. The discrete level info contains level number, energy, spin, parity, branching ratios and lifetimes of possible isomers. It is also indicated whether the spin (J) or parity (P) of a level is experimentally known or whether a value was assigned to it (see Section 5.4). The “string” of the original ENSDF database is also given, so that the user can learn about possible alternative choices for spin and parity. This output block begins with:

Discrete levels of Z= 41 N= 52 ( 93Nb)

Number	Energy	Spin	Parity	Branching	Ratio (%)	Lifetime(sec)	Assignment
0	0.0000	4.5	+				
1	0.0308	0.5	-			5.090e+08	
				---	0	100.0000	

```

2      0.6870  1.5  -
                                     ---->  1  100.0000
3      0.7439  3.5  +
                                     ---->  0  100.0000
4      0.8086  2.5  +
                                     ---->  0   96.1951
                                     ---->  3   3.8049
.....

```

Since **outdensity y**, we print all the level density parameters that are involved, as discussed in Section 4.7: the level density parameter at the neutron separation energy  $a(S_n)$ , the experimental and theoretical average resonance spacing  $D_0$ , the asymptotic level density parameter  $\tilde{a}$ , the shell damping parameter  $\gamma$ , the pairing energy  $\Delta$ , the shell correction energy  $\delta W$ , the matching energy  $E_x$ , the last discrete level, the levels for the matching problem, the temperature  $T$ , the back-shift energy  $E_0$ , the discrete state spin cutoff parameter  $\sigma$  and the spin cutoff parameter at the neutron separation energy. Next, we print a table with the level density parameter  $a$ , the spin cutoff parameter and the level density itself, all as a function of the excitation energy. This output block begins with:

Level density parameters for Z= 41 N= 52 ( 93Nb)

```

a(Sn)           : 11.57705
Experimental D0 :      0.00 eV +-      0.00000
Theoretical D0  :      84.70 eV
Asymptotic a    : 11.48972
Damping gamma   :  0.10131
Pairing energy   :  1.24434
Shell correction:  0.10752
Matching Ex     :  8.36497
Last disc. level:      20
Nlow            :      2
Ntop           :      24
Temperature     :  0.94199
E0             : -1.80827
disc. spin cut  :  3.11002
spin cut (Sn)   :  4.13315

```

Total level density for ground state

```

Ex      a      sp cut  total  JP= 0.5+  JP= 1.5+  JP= 2.5+  JP= 3.5+  JP= 4.5+
0.20 11.615  3.023 8.950E+00 4.635E-01 7.867E-01 8.977E-01 8.162E-01 6.236E-01
0.40 11.615  3.053 1.107E+01 5.626E-01 9.580E-01 1.099E+00 1.007E+00 7.765E-01
0.60 11.615  3.083 1.369E+01 6.831E-01 1.167E+00 1.345E+00 1.241E+00 9.663E-01
0.80 11.615  3.112 1.692E+01 8.297E-01 1.421E+00 1.647E+00 1.530E+00 1.202E+00
1.00 11.615  3.141 2.093E+01 1.008E+00 1.732E+00 2.016E+00 1.885E+00 1.494E+00
.....

```

Finally, a comparison of the total level density with the cumulative number of discrete levels is given,

Discrete levels versus constant temperature formula

Energy	Level	N_cumulative
0.0308	1	-5.094
0.6870	2	2.000
0.7439	3	2.881
0.8086	4	3.948
0.8104	5	3.979
0.9498	6	6.550
0.9700	7	6.955
0.9789	8	7.137
1.0827	9	9.381
1.1269	10	10.414
1.2844	11	14.520
1.2900	12	14.679
1.2972	13	14.886

.....

With **outgamma y** the gamma-ray information is printed. First, all relevant parameters are given: the total radiative width  $\Gamma_\Gamma$ , the s-wave resonance spacing  $D_0$ , the s-wave strength function  $S_0$  and the renormalisation factor for the gamma-ray strength function. Second, we print the giant resonance information. For each multipolarity, we print the strength of the giant resonance  $\sigma_0$ , its energy and its width. Next, the gamma-ray strength function and transmission coefficients for this multipolarity and as a function of energy are printed. This output block begins with:

```
##### GAMMA STRENGTH FUNCTIONS, TRANSMISSION COEFFICIENTS AND CROSS SECTION
```

```
Gamma-ray information for Z= 41 N= 53 ( 94Nb)
```

```
S-wave strength function parameters:
```

```
Exp. total radiative width= 0.14500 eV +/- 0.01000
Exp. D0                      = 44.00 eV +/- 4.00 Theor. D0
Exp. S-wave strength func.= 0.45000E-4 +/- 0.07000 Theor. S-wave strength func
Normalization factor        = 1.66018
```

```
Normalized gamma-ray strength functions and transmission coefficients for l= 1
```

```
Giant resonance parameters :
```

```
sigma0(M1) = 2.515          sigma0(E1) = 192.148
  E(M1)    = 9.017          E(E1)    = 16.523
gamma(M1)  = 4.000          gamma(E1) = 5.515
  k(M1)    = 8.67373E-08    k(E1)    = 8.67373E-08
```

```
  E          f(M1)          f(E1)          T(M1)          T(E1)
```

```

0.001  0.000000E+00  1.12967E-08  0.000000E+00  7.09794E-17
0.002  1.75304E-12  1.12961E-08  8.81174E-20  5.67806E-16
0.005  4.38260E-12  1.12944E-08  3.44209E-18  8.87059E-15
0.010  8.76522E-12  1.12914E-08  5.50735E-17  7.09462E-14
0.020  1.75306E-11  1.12855E-08  8.81182E-16  5.67273E-13
0.050  4.38284E-11  1.12677E-08  3.44228E-14  8.84961E-12
.....

```

which is repeated for each  $l$ -value. Finally, the photoabsorption cross section is printed:

Photoabsorption cross sections

```

E      reaction
0.001  7.8450E-05
0.002  1.5689E-04
0.005  3.9217E-04
0.010  7.8413E-04
0.020  1.5674E-03
0.050  3.9124E-03
0.100  7.8038E-03
0.200  1.5521E-02
0.300  2.3147E-02
0.400  3.0679E-02
0.500  3.8113E-02
.....

```

### Case 1e: Detailed pre-equilibrium information

The single- and double-differential spectra have already been covered in sample 1b. In addition to this, the contribution of the pre-equilibrium mechanism to the spectra and cross sections can be printed in more detail with the **outpreequilibrium** keyword. With the input file

```

#
# General
#
projectile n
element nb
mass 93
energy 14.
#
# Output
#
outpreequilibrium  y
outspectra        y
ddxmode           2

```

we obtain, in addition to the aforementioned output blocks, a detailed outline of the pre-equilibrium model used, in this case the default: the two-component exciton model. First, the parameters for the exciton model are printed, followed by the matrix elements as a function of the exciton number:

##### PRE-EQUILIBRIUM #####

+++++++ TWO-COMPONENT EXCITON MODEL ++++++

1. Matrix element for E= 21.076

Constant for matrix element : 1.000

p-n ratio for matrix element: 1.500

p(p)	h(p)	p(n)	h(n)	M2pipi	M2nunu	M2pinu	M2nupi
0	0	1	0	2.39474E-05	2.39474E-05	3.59211E-05	3.59211E-05
0	0	2	1	9.89863E-05	9.89863E-05	1.48479E-04	1.48479E-04
1	1	1	0	9.89863E-05	9.89863E-05	1.48479E-04	1.48479E-04
0	0	3	2	1.60585E-04	1.60585E-04	2.40877E-04	2.40877E-04
1	1	2	1	1.60585E-04	1.60585E-04	2.40877E-04	2.40877E-04

Next, the emission rates are printed: first as function of particle type and particle-hole number, and in the last column summed over particles:

2. Emission rates or escape widths

A. Emission rates ( /sec)

p(p)	h(p)	p(n)	h(n)	gamma	neutron	proton	deuteron	
0	0	1	0	2.15205E+18	0.00000E+00	0.00000E+00	0.00000E+00	0
0	0	2	1	4.85969E+17	1.83695E+21	0.00000E+00	0.00000E+00	0
1	1	1	0	5.13328E+17	9.15836E+20	2.71437E+20	4.76095E+19	0
0	0	3	2	1.04881E+17	5.68421E+20	0.00000E+00	0.00000E+00	0
1	1	2	1	8.72467E+16	3.78888E+20	1.45084E+19	5.78406E+18	2
2	2	1	0	1.27202E+17	1.70435E+20	2.53416E+19	3.31059E+18	0

Also, the alternative representation in terms of the escape widths, see Eqs. (4.106) and (4.107), is given,

B. Escape widths (MeV)

p(p)	h(p)	p(n)	h(n)	gamma	neutron	proton	deuteron	
0	0	1	0	1.41650E-03	0.00000E+00	0.00000E+00	0.00000E+00	0
0	0	2	1	3.19871E-04	1.20910E+00	0.00000E+00	0.00000E+00	0
1	1	1	0	3.37879E-04	6.02815E-01	1.78663E-01	3.13372E-02	0
0	0	3	2	6.90338E-05	3.74142E-01	0.00000E+00	0.00000E+00	0
1	1	2	1	5.74268E-05	2.49389E-01	9.54958E-03	3.80714E-03	1
2	2	1	0	8.37259E-05	1.12183E-01	1.66801E-02	2.17907E-03	0

The internal transition rates such as those of Eq. (4.72) and the associated damping and total widths are given next,

3. Internal transition rates or damping widths, total widths

A. Internal transition rates ( /sec)

p(p)	h(p)	p(n)	h(n)	lambdapiplus	lambdanuplus	lambdapinu	lambdanupi
0	0	1	0	1.98349E+21	1.06047E+21	0.00000E+00	0.00000E+00
0	0	2	1	4.33616E+21	2.22327E+21	0.00000E+00	2.21109E+20
1	1	1	0	2.06264E+21	4.23797E+21	1.77324E+20	0.00000E+00
0	0	3	2	4.45182E+21	2.17669E+21	0.00000E+00	9.72765E+20
1	1	2	1	3.04003E+21	3.30666E+21	2.35507E+20	3.12259E+20

The lifetimes,  $t(p, h)$  of Eq. (4.95) and the depletion factors  $D_{p,h}$  of Eq. (4.96), are printed next,

4. Lifetimes

p(p)	h(p)	p(n)	h(n)	Strength
0	0	1	0	3.28288E-22
0	0	2	1	4.21795E-23
1	1	1	0	8.56046E-23
0	0	3	2	1.39265E-23
1	1	2	1	8.03797E-23
2	2	1	0	2.95469E-23

The partial state densities are printed for the first particle-hole combinations as a function of excitation energy. We also print the exciton number-dependent spin distributions and their sum, to see whether we have exhausted all spins. This output block is as follows

+++++++ PARTIAL STATE DENSITIES ++++++

Particle-hole state densities

Ex	gp	gn	Configuration		p(p)	h(p)	p(n)	h(n)
			1 1 0 0	0 0 1 1	1 1 1 0	1 0 1 1	2 1 0 0	
1.000	2.733	3.533	7.4711E+00	1.2484E+01	9.7277E+00	1.1391E+01	3.6748E-0	
2.000	2.733	3.533	1.4942E+01	2.4969E+01	4.5589E+01	5.6335E+01	8.2121E+0	
3.000	2.733	3.533	2.2413E+01	3.7453E+01	1.0785E+02	1.3540E+02	2.6267E+0	
4.000	2.733	3.533	2.9884E+01	4.9938E+01	1.9651E+02	2.4860E+02	5.4533E+0	
5.000	2.733	3.533	3.7356E+01	6.2422E+01	3.1156E+02	3.9591E+02	9.3009E+0	
6.000	2.733	3.533	4.4827E+01	7.4907E+01	4.5301E+02	5.7735E+02	1.4170E+0	

Particle-hole spin distributions

n	J= 0	J= 1	J= 2	J= 3	J= 4	J= 5
1	1.7785E-02	4.3554E-02	4.8369E-02	3.6832E-02	2.1025E-02	9.3136E-03

2	6.3683E-03	1.7261E-02	2.3483E-02	2.4247E-02	2.0773E-02	1.5284E-02	9.8
3	3.4812E-03	9.7603E-03	1.4208E-02	1.6237E-02	1.5926E-02	1.3878E-02	1.0
4	2.2659E-03	6.4613E-03	9.7295E-03	1.1698E-02	1.2277E-02	1.1642E-02	1.0
5	1.6234E-03	4.6764E-03	7.1862E-03	8.9070E-03	9.7354E-03	9.7128E-03	8.9
6	1.2360E-03	3.5846E-03	5.5835E-03	7.0625E-03	7.9311E-03	8.1850E-03	7.8

.....

We print a table with the pre-equilibrium cross sections per stage and outgoing energy, for each outgoing particle. At the end of each table, we give the total pre-equilibrium cross sections per particle. Finally the total pre-equilibrium cross section summed over outgoing particles is printed,

+++++++ TOTAL PRE-EQUILIBRIUM CROSS SECTIONS ++++++

Pre-equilibrium cross sections for gamma

E	Total	p=1	p=2	p=3	p=4	p=5	p=
0.001	7.7796E-14	3.3942E-14	1.7004E-14	1.2867E-14	1.3982E-14	0.0000E+00	0.0000
0.002	6.2008E-13	2.6984E-13	1.3573E-13	1.0278E-13	1.1172E-13	0.0000E+00	0.0000
0.005	9.5837E-12	4.1388E-12	2.1067E-12	1.5989E-12	1.7394E-12	0.0000E+00	0.0000
0.010	7.5323E-11	3.2125E-11	1.6669E-11	1.2697E-11	1.3831E-11	0.0000E+00	0.0000
0.020	5.8248E-10	2.4256E-10	1.3049E-10	1.0009E-10	1.0933E-10	0.0000E+00	0.0000
0.050	8.3036E-09	3.2424E-09	1.9147E-09	1.4979E-09	1.6486E-09	0.0000E+00	0.0000
0.100	5.8404E-08	2.0886E-08	1.3890E-08	1.1181E-08	1.2446E-08	0.0000E+00	0.0000
.....							
19.500	1.2868E-01	1.2531E-01	3.2519E-03	1.2190E-04	9.8971E-07	0.0000E+00	0.0000
20.000	1.1744E-01	1.1477E-01	2.6309E-03	4.3524E-05	6.4873E-08	0.0000E+00	0.0000
21.000	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000
22.000	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000
	1.3202E+00	1.1850E+00	1.0809E-01	2.0517E-02	6.5982E-03	0.0000E+00	0.0000

Integrated: 1.32020

Pre-equilibrium cross sections for neutron

E	Total	p=1	p=2	p=3	p=4	p=5	p=
0.001	9.2470E-02	0.0000E+00	2.3603E-02	2.6619E-02	2.2236E-02	1.2354E-02	7.6581
0.002	1.3960E-01	0.0000E+00	3.5641E-02	4.0188E-02	3.3566E-02	1.8645E-02	1.1555
0.005	2.6296E-01	0.0000E+00	6.7194E-02	7.5723E-02	6.3212E-02	3.5093E-02	2.1735
0.010	4.7185E-01	0.0000E+00	1.2074E-01	1.3594E-01	1.1338E-01	6.2885E-02	3.8907
0.020	9.4922E-01	0.0000E+00	2.4359E-01	2.7370E-01	2.2789E-01	1.2616E-01	7.7891
0.050	2.7913E+00	0.0000E+00	7.2235E-01	8.0694E-01	6.6835E-01	3.6790E-01	2.2572
0.100	6.5806E+00	0.0000E+00	1.7270E+00	1.9105E+00	1.5685E+00	8.5529E-01	5.1924
.....							
16.500	1.4846E+00	0.0000E+00	0.0000E+00	0.0000E+00	6.8127E-04	9.2647E-06	2.0113
17.000	1.0827E+00	0.0000E+00	0.0000E+00	0.0000E+00	2.5663E-04	1.8777E-07	0.0000

```

17.500 1.5939E-01 0.0000E+00 0.0000E+00 0.0000E+00 5.4730E-06 0.0000E+00 0.0000
18.000 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000
18.500 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000
19.000 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000E+00 0.0000

1.8790E+01 0.0000E+00 0.0000E+00 0.0000E+00 1.7624E-02 1.8053E-02 7.4711

```

Integrated: 18.79024

Total pre-equilibrium cross section: 424.54468

**Case 1f: Discrete direct cross sections and angular distributions**

More specific information on the characteristics of direct reactions can be obtained with the following input file,

```

#
# General
#
projectile n
element nb
mass 93
energy 14.
#
# Output
#
outdiscrete      y
outangle         y
outlegendre     y
outdirect       y
outspectra      y

```

Now we obtain, through **outdirect y**, the direct cross sections from inelastic collective scattering and giant resonances. The output block begins with

+++++++ DIRECT CROSS SECTIONS ++++++

Direct inelastic cross sections

Level	Energy	E-out	J/P	Cross section	Def. par.
1	0.03082	13.81772	0.5-	0.00670	B 0.00239
2	0.68700	13.16154	1.5-	0.02617	B 0.00511
3	0.74391	13.10463	3.5+	4.28590	B 0.04699
4	0.80858	13.03996	2.5+	0.34804	B 0.01746
5	0.81041	13.03813	2.5-	3.20590	B 0.04070
6	0.94983	12.89871	6.5+	7.42960	B 0.06216

.....

92	12.99300	0.85554	0.5+	0.00348	B	0.00504
93	13.09000	0.75854	3.5-	0.01298	B	0.01008
94	13.54200	0.30654	7.5-	0.01675	B	0.01191
95	13.58100	0.26754	1.5+	0.01197	B	0.01426

Discrete direct inelastic cross section: 29.97186 Level 1- 20  
 Collective cross section in continuum : 39.60126

which for the case of  $^{93}\text{Nb}$  gives the results of the weak-coupling model. For every level, the angular distribution is given, since **outangle y** was specified:

Direct inelastic angular distributions

Angle	Ex= 0.031 JP= 0.5-	Ex= 0.687 JP= 1.5-	Ex= 0.744 JP= 3.5+	Ex= 0.809 JP= 2.5+	Ex= 0.810 JP= 2.5-	Ex= 0.950 JP= 6.5+	E
0.0	1.06390E-03	1.20540E-03	1.31080E+00	5.34730E-02	9.79820E-01	2.26740E+00	1.
2.0	1.06610E-03	1.21590E-03	1.30680E+00	5.36030E-02	9.76820E-01	2.26050E+00	1.
4.0	1.07260E-03	1.24700E-03	1.29520E+00	5.39920E-02	9.68170E-01	2.24050E+00	1.
6.0	1.08340E-03	1.29800E-03	1.27750E+00	5.46330E-02	9.54870E-01	2.20960E+00	1.
8.0	1.09840E-03	1.36810E-03	1.25530E+00	5.55120E-02	9.38300E-01	2.17110E+00	1.
.....							

The table with total giant resonance results is given next,

+++++++ GIANT RESONANCES ++++++

	Cross section	Exc. energy	Emis. energy	Width	Deform. par.
GMR :	0.00000	16.37500	-2.52646	3.00000	0.02538
GQR :	0.00000	14.34671	-0.49817	4.14092	0.13794
LEOR :	23.72300	6.84228	7.00626	5.00000	0.15585
HEOR :	0.00000	25.38264	-11.53410	7.36250	0.13210

Total: 23.72300

followed, since **outspectra y**, by the associated spectra,

Giant resonance spectra

Energy	Total	GMR	GQR	LEOR	HEOR	Collective
0.001	7.6137E-03	0.0000E+00	0.0000E+00	7.6137E-03	0.0000E+00	0.0000E+00
0.002	7.6258E-03	0.0000E+00	0.0000E+00	7.6258E-03	0.0000E+00	0.0000E+00
0.005	7.6623E-03	0.0000E+00	0.0000E+00	7.6623E-03	0.0000E+00	0.0000E+00
0.010	7.7233E-03	0.0000E+00	0.0000E+00	7.7233E-03	0.0000E+00	0.0000E+00
0.020	7.8467E-03	0.0000E+00	0.0000E+00	7.8467E-03	0.0000E+00	0.0000E+00
0.050	8.2278E-03	0.0000E+00	0.0000E+00	8.2278E-03	0.0000E+00	0.0000E+00
0.100	8.9005E-03	0.0000E+00	0.0000E+00	8.9005E-03	0.0000E+00	0.0000E+00

```

0.200 1.0398E-02 0.0000E+00 0.0000E+00 1.0398E-02 0.0000E+00 0.0000E+00
0.300 1.7966E-01 0.0000E+00 0.0000E+00 1.2119E-02 0.0000E+00 1.6754E-01
0.400 1.4094E-02 0.0000E+00 0.0000E+00 1.4094E-02 0.0000E+00 0.0000E+00
0.500 1.6353E-02 0.0000E+00 0.0000E+00 1.6353E-02 0.0000E+00 0.0000E+00
0.600 1.8931E-02 0.0000E+00 0.0000E+00 1.8931E-02 0.0000E+00 0.0000E+00
0.700 2.1866E-02 0.0000E+00 0.0000E+00 2.1866E-02 0.0000E+00 0.0000E+00
.....

```

The total, i.e. direct + compound cross section per discrete level of each residual nucleus was already described for sample 1b. In addition, we have now requested the angular distributions and the associated Legendre coefficients. First, the angular distribution for elastic scattering, separated by direct and compound contribution, is given. Since **outlegendre y** it is given first in terms of Legendre coefficients. This output block begins with:

8. Discrete state angular distributions

8a1. Legendre coefficients for elastic scattering

L	Total	Direct	Compound	Normalized
0	1.75971E+02	1.75971E+02	8.39371E-05	7.95781E-02
1	1.55728E+02	1.55728E+02	0.00000E+00	7.04236E-02
2	1.39719E+02	1.39719E+02	3.78743E-06	6.31843E-02
3	1.21487E+02	1.21487E+02	0.00000E+00	5.49392E-02
4	1.02658E+02	1.02658E+02	6.43797E-07	4.64242E-02
5	8.22089E+01	8.22089E+01	0.00000E+00	3.71767E-02
6	6.32520E+01	6.32520E+01	1.74904E-07	2.86040E-02

.....

where the final column means division of the Legendre coefficients by the cross section. This is followed by the associated angular distribution. This output block begins with:

8a2. Elastic scattering angular distribution

Angle	Total	Direct	Compound
0.0	6.69550E+03	6.69550E+03	1.12410E-04
2.0	6.62130E+03	6.62130E+03	1.12272E-04
4.0	6.40310E+03	6.40310E+03	1.11863E-04
6.0	6.05380E+03	6.05380E+03	1.11199E-04
8.0	5.59360E+03	5.59360E+03	1.10304E-04
10.0	5.04820E+03	5.04820E+03	1.09210E-04
12.0	4.44650E+03	4.44650E+03	1.07951E-04
14.0	3.81860E+03	3.81860E+03	1.06568E-04
16.0	3.19320E+03	3.19320E+03	1.05098E-04
18.0	2.59560E+03	2.59560E+03	1.03576E-04

.....

Next, the Legendre coefficients for inelastic scattering to each discrete level, separated by the direct and compound contribution, is given. This output block begins with:

8b1. Legendre coefficients for inelastic scattering

```

Level  1

L      Total      Direct      Compound      Normalized
0      5.50457E-04  5.33246E-04  1.72116E-05   7.95771E-02
1      1.86104E-04  1.86104E-04  0.00000E+00   2.69042E-02
2      6.21160E-05  6.21212E-05  -5.18825E-09   8.97982E-03
3      1.66501E-05  1.66501E-05  0.00000E+00   2.40703E-03
4     -1.38229E-05  -1.35861E-05  -2.36789E-07  -1.99831E-03
5     -1.90406E-05  -1.90406E-05  0.00000E+00  -2.75260E-03
6     -1.61407E-05  -1.61562E-05  1.54654E-08  -2.33339E-03
.....

```

which is also followed by the associated angular distributions. This output block begins with:

8b2. Inelastic angular distributions

```

Level  1

Angle   Total      Direct      Compound
0.0     1.07938E-03  1.06390E-03  1.54770E-05
2.0     1.08158E-03  1.06610E-03  1.54834E-05
4.0     1.08810E-03  1.07260E-03  1.55026E-05
6.0     1.09893E-03  1.08340E-03  1.55347E-05
8.0     1.11398E-03  1.09840E-03  1.55798E-05
10.0    1.13264E-03  1.11700E-03  1.56382E-05
.....

```

Finally, the same is given for the  $(n, p)$  and the other channels.

### Case 1g: Discrete gamma-ray production cross sections

The gamma-ray intensity for each mother and daughter discrete level appearing in the reaction can be obtained with the following input file,

```

#
# General
#
projectile n
element nb
mass 93
energy 14.
#

```

```
# Output
#
outgamdis          y
```

For all discrete gamma-ray transitions, the intensity is printed. For each nucleus, the initial level and the final level is given, the associated gamma energy and the cross section. This output block begins with:

10. Gamma-ray intensities

Nuclide: 94Nb

Initial level			Final level			Gamma Energy	Cross section	
no.	J/Pi	Ex	no.	J/Pi	Ex			
2	4.0+	0.0587	--->	1	3.0+	0.0409	0.01780	2.35107E-01
3	5.0+	0.0787	--->	0	6.0+	0.0000	0.07867	1.46791E-01
4	5.0+	0.1134	--->	0	6.0+	0.0000	0.11340	9.63191E-02
4	5.0+	0.1134	--->	2	4.0+	0.0587	0.05470	3.78759E-02
5	2.0-	0.1403	--->	1	3.0+	0.0409	0.09941	2.69549E-01
6	2.0-	0.3016	--->	5	2.0-	0.1403	0.16126	6.23859E-02
7	4.0+	0.3118	--->	2	4.0+	0.0587	0.25311	5.82774E-02

.....

When we discuss multiple incident energy runs in the other sample cases, we will see how the excitation functions for gamma production cross sections per level are accumulated and how they can be written to separate files for easy processing.

### Case 1h: The full output file

In this sample case we print basically everything that can be printed in the main output file for a single-energy reaction on a non-fissile nucleus. The input file is

```
#
# General
#
projectile n
element nb
mass 93
energy 14.
#
# Output
#
outbasic          y
outpreequilibrium y
outspectra       y
outangle         y
outlegendre      y
```

```

ddxmode          2
outgamdis        y
partable         y

```

resulting in an output file that contains all nuclear structure information, all partial results, and moreover all intermediate results of the calculation, as well as results of intermediate checking. Note that basically all flags in the "Output" block on top of the output file are set to **y**, the only exceptions being irrelevant for this sample case. In addition to the output that is already described, various other output blocks are present. First, since **outbasic y** automatically means **outomp y**, a block with optical model parameters is printed. The optical model parameters for all included particles are given as a function of incident energy. This output block begins with:

```

##### OPTICAL MODEL PARAMETERS #####

      neutron on 93Nb

Energy   V      rv      av      W      rw      aw      Vd      rvd      avd      Wd      rwd      awd

 0.001   51.02  1.215  0.663   0.14  1.215  0.663   0.00  1.274  0.534   3.32  1.274  0.534
 0.002   51.02  1.215  0.663   0.14  1.215  0.663   0.00  1.274  0.534   3.32  1.274  0.534
 0.005   51.02  1.215  0.663   0.14  1.215  0.663   0.00  1.274  0.534   3.32  1.274  0.534
 0.010   51.02  1.215  0.663   0.14  1.215  0.663   0.00  1.274  0.534   3.33  1.274  0.534
 0.020   51.02  1.215  0.663   0.14  1.215  0.663   0.00  1.274  0.534   3.33  1.274  0.534
.....

```

In the next part, we print general quantities that are used throughout the nuclear reaction calculations, such as transmission coefficients and inverse reaction cross sections. The transmission coefficients as a function of energy are given for all particles included in the calculation. Depending upon whether **outtransenergy y** or **outtransenergy n**, the transmission coefficient tables will be grouped per energy or per angular momentum, respectively. The latter option may be helpful to study the behavior of a particular transmission coefficient as a function of energy. The default is **outtransenergy n**, leading to the following output block,

```

##### TRANSMISSION COEFFICIENTS AND INVERSE REACTION CROSS SECTIONS #####

Transmission coefficients for incident neutron at 0.00101 MeV

L      T(L-1/2,L)      T(L+1/2,L)      Tav(L)

0      0.00000E+00      8.82151E-03      8.82151E-03
1      1.45426E-04      2.56094E-04      2.19204E-04

Transmission coefficients for incident neutron at 0.00202 MeV

L      T(L-1/2,L)      T(L+1/2,L)      Tav(L)

```

```

0  0.00000E+00  1.24534E-02  1.24534E-02
1  4.11564E-04  7.24748E-04  6.20353E-04
2  2.55792E-08  1.88788E-08  2.15589E-08
    
```

Transmission coefficients for incident neutron at 0.00505 MeV

```

L   T(L-1/2,L)   T(L+1/2,L)   Tav(L)

0  0.00000E+00  1.96206E-02  1.96206E-02
1  1.62865E-03  2.86732E-03  2.45443E-03
2  2.52143E-07  1.86211E-07  2.12583E-07
.....
    
```

which is repeated for each included particle type. Next, the (inverse) reaction cross sections is given for all particles on a LAB energy grid. For neutrons also the total elastic and total cross section on this energy grid is printed for completeness. This output block begins with:

Total cross sections for neutron

E	total	reaction	elastic	OMP reaction
0.00101	1.1594E+04	6.2369E+03	5.3568E+03	6.2369E+03
0.00202	1.0052E+04	4.7092E+03	5.3432E+03	4.7092E+03
0.00505	8.8645E+03	3.5517E+03	5.3128E+03	3.5517E+03
0.01011	8.4659E+03	3.1917E+03	5.2742E+03	3.1917E+03
0.02022	8.4355E+03	3.2206E+03	5.2150E+03	3.2206E+03
0.05054	8.9301E+03	3.8245E+03	5.1056E+03	3.8245E+03
0.10109	9.6340E+03	4.5803E+03	5.0537E+03	4.5803E+03
0.20217	1.0197E+04	5.0366E+03	5.1609E+03	5.0366E+03
0.30326	1.0067E+04	4.7875E+03	5.2798E+03	4.7875E+03
0.40434	9.6387E+03	4.3375E+03	5.3011E+03	4.3375E+03
0.50543	9.1155E+03	3.8892E+03	5.2263E+03	3.8892E+03
0.60651	8.5879E+03	3.5055E+03	5.0824E+03	3.5055E+03
0.70760	8.0913E+03	3.1968E+03	4.8945E+03	3.1968E+03
0.80869	7.6389E+03	2.9569E+03	4.6820E+03	2.9569E+03
0.90977	7.2332E+03	2.7749E+03	4.4583E+03	2.7749E+03
.....	.....	.....	.....	.....

The final column "OMP reaction" gives the reaction cross section as obtained from the optical model. This is not necessary the same as the adopted reaction cross section of the middle column, since sometimes (especially for complex particles) this is overruled by systematics, see the **sysreaction** keyword, page 128. For the incident energy, we separately print the OMP parameters, the transmission coefficients and the shape elastic angular distribution,

```

+++++++ OPTICAL MODEL PARAMETERS FOR INCIDENT CHANNEL ++++++++

neutron on 93Nb
    
```

Energy	V	rv	av	W	rw	aw	Vd	rvd	avd	Wd	rwd	awd
14.000	46.11	1.215	0.663	0.98	1.215	0.663	0.00	1.274	0.534	6.84	1.274	0.534

Optical model results

Total cross section : 3.9819E+03 mb  
 Reaction cross section: 1.7706E+03 mb  
 Elastic cross section : 2.2113E+03 mb

Transmission coefficients for incident neutron at 14.000 MeV

L	T(L-1/2,L)	T(L+1/2,L)	Tav(L)
0	0.00000E+00	7.46396E-01	7.46396E-01
1	8.02495E-01	7.78055E-01	7.86202E-01
2	7.77401E-01	8.08475E-01	7.96045E-01
3	7.75556E-01	6.94251E-01	7.29096E-01
4	9.15105E-01	9.53396E-01	9.36378E-01
5	6.01377E-01	6.19416E-01	6.11216E-01
6	7.00410E-01	4.72039E-01	5.77441E-01
7	1.15095E-01	1.90729E-01	1.55433E-01
8	1.59949E-02	1.88907E-02	1.75280E-02
9	2.36251E-03	2.49515E-03	2.43232E-03
10	3.55500E-04	3.61416E-04	3.58599E-04
11	5.38203E-05	5.39389E-05	5.38822E-05
12	8.20045E-06	8.17192E-06	8.18562E-06
13	1.26163E-06	1.25417E-06	1.25776E-06

Shape elastic scattering angular distribution

Angle	Cross section
0.0	6.69550E+03
2.0	6.62130E+03
4.0	6.40310E+03
6.0	6.05380E+03
8.0	5.59360E+03
10.0	5.04820E+03
12.0	4.44650E+03
14.0	3.81860E+03
16.0	3.19320E+03
18.0	2.59560E+03
20.0	2.04640E+03
.....	

At some point during a run, TALYS has performed the direct reaction calculation and the pre-equilibrium calculation. A table is printed which shows the part of the reaction population that is left for the formation of a compound nucleus. Since the pre-equilibrium cross sections are calculated on an emission energy

grid, there is always a small numerical error when transferring these results to the excitation energy grid. The pre-equilibrium spectra are therefore normalised. The output block looks as follows

```
##### POPULATION CHECK #####
```

```
Particle Pre-equilibrium Population
```

gamma	1.32020	1.31147
neutron	423.00357	406.83746
proton	37.51157	37.47223
deuteron	6.80613	6.78807
triton	0.43722	0.43606
helium-3	0.00000	0.00000
alpha	18.79024	18.73897

```
+++++++ Normalization of reaction cross section ++++++
```

Reaction cross section	:	1770.59998 (A)
Sum over T(j,l)	:	1770.60938 (B)
Compound nucleus formation c.s.	:	1237.40881 (C)
Ratio C/B	:	0.69886

After the compound nucleus calculation, the results from the binary reaction are printed. First, the binary cross sections for the included outgoing particles are printed, followed by, if **outspectra y**, the binary emission spectra. If also **outcheck y**, the integral over the emission spectra is checked against the cross sections. The printed normalisation factor has been applied to the emission spectra. This output block begins with:

```
##### BINARY CHANNELS #####
```

```
+++++++ BINARY CROSS SECTIONS ++++++
```

gamma	channel to Z= 41 N= 53 ( 94Nb):	2.97252E+00
neutron	channel to Z= 41 N= 52 ( 93Nb):	1.66248E+03
proton	channel to Z= 40 N= 53 ( 93Zr):	5.67462E+01
deuteron	channel to Z= 40 N= 52 ( 92Zr):	1.56242E+01
triton	channel to Z= 40 N= 51 ( 91Zr):	1.69988E+00
helium-3	channel to Z= 39 N= 52 ( 91Y ):	1.18587E-08
alpha	channel to Z= 39 N= 51 ( 90Y ):	3.10767E+01

```
Binary emission spectra
```

Energy	gamma	neutron	proton	deuteron	triton	helium-3
0.001	1.28431E-06	1.78574E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.002	2.56862E-06	3.51853E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.005	6.42156E-06	8.69890E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.010	1.28432E-05	1.73361E+01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00

```

0.020 2.56868E-05 3.46702E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.00000E+00
0.050 6.42239E-05 8.70823E+01 0.00000E+00 0.00000E+00 0.00000E+00 0.00000E+00
0.100 1.28490E-04 1.75155E+02 0.00000E+00 0.00000E+00 0.00000E+00 0.00000E+00
0.200 2.57243E-04 3.09603E+02 3.44003E-30 1.00473E-42 0.00000E+00 0.00000E+00
0.300 8.26832E-04 3.91481E+02 4.63229E-23 7.37855E-33 5.46001E-40 0.00000E+00
0.400 2.00068E-03 4.70986E+02 6.67507E-19 1.01526E-26 1.89812E-32 0.00000E+00
0.500 3.17500E-03 5.19460E+02 4.47055E-16 1.00460E-22 1.46916E-27 0.00000E+00
0.600 4.34979E-03 5.12247E+02 5.33358E-14 8.77018E-20 5.55849E-24 0.00000E+00
0.700 5.52504E-03 5.04658E+02 2.15272E-12 1.66469E-17 3.28683E-21 0.00000E+00
.....
+++++++ CHECK OF INTEGRATED BINARY EMISSION SPECTRA ++++++

```

	Continuum cross section	Integrated spectrum	Compound normalization
gamma	2.92930E+00	2.92930E+00	9.99662E-01
neutron	1.63248E+03	1.61642E+03	1.01720E+00
proton	5.22572E+01	5.22572E+01	1.00231E+00
deuteron	6.90078E+00	6.90078E+00	1.01691E+00
triton	4.42429E-01	4.42429E-01	1.01316E+00
helium-3	1.26526E-10	1.26526E-10	0.00000E+00
alpha	3.02202E+01	3.02202E+01	9.96359E-01

Since **outpopulation y**, the population that remains in the first set of residual nuclides after binary emission is printed,

```
+++++++ POPULATION AFTER BINARY EMISSION ++++++
```

```

Population of Z= 41 N= 53 ( 94Nb) after binary gamma emission: 2.97252E+00
Maximum excitation energy: 21.076 Discrete levels: 10 Continuum bins: 40 Contin

```

bin	Ex	Popul.	J= 0.0-	J= 0.0+	J= 1.0-	J= 1.0+	J= 2.0-	J= 2.0+
0	0.000	1.343E-06	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
1	0.041	7.080E-07	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
2	0.059	9.759E-07	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
3	0.079	1.607E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
4	0.113	3.621E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
5	0.140	1.105E-02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.105E-02	0.000E+00
6	0.302	1.007E-02	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.007E-02	0.000E+00
7	0.312	1.911E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
8	0.334	4.959E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
9	0.396	6.819E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
10	0.450	3.170E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
11	0.708	3.855E-02	1.874E-04	1.399E-04	1.483E-03	1.074E-03	3.145E-03	2.428E-03
12	1.224	6.000E-02	2.564E-04	1.913E-04	2.052E-03	1.485E-03	4.448E-03	3.434E-03
13	1.739	6.935E-02	2.592E-04	1.935E-04	2.094E-03	1.516E-03	4.625E-03	3.570E-03
14	2.255	7.741E-02	2.595E-04	1.937E-04	2.114E-03	1.530E-03	4.743E-03	3.661E-03

```
.....
```

where in this case bins 0-10 concern discrete levels and bins 11-50 concern continuum bins.

After this output of the binary emission, we print for each nuclide in the decay chain the population as a function of excitation energy, spin and parity *before* it decays. This loop starts with the initial compound nucleus and the nuclides formed by binary emission. When all excitation energy bins of the nucleus have been depleted, the final production cross section (per ground state/isomer) is printed. The feeding from this nuclide to all its daughter nuclides is also given. If in addition **outspectra y**, the emission spectra for all outgoing particles from this nucleus are printed. At high incident energies, when generally **multipreeq y**, the result from multiple pre-equilibrium emission is printed (not included in this output). If **outcheck y**, it is checked whether the integral over the emission spectra from this nucleus is equal to the corresponding feeding cross section. This output block begins with:

##### MULTIPLE EMISSION #####

Population of Z= 41 N= 53 ( 94Nb) before decay: 2.97252E+00  
 Maximum excitation energy: 21.076 Discrete levels: 10 Continuum bins: 40 Contin

bin	Ex	Popul.	J= 0.0	J= 1.0	J= 2.0	J= 3.0	J= 4.0	J= 5.0
0	0.000	1.343E-06	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00
1	0.041	7.080E-07	0.000E+00	0.000E+00	0.000E+00	7.080E-07	0.000E+00	0.000E+00
2	0.059	9.759E-07	0.000E+00	0.000E+00	0.000E+00	0.000E+00	9.759E-07	0.000E+00
3	0.079	1.607E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.607E-03
4	0.113	3.621E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	3.621E-03
5	0.140	1.105E-02	0.000E+00	0.000E+00	1.105E-02	0.000E+00	0.000E+00	0.000E+00
6	0.302	1.007E-02	0.000E+00	0.000E+00	1.007E-02	0.000E+00	0.000E+00	0.000E+00
7	0.312	1.911E-03	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.911E-03	0.000E+00
8	0.334	4.959E-03	0.000E+00	0.000E+00	0.000E+00	4.959E-03	0.000E+00	0.000E+00
9	0.396	6.819E-03	0.000E+00	0.000E+00	0.000E+00	6.819E-03	0.000E+00	0.000E+00
10	0.450	3.170E-03	0.000E+00	0.000E+00	0.000E+00	3.170E-03	0.000E+00	0.000E+00
11	0.708	3.855E-02	1.399E-04	1.074E-03	2.428E-03	3.512E-03	3.753E-03	2.993E-03
12	1.224	6.000E-02	1.913E-04	1.485E-03	3.434E-03	5.136E-03	5.738E-03	4.836E-03
13	1.739	6.935E-02	1.935E-04	1.516E-03	3.570E-03	5.491E-03	6.367E-03	5.621E-03
14	2.255	7.741E-02	1.937E-04	1.530E-03	3.661E-03	5.766E-03	6.900E-03	6.337E-03

.....  
 Emitted flux per excitation energy bin of Z= 41 N= 53 ( 94Nb):

bin	Ex	gamma	neutron	proton	deuteron	triton	helium
0	0.000	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
1	0.041	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
2	0.059	2.35107E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
3	0.079	1.46791E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
4	0.113	1.34195E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
5	0.140	2.69549E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
6	0.302	6.23859E-02	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00

.....  
 Emission cross sections to residual nuclei from Z= 41 N= 53 ( 94Nb):

```

gamma    channel to Z= 41 N= 53 ( 94Nb): 2.98091E+00
neutron  channel to Z= 41 N= 52 ( 93Nb): 1.64203E+00
proton   channel to Z= 40 N= 53 ( 93Zr): 2.93129E-03
deuteron channel to Z= 40 N= 52 ( 92Zr): 8.05241E-06
triton   channel to Z= 40 N= 51 ( 91Zr): 1.66602E-07
helium-3 channel to Z= 39 N= 52 ( 91Y ): 1.80790E-16
alpha    channel to Z= 39 N= 51 ( 90Y ): 2.01113E-03

```

Emission spectra from Z= 41 N= 53 ( 94Nb):

Energy	gamma	neutron	proton	deuteron	triton	helium-3
0.001	1.24453E-02	7.51987E-03	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.002	1.29187E-02	1.58766E-02	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.005	1.43370E-02	4.50036E-02	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.010	1.67009E-02	1.00411E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.020	2.14289E-02	1.87646E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00
0.050	4.49740E-02	3.44875E-01	0.00000E+00	0.00000E+00	0.00000E+00	0.00000E+00

.....  
+++++++ CHECK OF INTEGRATED EMISSION SPECTRA ++++++

	Cross section	Integrated spectrum	Average emission energy
gamma	2.98091E+00	2.98091E+00	1.824
neutron	1.64203E+00	1.64203E+00	1.233
proton	2.93129E-03	2.93113E-03	5.368
deuteron	8.05241E-06	7.88908E-06	5.077
triton	1.66602E-07	1.27887E-07	5.153
helium-3	1.80790E-16	0.00000E+00	0.000
alpha	2.01113E-03	2.01092E-03	10.719

Final production cross section of Z= 41 N= 53 ( 94Nb):

```

Total      : 1.32555E+00
Ground state: 6.47368E-01
Level 1    : 6.78179E-01

```

Note that once a new nucleus is encountered in the reaction chain, all nuclear structure information for that nucleus is printed as well.

### Case 1i: No output at all

It is even possible to have an empty output file. With the following input file,

```

#
# General
#
projectile n
element nb

```

```

mass 93
energy 14.
#
# Output
#
outmain n

```

it is specified that even the main output should be suppressed. The sample output file should be empty. This can be helpful when TALYS is invoked as a subroutine from other programs and the output from TALYS is not required (if the communication is done e.g. through shared arrays or subroutine variables). We have not yet used this option ourselves.

### 8.3.2 Sample 2: Excitation functions: $^{208}\text{Pb}$ (n,n'), (n,2n), (n,p) etc.

Often we are not interested in only one incident energy, but in excitation functions of the cross sections. If more than one incident energy is given in the file specified by the **energy** keyword, it is helpful to have the results, for each type of cross section, in a table as a function of incident energy. TALYS will first calculate all quantities that remain equal for all incident energy calculations, such as the transmission coefficients. Next, it will calculate the results for each incident energy. When the calculation for the last incident energy has been completed, the cross sections are collected and printed as excitation functions in the output if **outexcitation y** (which is the default if there is more than one incident energy). Moreover, we can provide the results in separate files: one file per reaction channel. Consider the following input file

```

#
# General
#
projectile n
element pb
mass 208
energy energies
#
# Parameters
#
gnorm 0.35
Rgamma 2.2
egr      82 209 12.0    E1 1
optmodfileN 82 pb.omp
#
# Output
#
channels y
filechannels y
filetotal y
fileresidual y
outdiscrete y

```

which provides all partial cross sections for neutrons incident on  $^{208}\text{Pb}$  for 46 incident energies, from 1 to 30 MeV, as given in the file *energies* that is present in this sample case directory. In the main output file, first the results per incident energy are given. At the end of the output file, there is an output block that begins with:

```
##### EXCITATION FUNCTIONS #####
```

The first table contains the most important total cross sections as a function of incident energy. This output block begins with:

```
##### EXCITATION FUNCTIONS #####
```

1. Total (binary) cross sections

Energy	Non-elastic	Elastic	Total	Comp. el.	Shape el.	Reaction	C
1.000E+00	5.4272E-01	4.8368E+03	4.8373E+03	1.7271E+03	3.1097E+03	1.7276E+03	5
1.200E+00	5.8887E-01	4.7813E+03	4.7819E+03	1.8194E+03	2.9619E+03	1.8200E+03	5
1.400E+00	6.4905E-01	4.9407E+03	4.9413E+03	1.9485E+03	2.9922E+03	1.9491E+03	6
1.600E+00	7.1533E-01	5.2462E+03	5.2470E+03	2.1038E+03	3.1424E+03	2.1045E+03	7
.....							

Next, the binary cross sections are printed. This output block begins with:

2. Binary non-elastic cross sections (non-exclusive)

Energy	gamma	neutron	proton	deuteron	triton	helium-3	
1.000E+00	1.9342E-01	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0
1.200E+00	2.3098E-01	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0
1.400E+00	2.7967E-01	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0
1.600E+00	3.3915E-01	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0
1.800E+00	4.1420E-01	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0.0000E+00	0
.....							

Next, the total particle production cross sections are printed. Parts of this output block look as follows:

3. Total particle production cross sections

gamma production

Energy	Cross section	Multiplicity
1.000E+00	2.41342E-01	1.39698E-04
1.200E+00	2.91629E-01	1.60236E-04
1.400E+00	3.57803E-01	1.83573E-04
1.600E+00	4.36437E-01	2.07383E-04
1.800E+00	5.35885E-01	2.36490E-04

```

2.000E+00 6.61168E-01 2.74127E-04
2.200E+00 8.15172E-01 3.22521E-04
.....
neutron production

Energy   Cross section Multiplicity

1.000E+00 4.34770E-03 2.51661E-06
1.200E+00 8.76553E-03 4.81623E-06
1.400E+00 1.53472E-02 7.87397E-06
1.600E+00 2.68953E-02 1.27799E-05
1.800E+00 4.29934E-02 1.89733E-05
2.000E+00 6.64016E-02 2.75308E-05
2.200E+00 9.98008E-02 3.94860E-05
2.400E+00 1.46869E-01 5.62891E-05
2.600E+00 2.07893E-01 7.81346E-05
2.800E+00 3.17467E+02 1.18048E-01
3.000E+00 5.15453E+02 1.90753E-01
3.200E+00 6.64864E+02 2.45700E-01
3.400E+00 8.75252E+02 3.23472E-01
3.600E+00 1.07209E+03 3.96308E-01
.....

```

Next in the output are the residual production cross sections. The output block begins with:

```

4. Residual production cross sections

Production of Z= 82 A=209 (209Pb) - Total

Q-value      =    3.936466
E-threshold=    0.000000

Energy   Cross section

1.000E+00 1.89063E-01
1.200E+00 2.22219E-01
1.400E+00 2.64322E-01
1.600E+00 3.12258E-01
1.800E+00 3.71203E-01
2.000E+00 4.42357E-01
2.200E+00 5.26132E-01
2.400E+00 6.25592E-01
2.600E+00 7.49680E-01
.....

```

and the remaining isotopes follow in decreasing order of mass and isotope.

The final part of the output, for this input file at least, concerns the exclusive reaction cross sections. This output block begins with:

## 6. Exclusive cross sections

Emitted particles						reaction
n	p	d	t	h	a	
0	0	0	0	0	0	(n,g)

Q-value = 3.936466  
E-threshold= 0.000000

Energy	Cross section	Gamma c.s.	c.s./res.prod.cs
1.000E+00	1.89063E-01	3.41681E-01	1.00000E+00
1.200E+00	2.22219E-01	4.03184E-01	1.00000E+00
1.400E+00	2.64322E-01	4.85242E-01	1.00000E+00
1.600E+00	3.12258E-01	5.77348E-01	1.00000E+00
1.800E+00	3.71203E-01	6.93799E-01	1.00000E+00
2.000E+00	4.42358E-01	8.37267E-01	1.00000E+00

.....

Emitted particles						reaction
n	p	d	t	h	a	
1	1	0	0	0	0	(n,np)

Q-value = -8.008137  
E-threshold= 8.046975

Energy	Cross section	Gamma c.s.	c.s./res.prod.cs
1.000E+00	0.00000E+00	0.00000E+00	0.00000E+00
1.200E+00	0.00000E+00	0.00000E+00	0.00000E+00
1.400E+00	0.00000E+00	0.00000E+00	0.00000E+00
1.600E+00	0.00000E+00	0.00000E+00	0.00000E+00
1.800E+00	0.00000E+00	0.00000E+00	0.00000E+00
2.000E+00	0.00000E+00	0.00000E+00	0.00000E+00
2.200E+00	0.00000E+00	0.00000E+00	0.00000E+00

.....

1.700E+01	2.18732E-01	8.37571E-02	7.04946E-02
1.800E+01	6.27584E-01	2.50876E-01	1.26002E-01
1.900E+01	1.46792E+00	6.36370E-01	1.99162E-01
2.000E+01	2.81092E+00	1.36675E+00	2.72657E-01
2.200E+01	7.94558E+00	5.58661E+00	4.35632E-01
2.400E+01	1.60863E+01	1.58609E+01	5.76845E-01
2.600E+01	2.60132E+01	3.37742E+01	6.76278E-01
2.800E+01	3.55149E+01	5.52658E+01	7.37553E-01
3.000E+01	4.31937E+01	7.50611E+01	7.77056E-01

For plotting data, or processing into ENDF-6 data files, it is more practical to have the data in individual output files. Note that, since **filechannels y**, several files with names as e.g. *xs200000.tot* have been created in your working directory. These files contain the entire excitation function per reaction channel.

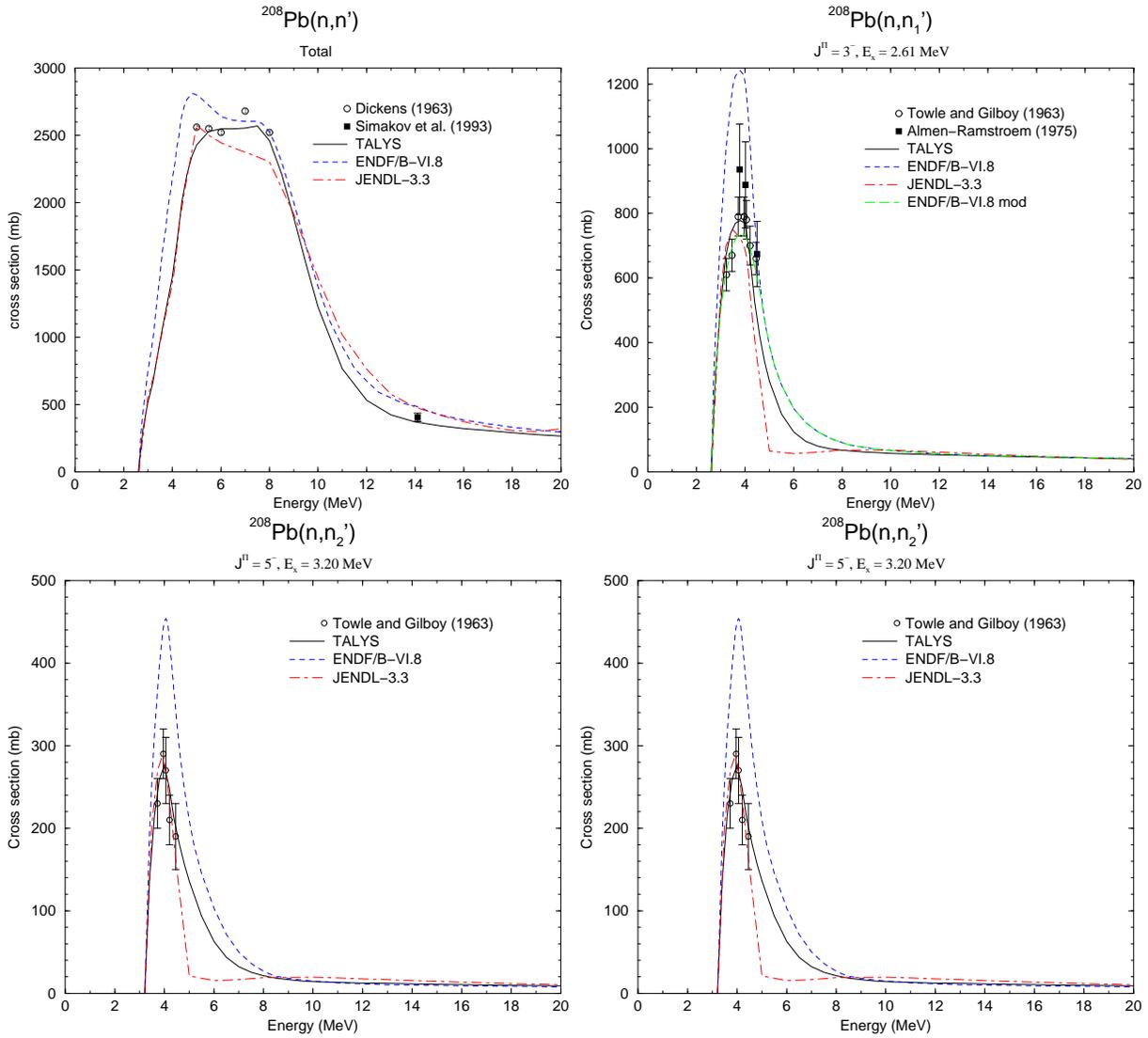
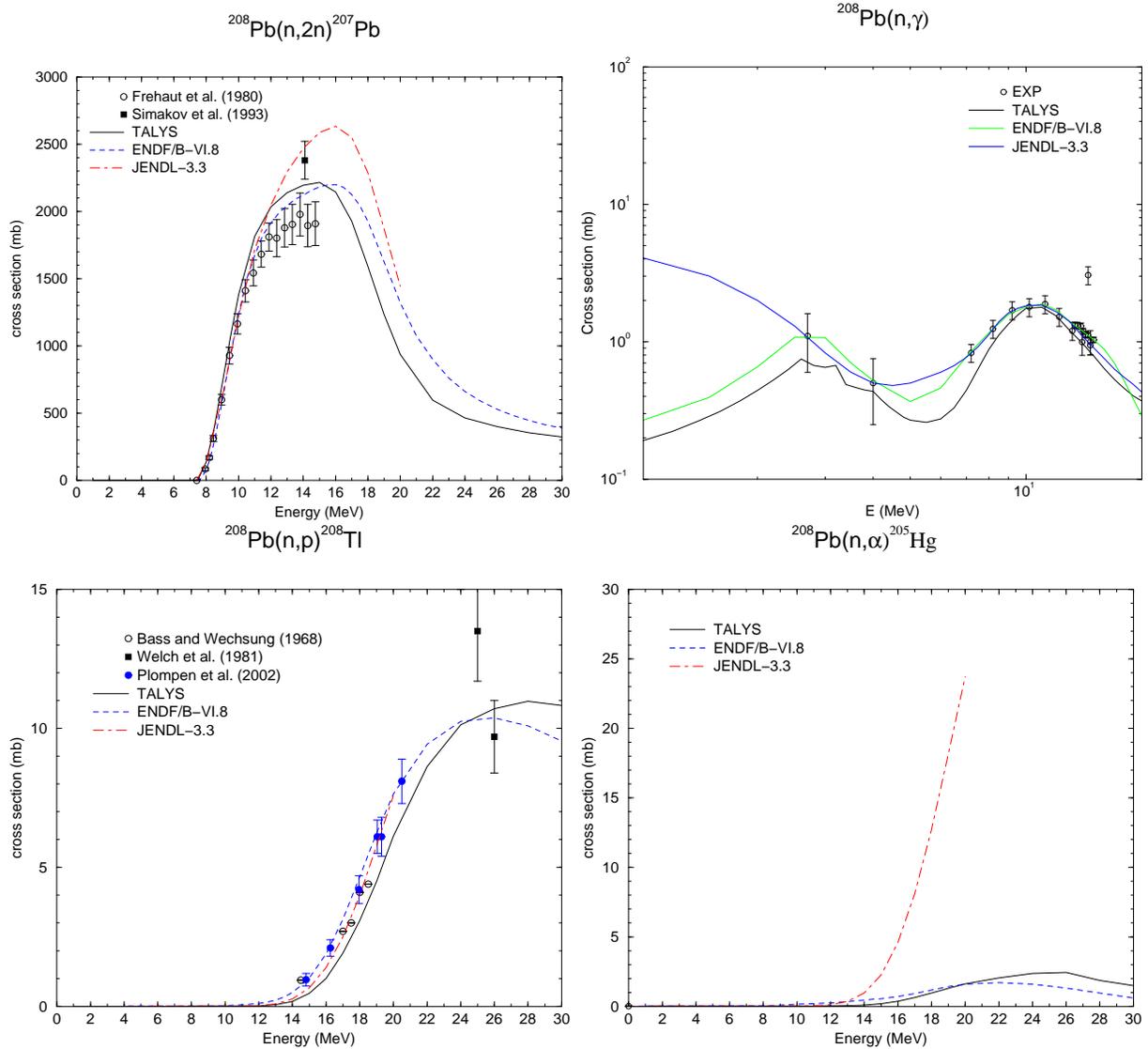


Figure 8.1: Partial cross sections for neutrons incident on  $^{208}\text{Pb}$ .

Figure 8.2: Partial cross sections for neutrons incident on  $^{208}\text{Pb}$ .

Besides these exclusive cross sections, residual production cross section files are produced (**fileresidual y**). Note that for this reaction, *rp082207.tot* and *xs200000.tot* obviously have equal contents.

We illustrate this sample case with various comparisons with measurements. Since **filetotal y**, a file *total.tot* is created with, among others, the total cross section. The resulting curves are shown in Figs. 8.1 and 8.2.

### 8.3.3 Sample 3: Comparison of compound nucleus WFC models: 10 keV n + <sup>93</sup>Nb

In this sample case, we demonstrate the difference between the various models for the width fluctuation correction in compound nucleus reactions, as discussed extensively in Ref. [6]. As sample case, we take 10 keV neutrons incident on <sup>93</sup>Nb and we ask for various compound nucleus models to calculate cross sections and angular distributions (**outangle y**), and to put the result for the elastic scattering angular distribution on a separate file, called *nn000.010ang.L00*. Since the GOE calculation (**widthmode 3**) is rather time-consuming, we reduce the number of bins to 20 for all cases. We wish to check whether the flux is conserved in the compound nucleus model for the various WFC models, so we set **outcheck y**. This means that for each set of quantum numbers, unitarity is checked by means of Eq. (4.149).

#### Case 3a: Hauser-Feshbach model

The following input file is used

```
#
# General
#
projectile n
element nb
mass 93
energy 0.01
#
# Parameters
#
bins 20
widthmode 0
#
# Output
#
outcheck y
outangle y
fileelastic y
```

This only new output block, i.e. not discussed before, is

```
+++++++ CHECK OF FLUX CONSERVATION OF TRANSMISSION COEFFICIENTS: Hauser-Feshb

Parity=- J= 3.0 j= 1.5 l= 1 T(j,l)= 7.98693E-03 Sum over outgoing channels=
Parity=- J= 4.0 j= 0.5 l= 1 T(j,l)= 4.54029E-03 Sum over outgoing channels=
Parity=- J= 4.0 j= 1.5 l= 1 T(j,l)= 7.98693E-03 Sum over outgoing channels=
```

Model	$\sigma^{comp-el}$
Hauser-Feshbach	2456.19 mb
Moldauer	2648.39 mb
HRTW	2773.34 mb
GOE	2648.30 mb

Table 8.2: Compound elastic cross section for 4 different compound nucleus models for 10 keV neutrons incident on  $^{93}\text{Nb}$ .

```

Parity=- J= 5.0  j= 0.5  l= 1  T(j,l)= 4.54029E-03  Sum over outgoing channels=
Parity=- J= 5.0  j= 1.5  l= 1  T(j,l)= 7.98693E-03  Sum over outgoing channels=
Parity=- J= 6.0  j= 1.5  l= 1  T(j,l)= 7.98693E-03  Sum over outgoing channels=
Parity=+ J= 2.0  j= 2.5  l= 2  T(j,l)= 1.02314E-06  Sum over outgoing channels=
.....

```

in which the aforementioned unitarity is checked.

### Case 3b: Moldauer model

As for case a, but now with **widthmode 1** in the input file.

### Case 3c: HRTW model

As for case a, but now with **widthmode 2** in the input file.

### Case 3d: GOE model

As for case a, but now with **widthmode 3** in the input file.

Table 8.2 lists the obtained compound nucleus elastic cross section for the 4 cases.

Fig. 8.3 displays the elastic angular distribution for the 4 models. Results like these made us conclude in Ref. [6] that Moldauer's model, which is closest to the exact GOE result, is the one to use in practical applications, especially when considering the calculation times as printed in Table 8.1. Obviously, this sample case can be extended to one with various incident energies, so that the differences between excitation functions can be studied, see also Ref. [6].

## 8.3.4 Sample 4: Recoils: 20 MeV n + $^{28}\text{Si}$

In this sample case, we calculate the recoils of the residual nuclides produced by 20 MeV neutrons incident on  $^{28}\text{Si}$  reaction. Two methods are compared.

### Case 4a: "Exact" approach

In the exact approach, each excitation energy bin of the population of each residual nucleus is described by a full distribution of kinetic recoil energies. The following input file is used

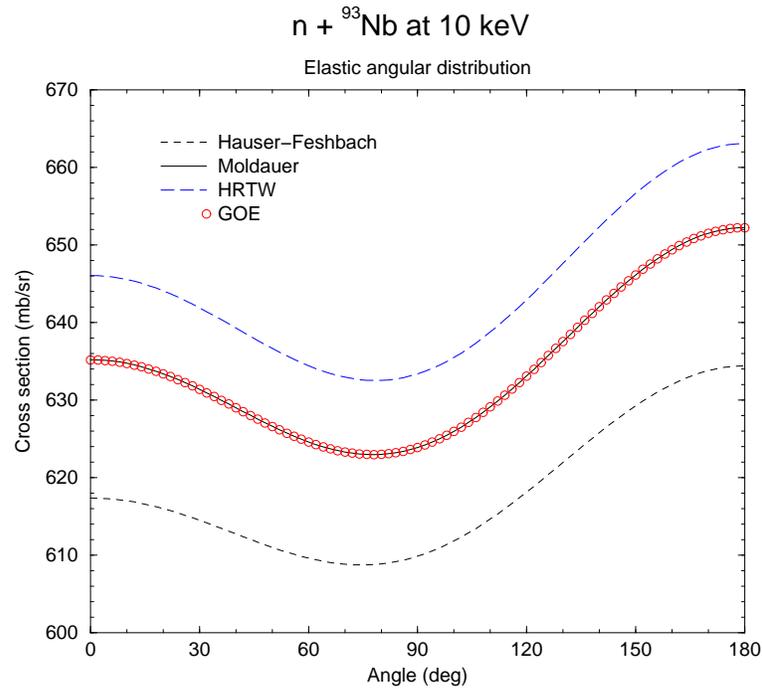


Figure 8.3: Total elastic angular distribution for 4 different compound nucleus models for 10 keV neutrons incident on  ${}^{93}\text{Nb}$ .

```
#
# General
#
projectile n
element si
mass 28
energy 20.
#
# Parameters
#
m2constant 0.70
sysreaction p d t h a
spherical y
#
# Output
#
recoil y
filerecoil y
```

For increasing incident energies, this calculation becomes quickly time-expensive. The recoil calculation yields separate files with the recoil spectrum per residual nucleus, starting with *rec*, followed by the Z, A and incident energy, e.g. *rec012024spec020.000.tot*. Also following additional output block is printed:

```
8. Recoil spectra
```

Recoil Spectrum for 29Si

Energy    Cross section

```

0.018 0.00000E+00
0.053 0.00000E+00
0.088 0.00000E+00
0.123 0.00000E+00
0.159 0.00000E+00
0.194 0.00000E+00
0.229 0.00000E+00
0.264 0.00000E+00

```

.....

```

0.723 2.53636E+00
0.758 2.53143E+00
0.793 2.52279E+00
0.829 2.32172E+00
0.864 1.76032E+00
0.899 1.44210E-01

```

Integrated recoil spectrum           : 8.23371E-01

Residual production cross section: 7.99754E-01

#### Case 4b: Approximative approach

As an approximation, each excitation energy bin of the population of each residual nucleus is described by a an average kinetic recoil energy. For this, we add one line to the input file above,

```
recoilaverage y
```

The results, together with those of case (a), are compared in Fig. 8.4.

### 8.3.5 Sample 5: Fission cross sections: n + <sup>239</sup>Pu

A systematic approach for fission is still lacking. It is possible to obtain very satisfactory fits to fission data with TALYS, but at the expense of using many adjustable input parameters. At the time of this writing, we are performing extensive model calculations to bring somewhat more structure in the collection of fitting parameters. In the meantime, we include a sample case for the description of the fission cross section. We use the following input file,

```

#
# General
#
projectile n
element pu
mass 239
energy energies
#
# Models and output

```

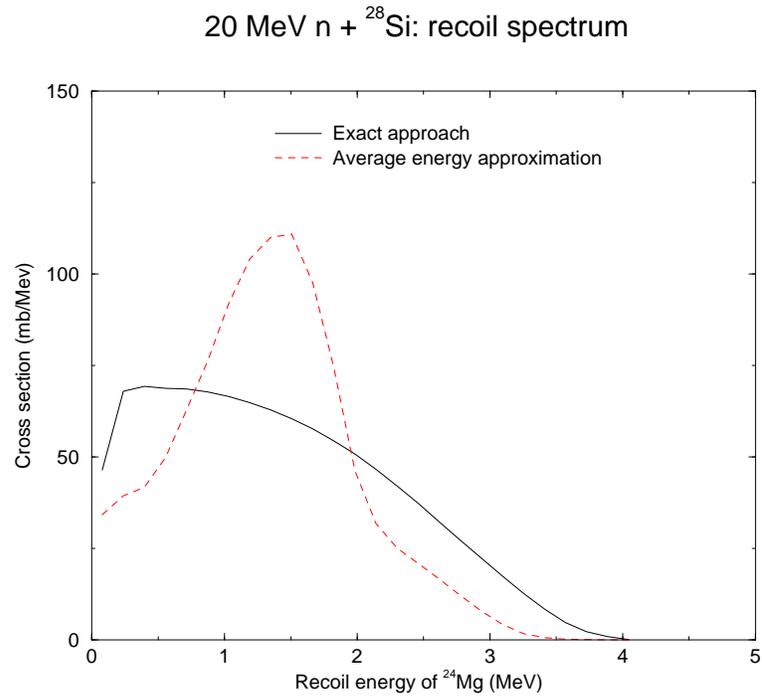


Figure 8.4: Recoil energy distribution of  $^{24}\text{Mg}$  for 20 MeV n +  $^{28}\text{Si}$  according to the exact and approximate approach.

```
#
ejectiles g n
optmod 94 239 z094a239n.omp n
class2 y
ldmodel 1
fismodel 1
maxrot 4
bins 30
partable y
outfission y
filefission y
#
# Parameters
#
fisbar 94 240 5.86598 1
fishw 94 240 0.75442 1
fisbar 94 240 5.79983 2
fishw 94 240 0.64346 2
a 94 240 30.85535
gammald 94 240 0.08051
pair 94 240 1.44454
deltaW 94 240 1.92382 0
Ntop 94 240 23 0
```

```

krotconstant  94 240    1.65051  0
deltaW       94 240    2.13515  1
Ntop        94 240    31  1
krotconstant  94 240    0.83718  1
deltaW       94 240    0.98397  2
Ntop        94 240    16  2
krotconstant  94 240    1.77575  2
class2width  94 240    0.18575  1
rtransmom   94 240    0.42452  1
rclass2mom  94 240    1.00692  1
rtransmom   94 240    1.29815  2
rclass2mom  94 240    2.28954  2
fisbar      94 239    5.63731  1
fishw       94 239    0.69663  1
fisbar      94 239    5.77552  2
fishw       94 239    0.60689  2
a           94 238    28.15777
m2constant  1.20344
a           94 239    27.97096
fisbar      94 238    6.15134  1
fishw       94 238    1.01618  1
fisbar      94 238    5.53253  2
fishw       94 238    0.78091  2
ufermi      40.31846
cfermi      11.96158
ufermibf    42.42088
cfermibf    24.29564

```

which has been obtained from an automated fitting procedure, and does not yet contain the optimal result. The optical model file *z094239.omp* contains the parameters of a recent global deformed OMP by Soukhovitskii et al.[113]. The keyword **filefission y** ensures that the total fission cross section appear in the file *fission.tot*, and this is plotted together with experimental data in Fig. 8.5.

Due to the presence of **outfission y** in the input file, all nuclear structure related to the fission process is given in the output for the target and the compound nucleus

Fission information for Z= 94 N=145 (239Pu)

```

Number of fission barriers      :  2
Number of sets of class2 states :  1

```

Parameters for fission barrier 1

```

Type of axiality                :  2 (tri-axial)
Height of fission barrier 1     :  5.637
Width of fission barrier 1     :  0.697
Rtransmom                       :  0.600
Moment of inertia               :  99.087
Number of head band transition states:  4
Start of continuum energy      :  0.080

```

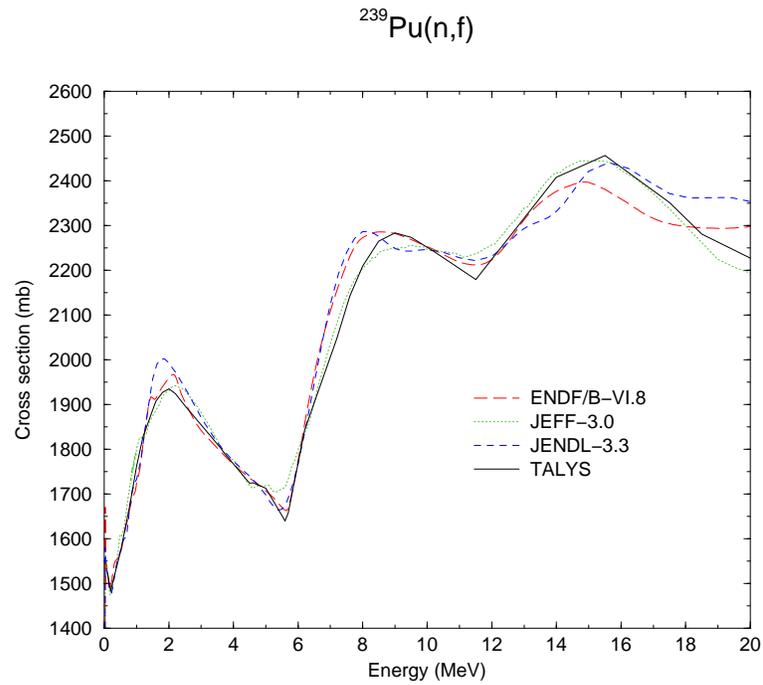


Figure 8.5: Neutron induced fission cross section of  $^{239}\text{Pu}$  compared with some major nuclear data libraries.

#### Head band transition states

no.	E	spin	parity
1	0.000	0.5	+
2	0.080	2.5	+
3	0.050	0.5	-
4	0.000	1.5	-

#### Rotational bands

no.	E	spin	parity
1	0.000	0.5	+
2	0.000	1.5	-
3	0.015	1.5	+
4	0.025	2.5	-
5	0.040	2.5	+
6	0.050	0.5	-
7	0.061	3.5	-
8	0.065	1.5	-
9	0.076	3.5	+
10	0.080	2.5	+

Parameters for fission barrier 2

.....

Parameters for set 1 of class2 states

Rclass2mom : 1.000  
 Moment of inertia : 165.145  
 Number of class2 states : 10  
 Width of class2 states (MeV) : 0.200

Class 2 states

no.	E	spin	parity
1	2.600	0.5	+
2	3.100	2.5	+
3	3.300	4.5	-
4	3.800	2.5	-
5	4.200	5.5	+
6	4.500	0.5	+
7	4.800	3.5	+
8	5.200	2.5	+
9	5.500	1.5	-
10	5.600	3.5	+

Rotational bands

no.	E	spin	parity
1	2.600	0.5	+
2	2.609	1.5	+
3	2.624	2.5	+
4	2.645	3.5	+
5	2.673	4.5	+
6	2.706	5.5	+
7	2.745	6.5	+
8	2.791	7.5	+
9	2.842	8.5	+
10	2.900	9.5	+
11	2.963	10.5	+
12	3.033	11.5	+
13	3.100	2.5	+
14	3.109	12.5	+
15	3.121	3.5	+

.....

Moreover, the corresponding fission transmission coefficients are printed for all excitation energies encountered in the calculation

Fission transmission coefficients for  $Z=94$   $N=146$  ( $^{240}\text{Pu}$ ) and an excitation energy of

J	T(J,-)	T(J,+)
0.0	1.01559E-01	7.60491E-01
1.0	1.25751E+00	2.91318E-01
2.0	6.98388E-01	1.61488E+00
3.0	1.38738E+00	8.33594E-01
4.0	9.20465E-01	1.43045E+00
5.0	1.41139E+00	8.89080E-01
6.0	0.00000E+00	0.00000E+00
7.0	0.00000E+00	0.00000E+00
8.0	0.00000E+00	0.00000E+00
9.0	0.00000E+00	0.00000E+00
10.0	0.00000E+00	0.00000E+00
11.0	0.00000E+00	0.00000E+00
12.0	0.00000E+00	0.00000E+00
.....		

The fission information for all residual nuclides can be obtained in the output file as well by adding *outpopulation y* to the input file.

### 8.3.6 Sample 6: Continuum spectra at 63 MeV for $\text{Bi}(n,\text{xp})\dots\text{Bi}(n,\text{x}\alpha)$

In this sample case, we calculate angle-integrated and double-differential particle spectra for 63 MeV neutrons on  $^{209}\text{Bi}$ , see Ref. [25].

#### Case 6a: Default calculation

The following input file is used

```
#
# General
#
projectile n
element bi
mass 209
energy 63.
#
# Output
#
ddxmode 2
filespectrum n p d t h a
fileddxa p 20.
fileddxa p 70.
fileddxa p 110.
```

```

fileddxa d 20.
fileddxa d 70.
fileddxa d 110.
fileddxa t 20.
fileddxa t 70.
fileddxa t 110.
fileddxa h 20.
fileddxa h 70.
fileddxa h 110.
fileddxa a 20.
fileddxa a 70.
fileddxa a 110.

```

Note that we request that angle-integrated spectra for all particles are written on separate files through *filespectrum n p d t h a*. At 20, 70 and 110 degrees, we also ask for the double-differential spectrum for protons up to alpha-particles. The resulting files *pspec063.000.tot*, *pddx020.0.deg*, etc. are presented, together with experimental data, in Figs. 8.6 and 8.7.

#### Case 6b: Adjusted matrix element

The default results of case (a) for the proton spectra are a bit high. Therefore, as a second version of this sample case, we adjust a pre-equilibrium parameter and add the following to the input above:

```

#
# Parameters
#
M2constant 1.30

```

By increasing **M2constant** by 30% (which is a common and acceptable deviation from the average), we favor the pre-equilibrium damping rate over the emission rate, leading to a softer spectrum. The result is shown in Fig. 8.6 for the proton spectrum.

### 8.3.7 Sample 7: Pre-equilibrium angular dist. and multiple pre-equilibrium emission

At high incident energies, multiple pre-equilibrium reactions play a significant role. In this sample case, we show the results for this mechanism in the output file. Also, as an alternative to the previous sample case, we present another way of producing double-differential cross sections, namely as a function of angle at a fixed outgoing energy. With the following input file, the reaction of 120 MeV protons incident on  $^{90}\text{Zr}$  is simulated:

```

#
# General
#
projectile p
element zr
mass 90
energy 120.

```

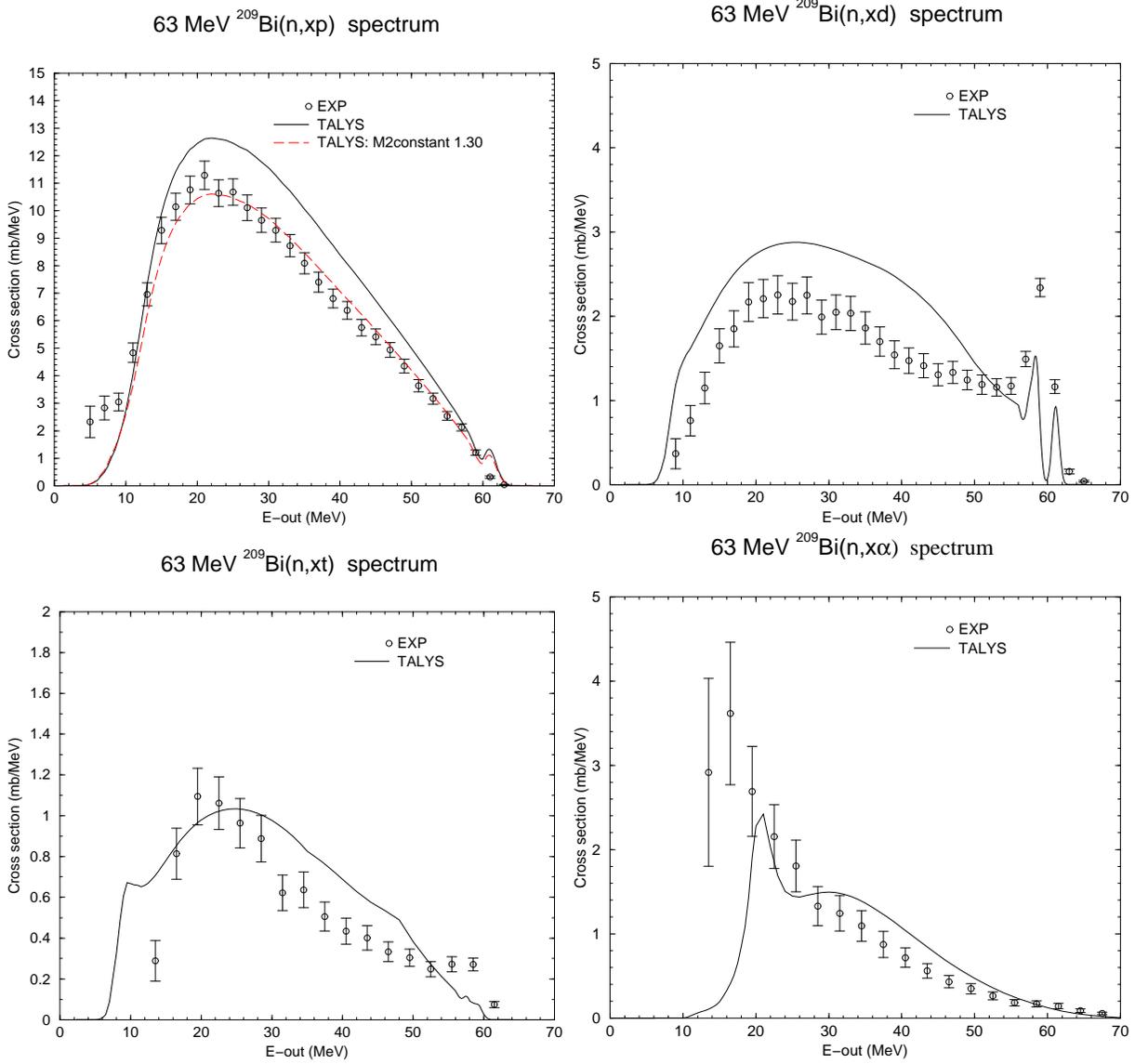


Figure 8.6: Angle-integrated proton, deuteron, triton and alpha emission spectra for 63 MeV neutrons on  $^{209}\text{Bi}$ . The experimental data are from [25].

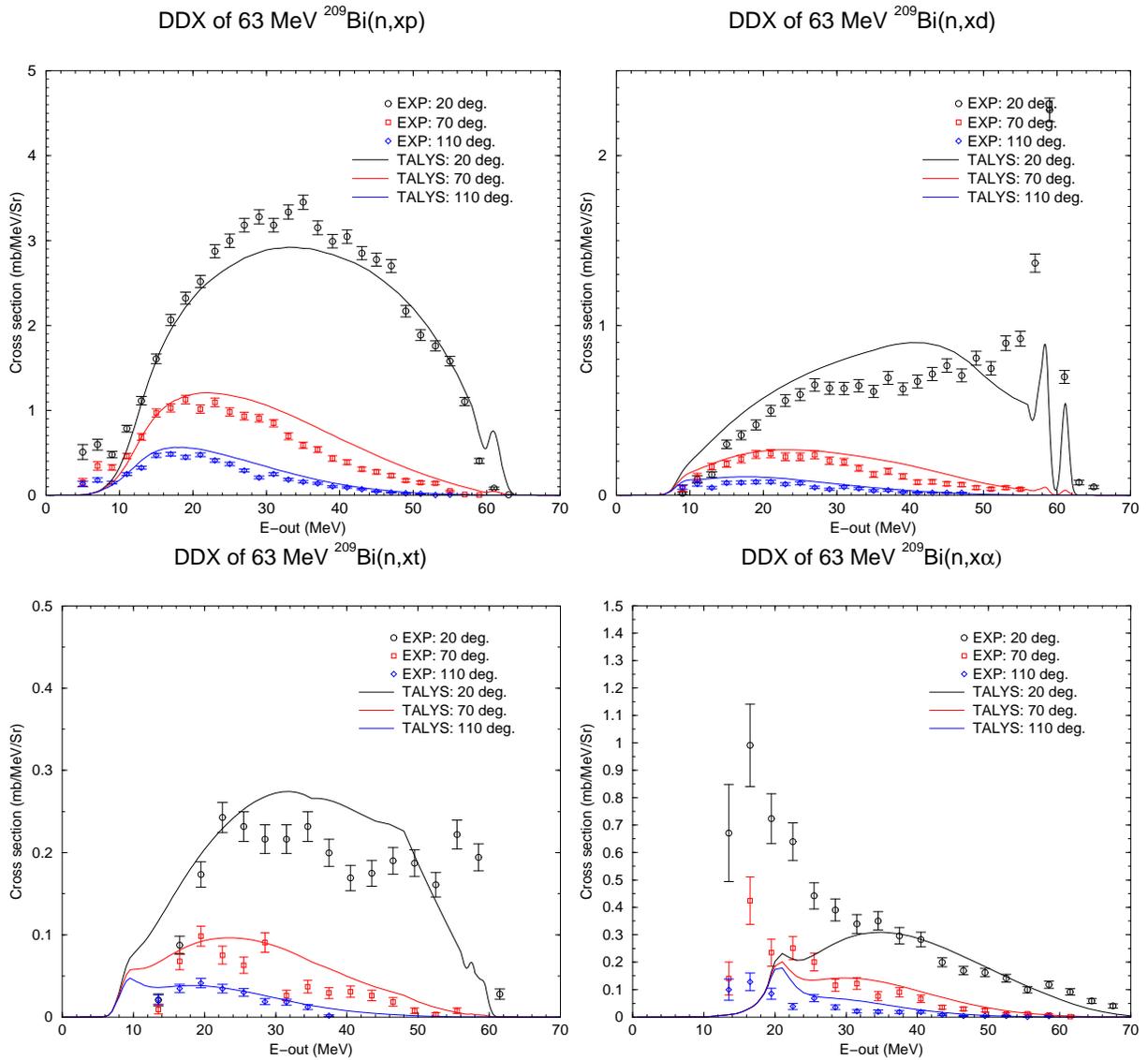


Figure 8.7: Double-differential proton, deuteron, triton and alpha emission spectra for 63 MeV neutrons on  $^{209}\text{Bi}$ . The experimental data are from [25].



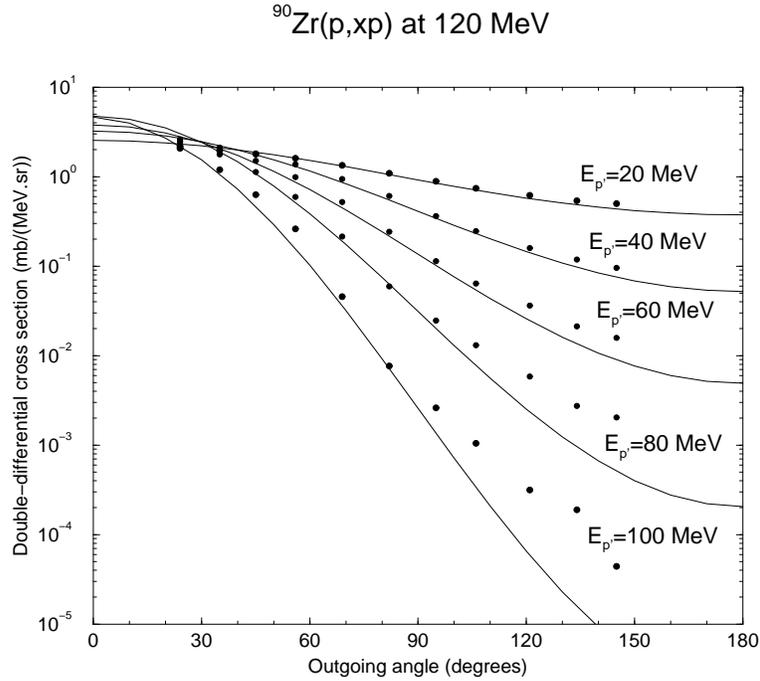


Figure 8.9: Double-differential (p,xp) spectra for 120 MeV protons on  $^{90}\text{Zr}$ . Experimental data are taken from [107]

12	4.980	0.00000	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	1.366E+00	0.000E+00
13	7.752	0.00000	0.000E+00	0.000E+00	0.000E+00	0.000E+00	0.000E+00	2.143E+00	0.000E+00
14	10.524	0.00001	0.000E+00	4.260E-05	0.000E+00	0.000E+00	0.000E+00	2.891E+00	0.000E+00
15	13.296	0.00535	0.000E+00	1.976E-02	0.000E+00	0.000E+00	0.000E+00	3.607E+00	0.000E+00
16	16.067	0.04738	3.113E-03	2.058E-01	0.000E+00	0.000E+00	0.000E+00	4.293E+00	0.000E+00
17	18.839	0.10588	2.567E-02	5.157E-01	0.000E+00	0.000E+00	0.000E+00	4.948E+00	0.000E+00
18	21.611	0.17182	6.235E-02	9.350E-01	0.000E+00	0.000E+00	0.000E+00	5.572E+00	0.000E+00
19	24.383	0.23120	1.153E-01	1.383E+00	0.000E+00	0.000E+00	0.000E+00	6.160E+00	0.000E+00
.....									

For each continuum bin, with excitation energy  $E_x$ , we print the fraction of the population that is emitted as multiple pre-equilibrium. Also the total neutron and proton emission per residual nucleus is printed, as well as the feeding terms from previous particle-hole configurations. With this input file, files *nspec120.000.tot* and *pspec120.000.tot* are created through the *filespectrum n p* keyword. The results are displayed in Fig. 8.8. Also, the combination of **ddxmode 1** and the various **fileddxe** keywords generate the *pddx100.0.mev*, etc. files that are compared with experimental data in Fig. 8.9.

### 8.3.8 Sample 8: Residual production cross sections: p + $^{nat}\text{Fe}$ up to 100 MeV

In this sample case, we calculate the residual production cross sections for protons on  $^{nat}\text{Fe}$  for incident energies up to 100 MeV. A calculation for a natural target is launched, meaning that successive TALYS calculations for each isotope are performed, after which the results are weighted with the natural abundance. We restrict ourselves to a calculation with all nuclear model parameters set to their default values.

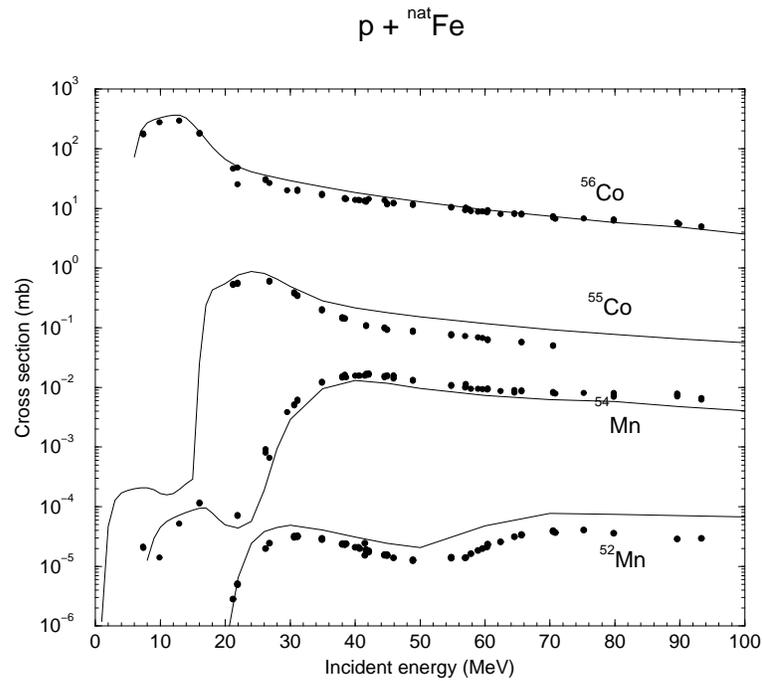


Figure 8.10: Residual production cross sections for protons incident on  ${}^{\text{nat}}\text{Fe}$ . Experimental data are obtained from [109].

The following input file is used:

```
#
# General
#
projectile p
element fe
mass 0
energy energies
#
# Output
#
fileresidual      y
```

The file *energies* contains 34 incident energies between 1 and 100 MeV. Obviously, this sample case can be extended to more incident energies, e.g. up to 200 MeV, by simply adding numbers to the *energies* file. In that case, we recommend to include more energy bins in the calculation, (e.g. **bins 80**) to avoid numerical fluctuations, although this will inevitably take more computer time. Note that we have enabled the **fileresidual** keyword, so that a separate cross sections file for each final product is produced. The results from the files *rp027056.tot*, *rp027055.tot*, *rp025054.tot* and *rp025052.tot* are presented, together with experimental data, in Fig. 8.10.

### 8.3.9 Sample 9: Spherical optical model and DWBA: $n + {}^{208}\text{Pb}$

Three types of optical model calculations are included in the set of sample cases. In this first one, we treat  ${}^{208}\text{Pb}$  as a spherical nucleus and request calculations for the elastic angular distributions and inelastic angular distributions at a few incident energies. This is accomplished with the input file

```
#
# General
#
projectile n
element pb
mass 208
energy energies
#
# Avoid unnecessary calculations and output
#
ejectiles n
preequilibrium n
compound n
maxZ 0
maxN 0
bins 5
fileresidual n
filetotal n
#
# Output
#
outangle y
fileelastic y
fileangle 1
fileangle 2
```

where the file *energies* consists of the energies 11., 13.7, 20., 22., and 25.7 MeV (for which experimental data exists). The keyword *fileelastic y* has created the files *nn011.000ang.L00*, etc. which contain the elastic scattering angular distribution and are compared with experimental data in Fig. 8.11. With **fileangle 1** and **fileangle 2** we have created the files *nn010.000ang.L01*, etc. with the inelastic scattering angular distribution to the first and second discrete state. These are also plotted in Figs. 8.11. Note that the keywords in the middle block (**ejectiles n** up to **filetotal n**) have been added to avoid a full calculation of all the cross sections. For the present sample case we assume that only elastic scattering and DWBA angular distributions are of interest, so we economize on output options, number of bins, ejectiles and nuclides that can be reached. Obviously, for reliable results for all observables this middle block would have to be deleted. See also sample case (1f) for obtaining more specific information from the output.

### 8.3.10 Sample 10: Coupled-channels rotational model: $n + {}^{28}\text{Si}$

In this sample case, we consider spherical OMP and rotational coupled-channels calculations for the deformed nucleus  ${}^{28}\text{Si}$ .

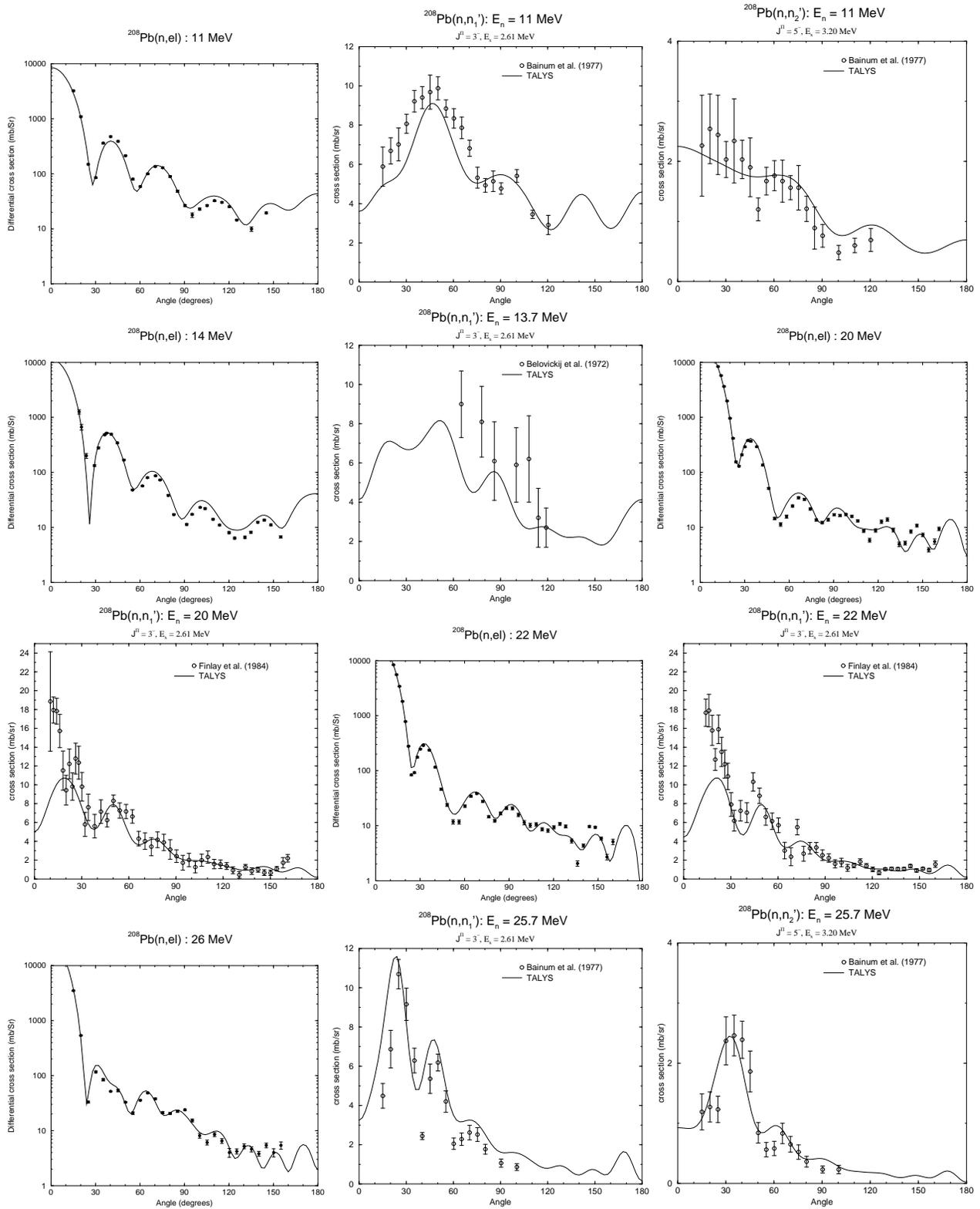


Figure 8.11: Elastic and inelastic scattering angular distributions between 11 and 26 MeV for  $^{208}\text{Pb}$ .

**Case 10a: Spherical optical model**

In the first case, we treat  $^{28}\text{Si}$  as a spherical nucleus and include the first ( $2^+$ ), second ( $4^+$ ) and sixth ( $3^-$ ) level as weakly coupled levels, i.e. the cross sections are calculated with DWBA. The input file is

```
#
# General
#
projectile n
element si
mass 28
energy energies
#
# Parameters
#
spherical y
#
# Output
#
channels y
filechannels y
```

For the default calculation, TALYS will look in the *deformation/exp* database to see whether a coupling scheme is given. Since this is the case for  $^{28}\text{Si}$ , we have to put **spherical y** to enforce a spherical calculation.

**Case 10b: Symmetric rotational model**

In the second case, we include the first and second level of the ground state rotational band and the  $3^-$  state in the coupling scheme. This is accomplished with the input file

```
#
# General
#
projectile n
element si
mass 28
energy energies
#
# Output
#
channels y
filechannels y
```

In Fig. 8.12, the calculated total inelastic scattering for cases a and b are plotted.

**8.3.11 Sample 11: Coupled-channels vibrational model: n + Ge-74**

In this sample case we consider a neutron-induced reaction on the vibrational nucleus  $^{74}\text{Ge}$  which consists of a one-phonon state ( $2^+$ ) followed by a ( $0^+$ ,  $2^+$ ,  $4^+$ ) triplet of two-phonon states, and a  $3^-$  phonon

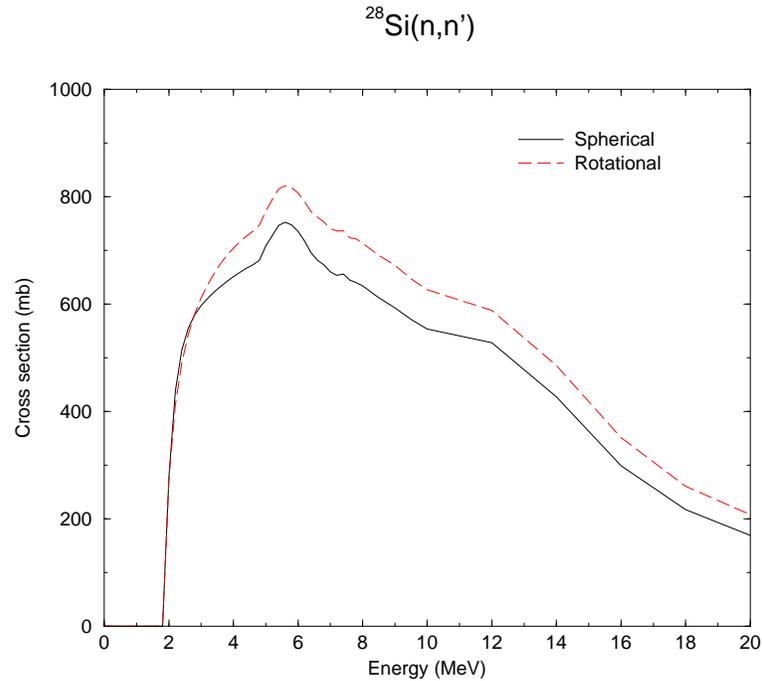


Figure 8.12: Total inelastic neutron scattering off  $^{28}\text{Si}$  for a spherical and a deformed OMP.

state. The coupling scheme as stored in *structure/deformation/exp/z032* is automatically adopted. The following input file is used:

```
#
# General
#
projectile n
element ge
mass 74
energy energies
#
# Output
#
outexcitation n
outdiscrete y
filediscrete 1
```

In Fig. 8.13, the calculated inelastic scattering to the first discrete state is plotted.

### 8.3.12 Sample 12: Inelastic spectra at 20 MeV: Direct + Preeq + GR + Compound

For pre-equilibrium studies, it may be worthwhile to distinguish between the various components of the emission spectrum. This was already mentioned in sample case (1c). As an extra sample case, we compare the calculated  $^{209}\text{Bi}(n,xn)$  spectrum at 20 MeV with experimental data. This is accomplished with the following input file,

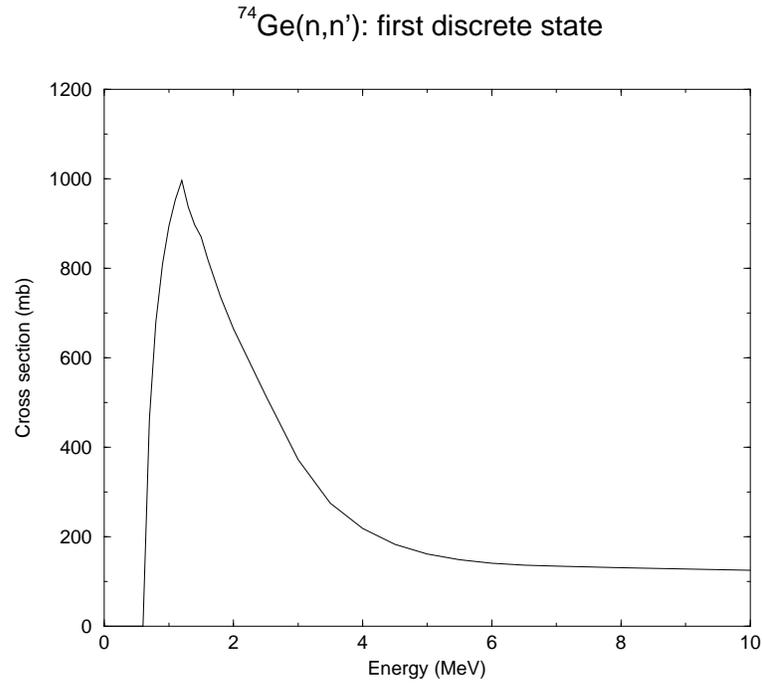


Figure 8.13: Inelastic scattering to the first discrete state of  $^{74}\text{Ge}$ .

```
#
# General
#
projectile n
element bi
mass 209
energy 20.
#
# Parameters
#
ddxmode 2
filespectrum n
```

The various components of the spectrum, and the total, as present in the file *nspec020.000.tot*, are plotted in Fig. 8.14.

### 8.3.13 Sample 13: Gamma-ray intensities: $^{208}\text{Pb}(n, n\gamma)$ and $^{208}\text{Pb}(n, 2n\gamma)$

This feature could simply have been included in the sample case on excitation functions for  $^{208}\text{Pb}$ , but in order not to overburden the description of that sample case we include it here. With the input file

```
#
# General
#
projectile n
element pb
```

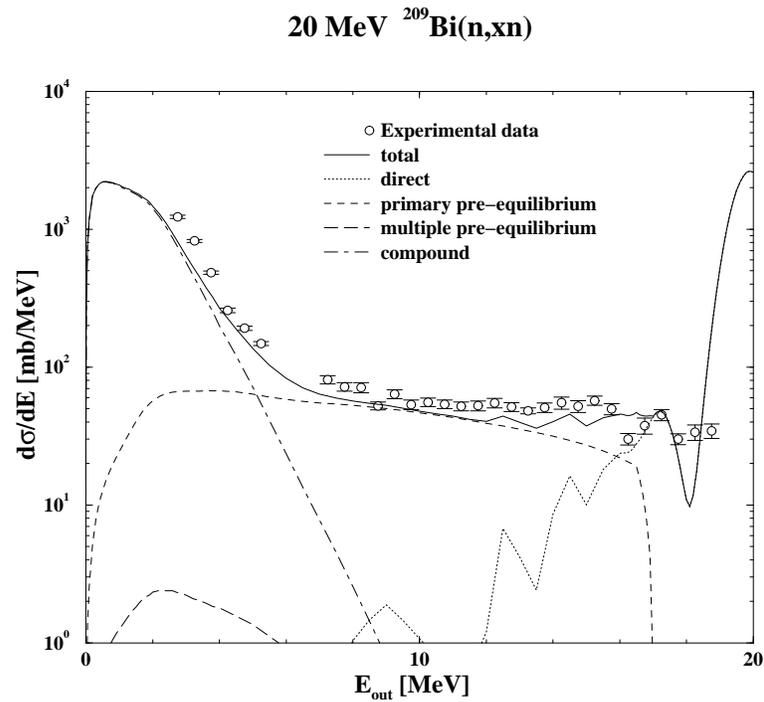


Figure 8.14:  $^{209}\text{Bi}(n,xn)$  spectrum at 20 MeV. Experimental data are obtained from [111].

```

mass 208
energy energies
#
# Parameters
#
isomer 1.e-4
maxZ 0
gnorm 0.35
Rgamma 2.2
egr      82 209 12.0    E1 1
optmodfileN 82 pb.omp
#
# Output
#
channels y
filechannels y
fileresidual y
outgamdis y

```

all discrete gamma lines are printed and stored in separate files. To avoid the production of too many data files, we have put **maxZ 0** so that only the gamma-ray production files for Pb-chain are created. Also, we include a special OMP with the file *pb.omp* and we set **isomer 1.e-4** to allow for gamma decay of some rather short-lived levels. Experimental data exists for the  $^{208}\text{Pb}(n, n'\gamma)$  cross section for level 1 to level 0 and the  $^{208}\text{Pb}(n, 2n'\gamma)$  cross section for level 2 to level 0 and for level 1 to level 0. These data have been

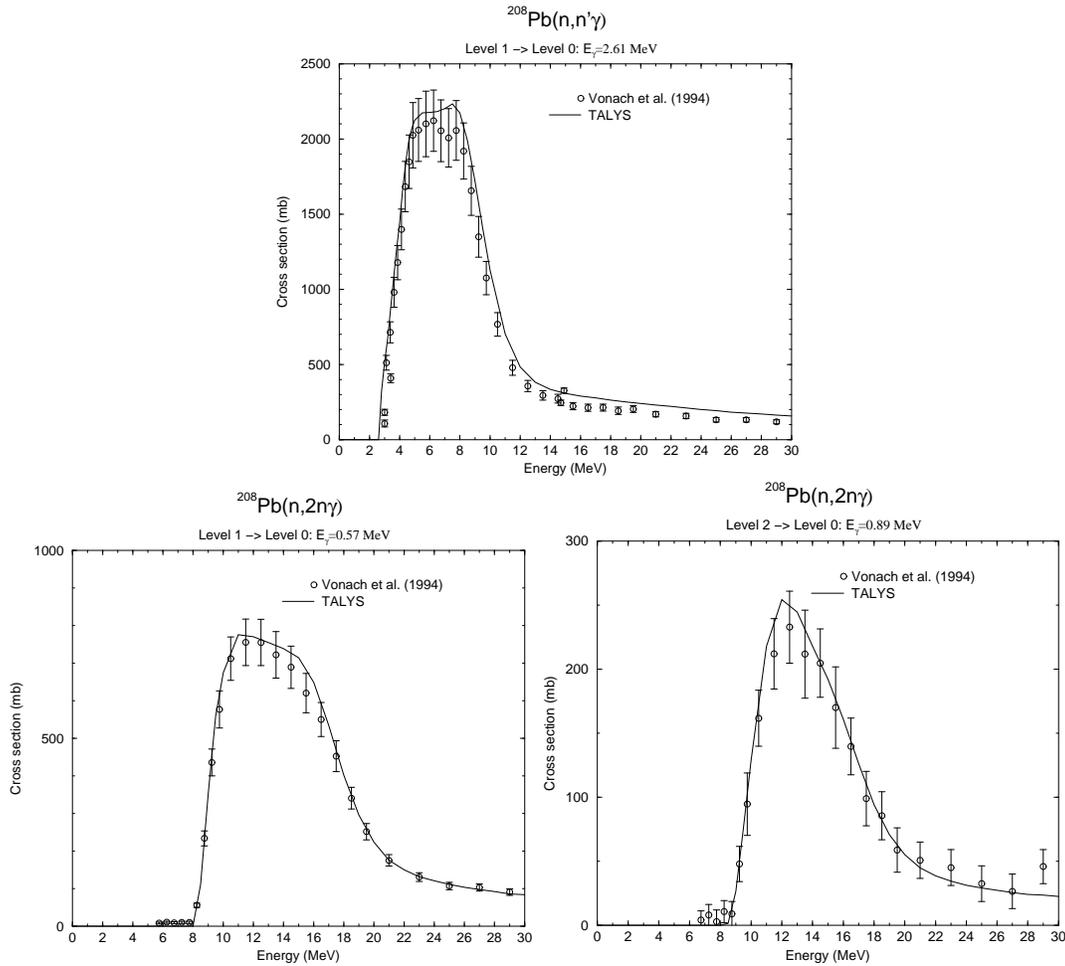


Figure 8.15: Gamma-ray production lines for a few transitions in  $^{208}\text{Pb}(n,n')$  and  $^{208}\text{Pb}(n,2n)$  reactions. The experimental data are from [112].

plotted together with the results of the calculated files *gam082208L01L00.tot*, *gam082207L02L00.tot* and *gam082207L01L00.tot*, in Fig. 8.15.

### 8.3.14 Sample 14: Fission yields for $^{238}\text{U}$

In this sample case we compute fission fragment/product mass/isotope yields.

#### Case 5a

The fission fragment mass yield curve is determined for neutrons on  $^{238}\text{U}$  at an incident energy of 1.6 and 5.5 MeV (these incident energies are given in the file *energies*). The following input file is used:

```
#
# General
#
projectile n
```

```

element u
mass 238
energy energies
#
# Parameters
#
fismodel 1
fismodelalt 4
maxband 0
ldmodel 1
optmod 92 238 z092a238n.omp
fisbar 92 239 6.10 1
fisbar 92 239 5.90 2
fisbar 92 238 6.00 1
fisbar 92 238 5.60 2
fisbar 92 237 5.40 1
fisbar 92 237 5.60 2
fishw 92 239 0.61 1
fishw 92 239 0.40 2
fishw 92 238 0.85 1
fishw 92 238 0.50 2
fishw 92 237 0.70 1
fishw 92 237 0.42 2
m2constant 0.94
a 92 239 34.30
a 92 238 32.80
a 92 237 28.10
class2 y
#
# Output
#
filefission y
massdis y
ffevaporation y

```

The long list of input parameters is mainly needed to give a correct description of the total fission cross section. The TALYS results for the pre-neutron emission mass yields can be found in *yield001.600.fis* and *yield005.500.fis* and are given in the upper plot of Fig. 8.16. The two other plots show a comparison of the normalised yields with experimental data [103].

Since we have added the keyword *ffevaporation y* to the input, we have also calculated the fission product isotope yields. Fig. 8.17 contains the result for the production of the fission products  $^{115}\text{Cd}$  and  $^{140}\text{Ba}$ . The left plot shows the cumulative yield (obtained after adding the calculated independent yields of all beta-decay precursors). The normalised cumulative yields are compared to experimental data [104, 105] in the other two plots.

The output contains the fission cross section per fissioning nucleus both per incident energy and as excitation functions:

4b. Fission cross sections per fissioning nuclide

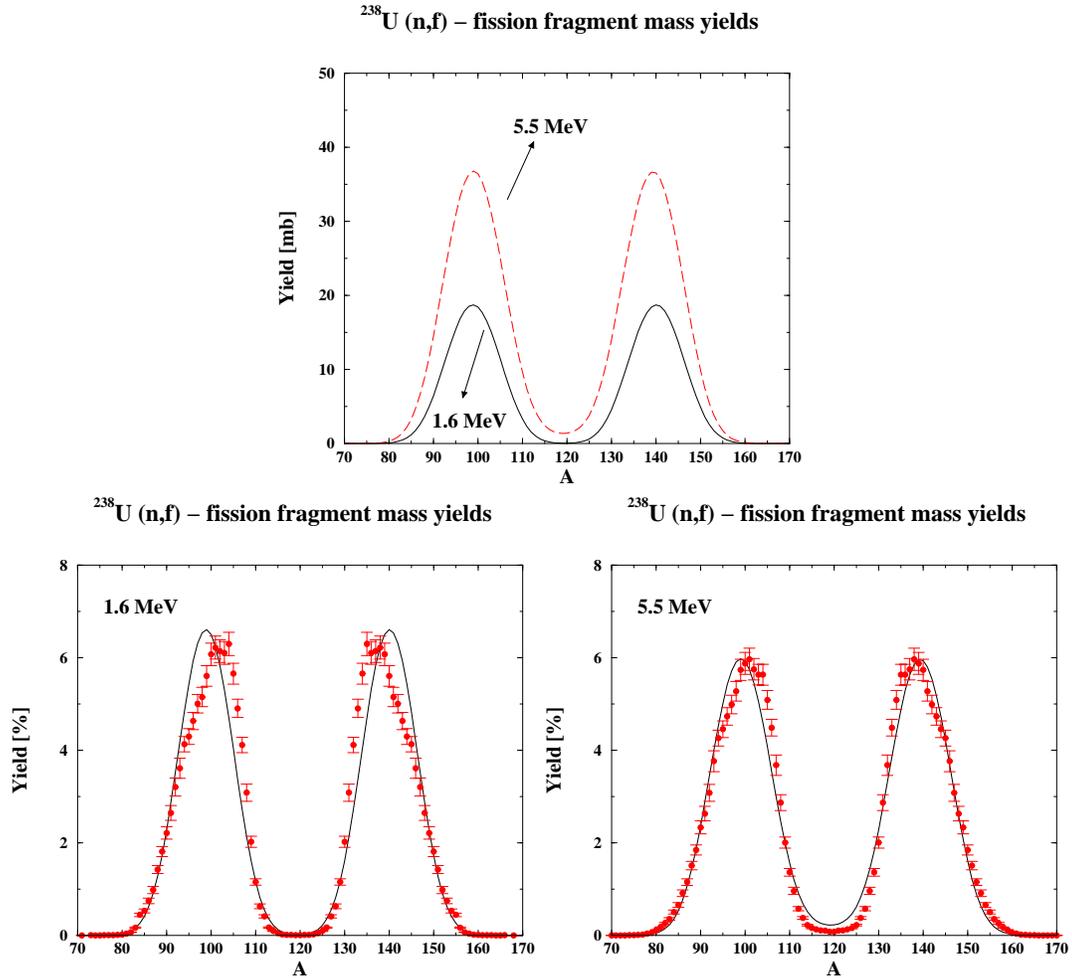


Figure 8.16: Fission fragment mass yield curves as function of the mass number  $A$ , produced by 1.6 MeV and 5.5 MeV neutrons on  $^{238}\text{U}$ . The upper curve shows the results as they are produced by TALYS and the other two plots contain the comparison with experimental data in terms of normalised yields [103].

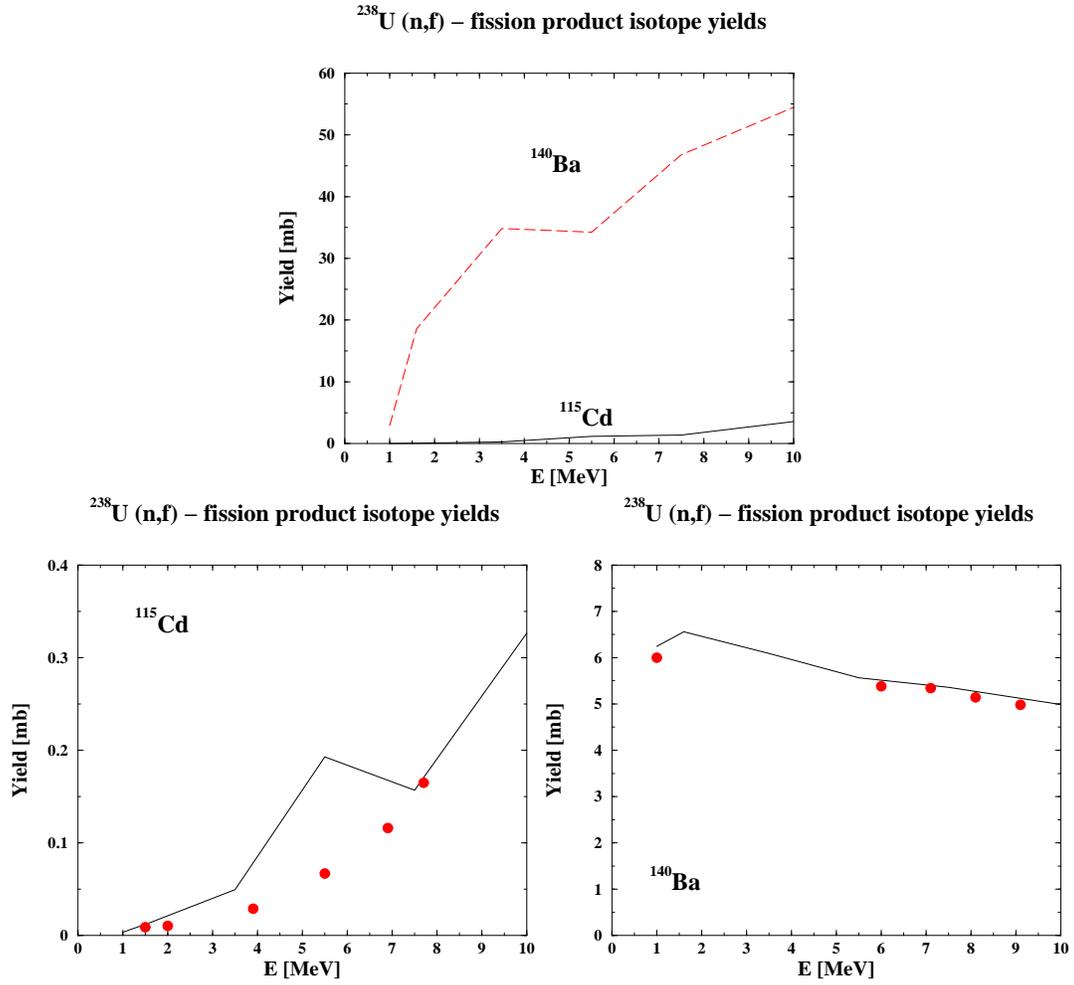


Figure 8.17: Fission product isotope yields produced by neutrons on  $^{238}\text{U}$  as function of the mass number A. The upper plot shows the results for  $^{115}\text{Cd}$  and  $^{140}\text{Ba}$  as they are produced by TALYS and the other two plots contain the comparison with experimental data in terms of normalised yields [104, 105].

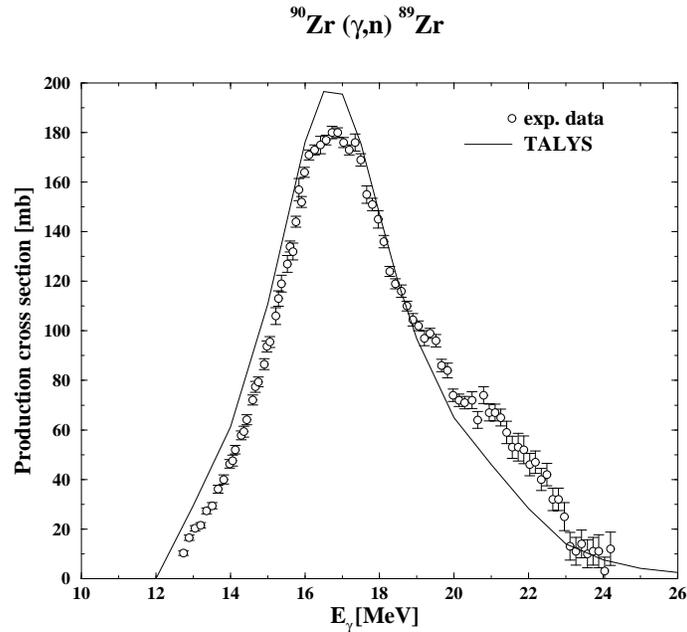


Figure 8.18: Photonuclear reaction on  $^{90}\text{Zr}$ . Experimental data are obtained from [110].

Fission cross section for  $Z=92$   $A=239$  ( $^{239}\text{U}$ )

Energy	Cross section
1.000E+00	4.68558E+01
1.600E+00	2.83741E+02
3.500E+00	5.71806E+02
5.500E+00	2.70372E+02
....	

### 8.3.15 Sample 15: Photonuclear reactions: $g + ^{90}\text{Zr}$

This sample case illustrates the capabilities of TALYS to treat photonuclear reactions. We calculate the  $(\gamma, n)$  reaction on  $^{90}\text{Zr}$  as a function of incident energy, with default model parameters, and compare the result to experimental data. The following input file is used

```
#
# General
#
projectile g
element zr
mass 90
energy energies
```

Fig. 8.18 displays the resulting production cross section of  $^{89}\text{Zr}$ , as obtained in file *rp040089.tot*.

## Chapter 9

# Outlook and conclusions

This manual describes TALYS-0.64, a nuclear reaction code developed at NRG Petten and CEA Bruyères-le-Châtel. After 6 years of development, and application in various areas [1]-[30], we decided that this Beta version of the code was ready to be released. In the coming year, we hope that extensive use of the code will result in valuable suggestions and improvements, eventually leading to the official Version 1.0.

We note that various extensions are possible for the physics included in TALYS, and some will be mentioned below. Obviously, we can not guarantee that these will all be included in the next release. This depends on the required effort, your willingness to share your extensions with us and, in the case of significant extensions, financial input from research programs that require nuclear data.

In general, the nuclear structure database can be extended with more tables produced with microscopic methods, for e.g. level densities, gamma strength functions, fission parameters, etc. Through a trivial change in the TALYS code, the impact of these ingredients on reaction calculations can immediately be tested.

The default local and global optical models that are used in TALYS are quite powerful. However, this statement holds mostly for (near-)spherical nuclides. Although we already have the full flexibility to use any deformed potential we want as specific input, it would be good to extend the optical model database for deformed nuclides as well. The same holds for light nuclides ( $A < 24$ ). Also, TALYS is already being used with microscopic OMPs, but through a non-standard use of the code. This may also be streamlined in the future. A few direct reaction items, such as the prediction of the Isobaric Analogue State, are also yet to be completed.

In the unresolved resonance range, we could implement an approach based on average resonance parameters, by allowing more flexibility per ( $l$ -dependent) transmission coefficient. This would improve especially the calculated capture and total cross sections in the tens to hundreds of keV range.

One type of observable still missing is the fission neutron spectrum. For this, both phenomenological and more physical approaches (in the latter, one would perform a loop over all excited fission fragments) are possible. Simultaneously, models for simulating the number of prompt and delayed neutrons could be included. In general, the fission parameter database for TALYS still needs to be settled. The length of some sample input files in the manual illustrates this. A general analysis of all actinides simultaneously should result in a stable, ready-to-use fission database. It is clear that the theoretical fission models themselves are also not yet mature. Inclusion of microscopic fission paths and  $l$ -dependent fission barriers may prove to be helpful extensions.

A revised complex-particle pre-equilibrium emission model by Kalbach is expected in the near future and will be included. Also, there exists a microscopic multi-step direct code, MINGUS, for quantum-mechanical pre-equilibrium calculations [82], which still needs to be merged with TALYS.

Coupling with high-energy intranuclear cascade (INC) codes is also possible, once TALYS is able to take a pre-defined population distribution as the starting point. The INC code would take care of energies above e.g. 200 MeV, while TALYS takes over below that cutoff energy. The well-validated pre-equilibrium and Hauser-Feshbach approach at lower energies may then lead to more precise simulated data (including isomer production), even for reactions in the GeV range.

We plan a relatively simple extension of the Hauser-Feshbach formalism to make TALYS amenable for large scale astrophysical calculations (reaction rates).

As for computational possibilities, the current day computer power enables to use nuclear model codes in ways that were previously thought impossible. Activities that are now within reach are the generation of nuclear-model based covariances with Monte Carlo methods, automatic multi-parameter fitting of all partial cross sections to the existing experimental data, and dripline-to-dripline generation of all cross sections over the entire energy and projectile range. The applications range from basic science (e.g. astrophysics) to the production of nuclear data libraries for existing and future nuclear technologies.

We are considering a complete upgrade of TALYS to Fortran90/95. For the moment, however, we have restricted ourselves to adding as much modules to TALYS as possible, using Fortran77, without letting that project interfere with the use of other programming languages. Once we feel TALYS has reached a certain level, in terms of included physics and options, that calls for a global upgrade to a more modern language, we will certainly do so and we will apply such an update to the whole code *at once*. At the moment, all authors of TALYS master at least Fortran77, which is a strong argument in favor of the present approach.

At some point, the software that transforms the TALYS results into ENDF-6 data libraries, called TEFAL [2], may also become available, although it is not yet known whether this will be released under the GPL terms that apply to TALYS.

The development of TALYS has followed the “first completeness, then quality” principle. This merely means that, in our quest for completeness, we try to divide our effort equally among all nuclear reaction types. We think that, with the exception of a few items the code is indeed *complete* in terms of predicted quantities. *Quality* is obviously a different and subjective issue, and it is certain that future theoretical enhancements as suggested above are needed to bring our computed results even closer to measurements.

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